

INVESTIGATING ANISOTROPY AND INHOMOGENEITY  
USING TOMOGRAPHIC INVERSION OF VSP TRAVELTIMES:  
VALIDATION OF ANALYTIC EXPRESSIONS FOR  
LINEARLY INHOMOGENEOUS ELLIPTICALLY  
ANISOTROPIC MODELS

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**Investigating anisotropy and inhomogeneity using tomographic inversion  
of VSP traveltimes: Validation of analytic expressions for linearly  
inhomogeneous elliptically anisotropic models**

by

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## ABSTRACT

Tomographic inversions of zero-offset and walkaway VSP data were performed using an analytical traveltime expression for a linearly inhomogeneous elliptically anisotropic model. Both isotropic and anisotropic conditions were investigated by forward and inverse modelling. It was realized that to accommodate long offsets, i.e., beyond the turning-ray offset, the analytic equation for traveltime needed to be reformulated so that only single-valued functions were obtained with offset.

A practical aspect of determining the elliptical anisotropy parameter,  $\chi$ , is in applying it in the expression for the curve that distinguishes between the downgoing and upgoing arrivals or 'turning points'. This has importance in the planning and designing of surveys, in that appropriate depths for receiver and source placements can be predetermined, with a reasonable estimation of inhomogeneity and anisotropy, to avoid acquiring data that would not be useful.

Extensively applying the algorithm to a large volume of real and synthetic data is an indication of the robustness of the methodology.

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## LIST OF SYMBOLS AND ACRONYMS

$a$	vertical velocity at zero depth
$b$	gradient (rate of increase in vertical velocity with depth)
$\chi$	ellipticity parameter
$p$	ray parameter
$\theta$	ray angle
$v$	velocity
$v_H$	horizontal velocity
$v_V$	vertical velocity
$V_x$	magnitude of horizontal ray velocity
$V_z$	magnitude of vertical ray velocity
$z$	depth
AVO	amplitude versus offset
MSL	mean sea level
3C	three-component
VD	vertical depth
VSP	vertical seismic profiling
VTI	vertical transverse isotropy
WAVSP	walkaround VSP
WVSP	walkaway VSP
ZVSP	zero-offset VSP

## CHAPTER 1: INTRODUCTION AND OVERVIEW

### 1.1 INTRODUCTION

Vertical seismic profiling (VSP) is a technique for obtaining measurements in the vicinity of a borehole by placing one or more receivers in the borehole with sources at the surface or *vice versa*. An analytical expression and algorithm was developed by Slawinski et al. (2004) using tomographic inversion of VSP traveltimes to determine the anisotropy in transversely isotropic media with a vertical axis of symmetry (VTI) by a velocity model described by three parameters  $a$ ,  $b$  and  $\chi$ , with the assumptions that

i) velocity ( $v$ ) increases linearly with depth, i.e.,  $v = a + bz$ ,

with  $a$  being the velocity at zero depth,  $b$  being the gradient which defines the rate of increase in velocity with depth,  $z$ , and

ii) anisotropy results from an elliptical velocity dependence on direction, defined by the ellipticity parameter,  $\chi$ , given by:

$$\chi := \frac{v_H^2 - v_V^2}{2v_V^2}, \quad (1.1)$$

which is a constant for all  $z$ , with  $v_H$  and  $v_V$  being the horizontal and vertical wavefront velocities, at any depth, respectively.



The following analytical expression and subsequent algorithm for traveltimes as described by Slawinski et al. (2004) was tested with acquired walkaway VSP data and found to be suitable for offset distances up to the ‘turning point’ of the ray:

$$t = \frac{1}{b} \ln \left[ \frac{a+bz}{a} \frac{1 + \sqrt{1 - p^2 a^2 (1 + 2\chi)}}{1 + \sqrt{1 - p^2 (a+bz)^2 (1 + 2\chi)}} \right], \quad (1.2)$$

where  $p$  is the ray parameter, and  $\chi$  is the ellipticity parameter defined above.

As a result of the findings that expression (1.2) was not applicable to offsets beyond the turning points of rays it was modified by Slawinski (pers. comm.) to take into account longer offsets:

$$t = \frac{1}{2b} \left[ \ln \frac{1 - \sqrt{1 - p^2 a^2 (1 + 2\chi)} + pbX}{1 + \sqrt{1 - p^2 a^2 (1 + 2\chi)} - pbX} - \ln \frac{1 - \sqrt{1 - p^2 a^2 (1 + 2\chi)}}{1 + \sqrt{1 - p^2 a^2 (1 + 2\chi)}} \right], \quad (1.3)$$

where  $a, b, \chi$  are as described above,  $p$  is the ray parameter,  $X$  is the offset.

To obtain expression (1.3), integration is performed along the offset ( $x$ )-axis giving a single-valued function of traveltimes for the ray, whereas expressing the ray by integration along the depth ( $z$ )-axis in obtaining expression (1.2) gave a nonsingle-valued

function due to the same traveltime for downgoing and upgoing signals at the same depth.

Vertical seismic profiling (VSP) data acquired offshore Newfoundland are used for the determination of  $a$ ,  $b$  and  $\chi$ , and to show the fit to both the original traveltime expression (1.2) and the reformulated expression (1.3).

A brief description on the theoretical basis of the traveltime equations is included. Synthetic data sets generated to confirm the algorithm as well as to help with the understanding of the results obtained with the real-data set used are also discussed. Our main focus, however, is on the results obtained using the real data. We show the fit of real data to the original equation on which the algorithm is based for the determination of anisotropy parameters, the justification to change the equation to accommodate longer offsets and the results of comparing forward modelling to the real data using both the original and newly derived equations. We also show the expression for the curve that distinguishes between the downgoing and upgoing arrivals or 'turning points'. This has importance in the planning and designing of surveys, since with a reasonable guess of  $a$ ,  $b$  and  $\chi$  one can determine the appropriate depths for receiver and source placements and avoid acquiring data that would not be useful.

This thesis complements the M.Sc. thesis of Chad J. Wheaton (2004) supervised by Dr. Michael A. Slawinski, entitled: Tomographic traveltime inversion for linear

inhomogeneity and elliptical anisotropy, which showed the derivation of the original traveltime expression.



## 1.2 OBJECTIVES

The objective of the thesis is to assess the fit of real data to an analytically derived traveltime expression for a linearly inhomogeneous elliptical anisotropic model, thereby

- i) validating the methodology and algorithm used,
- ii) confirming the assumptions of linear inhomogeneity and elliptical anisotropy,  
and
- iii) showing the contribution of anisotropy in modelling the real earth.

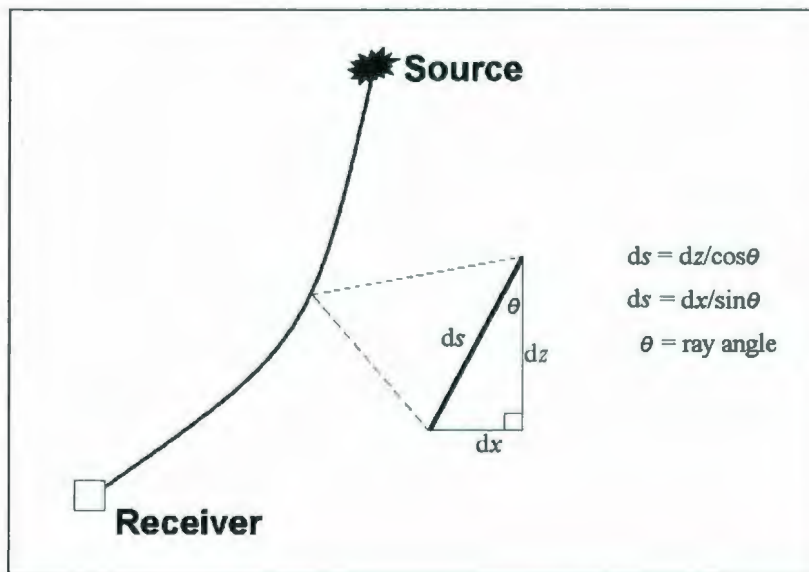
## 1.3 OVERVIEW OF THEORY

### 1.3.1 Traveltime Integral

The total traveltime along a ray, for a given source receiver pair can be written in integral form as:

$$t = \int \frac{ds}{V}, \quad (1.4)$$

where  $ds$  is the arclength element along the ray, and  $V$  is the velocity of propagation along this element, as shown in Figure 1.1.



**Figure 1.1:** Arclength of an element,  $ds$ , along a ray. The traveltime integral between source and receiver is obtained by integration along the  $x$ -axis, as shown in expression (1.5).

In the  $xz$ -plane, the arclength element,  $ds$ , is given by  $ds = dx/\sin\theta$  or as  $ds = dz/\cos\theta$ , where  $\theta$  is the ray angle. To get the traveltime integral between source at  $(0, 0)$  and receiver at  $(X, Z)$ , we integrate along the  $x$ -axis (along the  $x$ -axis a ray is expressed as a single-valued function, whereas this is not the case along the  $z$ -axis due to downgoing and upgoing rays):

$$t = \int_0^X \frac{dx}{V(\theta, z)\sin\theta}, \quad (1.5)$$

To integrate, we need to know the expression for  $V(\theta, z)$  and  $\sin\theta$  in terms of constants  $a, b, \chi, p$ , and the integration variable  $x$ .

We consider the source at  $(0, 0)$  and receiver at  $(X, Z)$  in derivations and discussions for convenience. However, the two are interchangeable, i.e., the source can be at  $(X, Z)$  and receiver at  $(0, 0)$ .



### 1.3.2 Ellipticity Parameter, $\chi$

Assuming that the ray velocity varies along the  $z$ -axis in such a way that the ratio of magnitudes of horizontal and vertical ray velocities,  $\chi$ , remains constant,  $V(\theta, z)$  is given by Slawinski (2007):

$$V(\theta, z) = V_z(z) \sqrt{\frac{1 + 2\chi}{1 + 2\chi \cos^2 \theta}}. \quad (1.6)$$

Parameter  $\chi$  is the measure of the ellipticity, given by

$$\chi := \frac{V_x^2 - V_z^2}{2V_z^2}, \quad (1.7)$$

where  $V_x$  and  $V_z$  are the magnitudes of the horizontal and the vertical ray velocities, respectively. Since the  $x$ -axis and  $z$ -axis are the symmetry axes for an ellipse, the ray velocities are equal to wavefront velocities used in expression (1.1).

### 1.3.3 Direct Traveltime Expression

If we assume further that the magnitude of the ray velocity increases linearly along the  $z$ -axis, we can write expression (1.6) as

$$V(\theta, z) = (a + bz) \sqrt{\frac{1 + 2\chi}{1 + 2\chi \cos^2 \theta}}, \quad (1.8)$$

where  $a$  and  $b$  are positive constants.

Provided the ray velocity varies in the  $z$ -direction, and not in the  $x$ -direction, the ray parameter,  $p$ , along a given ray,  $z(x)$ , which is a conserved quantity, is given by Slawinski and Webster (1999):

$$p = \cos\theta \frac{\partial}{\partial\theta} \left[ \frac{1}{V(\theta, z)} \right] + \frac{\sin\theta}{V(\theta, z)}. \quad (1.9)$$

Substituting for  $V(\theta, z)$ , we obtain:

$$p = \cos\theta \frac{\partial}{\partial\theta} \left[ \frac{1}{(a+bz)\sqrt{\frac{1+2\chi}{1+2\chi \cos^2\theta}}} \right] + \frac{\sin\theta}{(a+bz)\sqrt{\frac{1+2\chi}{1+2\chi \cos^2\theta}}} \quad (1.10)$$

$$= \frac{1}{(a+bz)\sqrt{1+2\chi}} \left( \cos\theta \frac{\partial}{\partial\theta} \sqrt{1+2\chi \cos^2\theta} + \sin\theta \sqrt{1+2\chi \cos^2\theta} \right) \quad (1.11)$$

$$= \frac{\sin\theta}{(a+bz)\sqrt{1+2\chi}\sqrt{1+2\chi \cos^2\theta}}. \quad (1.12)$$

So,

$$\sin \theta = p(a+bz)\sqrt{1+2\chi}\sqrt{1+2\chi \cos^2 \theta} . \quad (1.13)$$

And,

$$V(\theta, z) \sin \theta = (a+bz) \sqrt{\frac{1+2\chi}{1+2\chi \cos^2 \theta}} p (a+bz)\sqrt{1+2\chi}\sqrt{1+2\chi \cos^2 \theta} \quad (1.14)$$

$$= p (a+bz)^2 (1+2\chi) . \quad (1.15)$$

To proceed with integration, we must express  $z$  in terms of  $x$ .

From expression (1.13),

$$p = \frac{\sin \theta}{(a+bz)\sqrt{1+2\chi}\sqrt{1+2\chi \cos^2 \theta}} . \quad (1.16)$$

To obtain the ray parameter,  $p$ , in terms of position variables  $x$  and  $z$ , we divide both the numerator and the denominator by  $\sin \theta$ , to get

$$p = \frac{1}{(a+bz)\sqrt{1+2\chi}\sqrt{1+\frac{2\chi+1}{\tan^2 \theta}}} . \quad (1.17)$$

Squaring both sides and rearranging, we get



$$\frac{1}{\tan^2 \theta} = \frac{1 - p^2 (a + bz)^2 (1 + 2\chi)}{p^2 (a + bz)^2 (1 + 2\chi)^2}. \quad (1.18)$$

Now,  $1/\tan^2 \theta = (dz/dx)^2$ , so the above equation can be rewritten in terms of position variables,  $x$  and  $z$ , as

$$\frac{dz}{dx} = \frac{\sqrt{1 - p^2 (a + bz)^2 (1 + 2\chi)}}{p (a + bz) (1 + 2\chi)}, \quad (1.19)$$

and subsequently,

$$dx = \frac{p (a + bz) (1 + 2\chi)}{\sqrt{1 - p^2 (a + bz)^2 (1 + 2\chi)}} dz. \quad (1.20)$$

If we consider the source to be located at the origin, we can set the initial conditions as  $z(0) = 0$ , and integrate as follows:

$$\int_0^x d\varepsilon = \int_0^z \frac{p (a + b\varsigma) (1 + 2\chi)}{\sqrt{1 - p^2 (a + b\varsigma)^2 (1 + 2\chi)}} d\varsigma, \quad (1.21)$$

where  $\xi$  and  $\varsigma$  are the integration variables, to obtain

$$x = \frac{1}{pb} \left[ \sqrt{1 - p^2 a^2 (1 + 2\chi)} - \sqrt{1 - p^2 (a + bz)^2 (1 + 2\chi)} \right], \quad (1.22)$$

which describes the ray given by  $x(z)$  for elliptical velocity dependence with direction and a linear velocity dependence with depth.

We can write expression (1.22) as

$$\left( pbx - \sqrt{1 - p^2 a^2 (1 + 2\chi)} \right)^2 = 1 - p^2 (a + bz)^2 (1 + 2\chi). \quad (1.23)$$

Recalling from expressions (1.14) and (1.15) that

$$V(\theta, z) \sin \theta = p (a + bz)^2 (1 + 2\chi), \quad (1.24)$$

and substituting, we get

$$\left( pbx - \sqrt{1 - p^2 a^2 (1 + 2\chi)} \right)^2 = 1 - pV(\theta, z) \sin \theta. \quad (1.25)$$

Solving for  $V \sin \theta$ , we get

$$V(\theta, z) \sin \theta = \frac{1 - \left( pbx - \sqrt{1 - p^2 a^2 (1 + 2\chi)} \right)^2}{p}, \quad (1.26)$$

which is the denominator in the integral expressed in terms of variable  $x$ , expression (1.5). Inserting expression (1.26) into expression (1.5) and using the fact that  $p$  is constant for a given source-receiver pair, we can write

$$t = p \int_0^X \frac{dx}{1 - \left( pbx - \sqrt{1 - p^2 a^2 (1 + 2\chi)} \right)^2}. \quad (1.27)$$

By substituting

$$\zeta := pbx - \sqrt{1 - p^2 a^2 (1 + 2\chi)}, \quad (1.28)$$

we can rewrite the above equation as:

$$t = \frac{1}{b} \int_{-\sqrt{1 - p^2 a^2 (1 + 2\chi)}}^{pbx - \sqrt{1 - p^2 a^2 (1 + 2\chi)}} \frac{d\zeta}{1 - \zeta^2}. \quad (1.29)$$

Using partial fractions, we get

$$t = \frac{1}{2b} \int_{-\sqrt{1 - p^2 a^2 (1 + 2\chi)}}^{pbx - \sqrt{1 - p^2 a^2 (1 + 2\chi)}} \left( \frac{1}{1 - \zeta} + \frac{1}{1 + \zeta} \right) d\zeta. \quad (1.30)$$



Integrating, we get

$$t = \frac{1}{2b} \ln \frac{1+\zeta}{1-\zeta} \Bigg|_{-\sqrt{1-p^2a^2(1+2\chi)}}^{pbX - \sqrt{1-p^2a^2(1+2\chi)}}. \quad (1.31)$$

Evaluating, we obtain

$$t = \frac{1}{2b} \left[ \ln \frac{1 - \sqrt{1-p^2a^2(1+2\chi)} + pbX}{1 + \sqrt{1-p^2a^2(1+2\chi)} - pbX} - \ln \frac{1 - \sqrt{1-p^2a^2(1+2\chi)}}{1 + \sqrt{1-p^2a^2(1+2\chi)}} \right], \quad (1.32)$$

which is equation (1.3).

Using the identity for hyperbolic functions

$$\tanh^{-1} \zeta = \frac{1}{2} \ln \frac{1+\zeta}{1-\zeta}, \quad (1.33)$$

we can write

$$t = \frac{\tanh^{-1} \left[ \frac{pbX - \sqrt{1-p^2a^2(1+2\chi)}}{b} \right] + \tanh^{-1} \sqrt{1-p^2a^2(1+2\chi)}}{b}. \quad (1.34)$$

Expression (1.34) is equivalent to expression (1.3). It allows us to obtain the traveltimes for a signal between a given source-receiver pair along an elliptical arc using the property that the ray parameter,  $p$ , is constant and unique for a particular ray in a laterally homogeneous continuum.

#### 1.3.4 Ray Parameter, $p$

To find the expression for  $p$  that corresponds to the source at  $(X, 0)$  and the receiver at  $(0, Z)$ , we use the fact that  $p$  is a constant since, for a given source receiver pair in a laterally homogeneous continuum,  $p$  is a conserved quantity along the ray.

Recalling expression (1.22) ,

$$x = \frac{1}{pb} \left[ \sqrt{1 - p^2 a^2 (1 + 2\chi)} - \sqrt{1 - p^2 (a + bz)^2 (1 + 2\chi)} \right],$$

we can write, (Slawinski, 2009):

$$X = \frac{1}{pb} \left[ \sqrt{1 - p^2 a^2 (1 + 2\chi)} - \sqrt{1 - p^2 (a + bZ)^2 (1 + 2\chi)} \right]. \quad (1.35)$$

Solving for  $p$ , we obtain

$$p = \frac{2X}{\sqrt{[X^2 + (1 + 2\chi)Z^2] [(2a + bZ)^2(1 + 2\chi) + b^2X^2]}}. \quad (1.36)$$

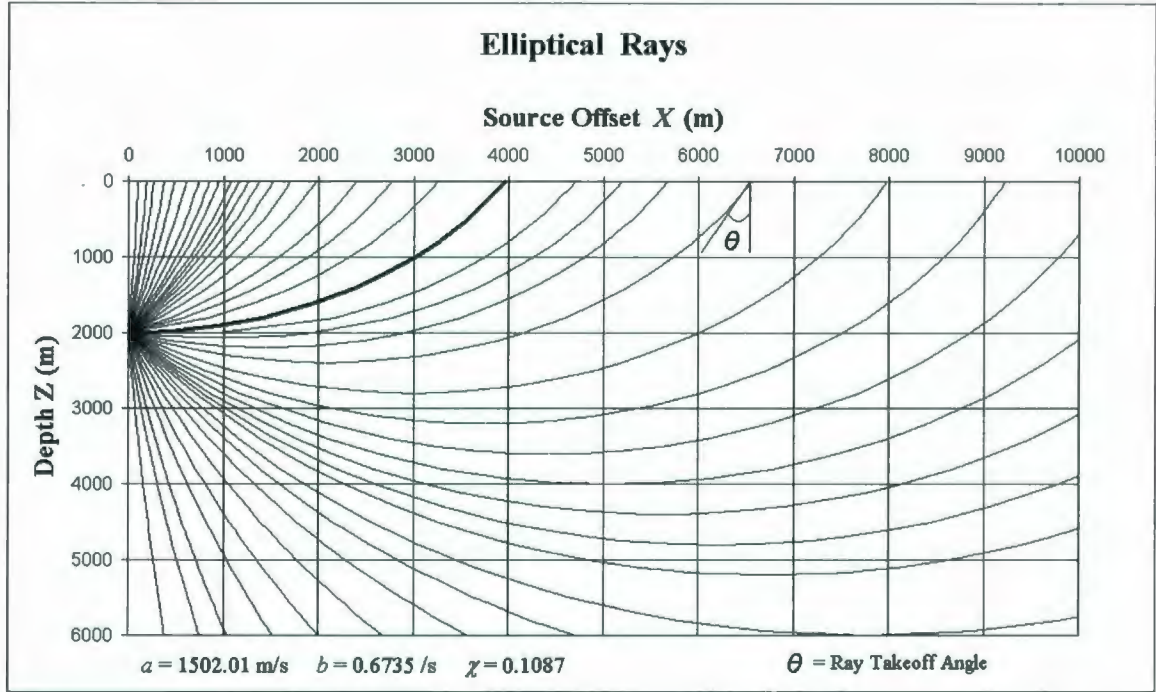
Using expression (1.36) we can obtain  $p$ , which is constant and unique for a particular choice of source-receiver pair. We can then use expression (1.34) to obtain the traveltime for a signal between the source and receiver.

### 1.3.5 Elliptical Rays - Downgoing and Upgoing Signals (Turning Points)

For traveltime measurements, the receiver in the borehole can be reached by a downgoing or an upgoing signal travelling along an elliptical arc.

If the source is directly above a given receiver, the takeoff ray angle for the downgoing signal is  $\theta = 0$ . As the source offset  $X$  increases, so does  $\theta$ , until the takeoff ray angle corresponds to the ray that horizontally impinges the receiver from the source at  $(X, Z)$ ; the takeoff angle is at its maximum. From that point on, the ray takeoff angle begins to decrease, and the receiver is reached by the upgoing signal travelling along an elliptical arc. For a source at an infinite horizontal distance, the receiver would be reached by a ray whose takeoff angle is nearly zero - the ray is nearly vertical at takeoff. Figure 1.2 illustrates the rays for a receiver at a depth of 2000 m. The 'impinging ray' (thick curve) has a source offset of approximately 4000 m. To the left of this curve

signals at the receiver arrive from above and are downgoing. To the right of this curve signals arrive from below the receiver and are upgoing.



**Figure 1.2:** The thick curve shows the ray that horizontally impinges the receiver at (0, 2000) with the source at (4000, 0) and where  $\theta$ , the ray takeoff angle is at its maximum. For sources placed to the left of this curve, signals at the receiver arrive from above and are downgoing.  $\theta = 0$  when the source is directly above the receiver. For sources placed to the right of this curve, signals at the receiver arrive from below the receiver and are upgoing.

To find point  $x$  at depth  $Z$  at which the ray angle reaches its largest value, which is the so-called turning point, we write expression (1.36), Slawinski (2009), as



$$p(x;Z) = \frac{2x}{\sqrt{[x^2 + (1+2\chi)Z^2] [(2a+bZ)^2(1+2\chi) + b^2x^2]}}, \quad (1.37)$$

and consider its derivative. To find  $x$  that corresponds to the maximum of the takeoff angle, we set this derivative to zero and proceed to rearrange the resulting equation using the fact that  $a$ ,  $b$ ,  $\chi$ , and  $Z$  are real and  $a$ ,  $b$ , and  $Z$  are positive. Thus, we obtain the required solution:

$$x = \sqrt{\frac{1+2\chi}{b}} (2a+bZ)Z. \quad (1.38)$$

We can rewrite this solution as

$$\frac{x^2}{\left(\frac{a}{b}\right)^2 (1+2\chi)} - \frac{\left(Z + \frac{a}{b}\right)^2}{\left(\frac{a}{b}\right)^2} = 1, \quad (1.39)$$

which is an expression for an hyperbola. To find its asymptote, we set the right-hand side to zero, and solve for  $x$  to obtain

$$x = \sqrt{1+2\chi} \left( Z + \frac{a}{b} \right). \quad (1.40)$$

This is the expression for the curve that distinguishes between the downgoing and upgoing arrivals.

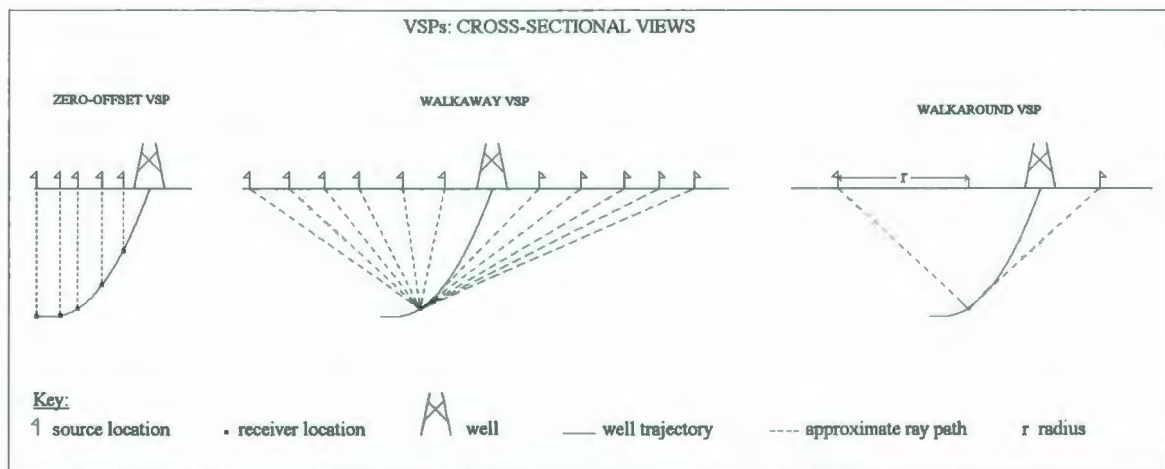
The subsurface receiver at  $(0, Z)$  is reached by the downgoing signal from the source at  $(X, 0)$ , if

$$X < \sqrt{\frac{1+2\chi}{b}(2a+bZ)Z} . \quad (1.41)$$

For the value of  $X$  equal to the right-hand side, the signal is at its deepest point when it reaches the receiver.

## CHAPTER 2: DATA ACQUISITION

Data sets from three types of VSPs with different source receiver configurations were utilized: a zero-offset VSP (ZVSP), a walkaround VSP (WAVSP) and a walkaway VSP (WVSP). Each is described below, in the context of how traveltimes are used, and illustrated in Figure 2.1.



**Figure 2.1:** Cross-sectional views of the three types of VSPs from which data were acquired. For the zero-offset VSP, sources were placed above the receivers to obtain vertically incident rays. For the walkaway VSP, sources were placed at various offset intervals linearly in a particular direction from the receiver array. In the case of the walkaround VSP, sources were arranged radially around the receiver array.

### Zero-offset VSP (ZVSP)

For this type of VSP, for a deviated well, sources are placed at various distances offset from the well and generally vertically above receiver positions in the well. Rays

are considered to be vertically incident. Traveltimes observed are used for calibrating sonic logs to seismic times. This type of VSP is also referred to as a walkabove VSP.

#### Walkaround VSP (WAVSP)

For a walkaround VSP the source is placed at various azimuths in a radial pattern around a receiver position or receiver array. A walkaround VSP provides information on azimuthal variation in traveltimes.

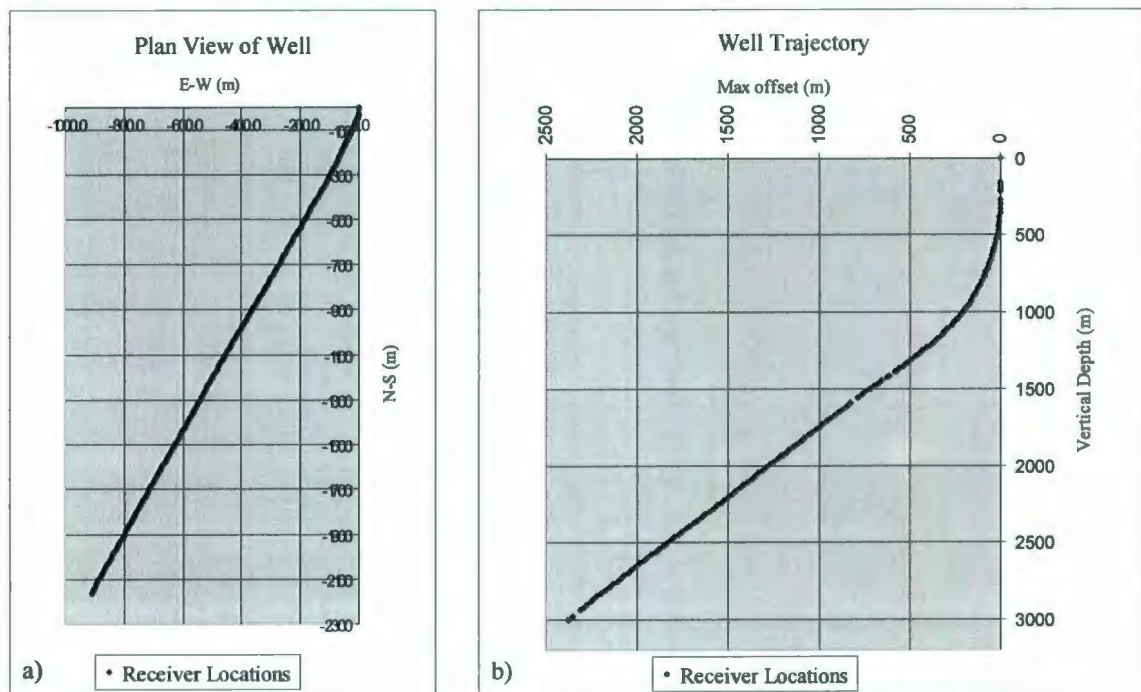
#### Walkaway VSP (WVSP)

For a walkaway VSP, sources are placed at various offset intervals in a straight line and in specified directions from the receiver position or receiver array. A walkaway VSP is used for imaging a particular horizon, studying amplitude versus offset (AVO) effects, or, as in this case, for the determination of anisotropy from observed traveltimes. It is the key '*in-situ*' field technique available for estimating the anisotropy in a medium.



## 2.1 WELL CONFIGURATION

VSP data were acquired using the well whose geometry is shown below. Figures 2.2a and 2.2b show a plan view and a cross-sectional view of the well trajectory, respectively. The well was deviated, with a maximum deviation of  $52.3^\circ$ .



**Figure 2.2a):** Plan view of well trajectory, referenced to the well location at (0, 0).

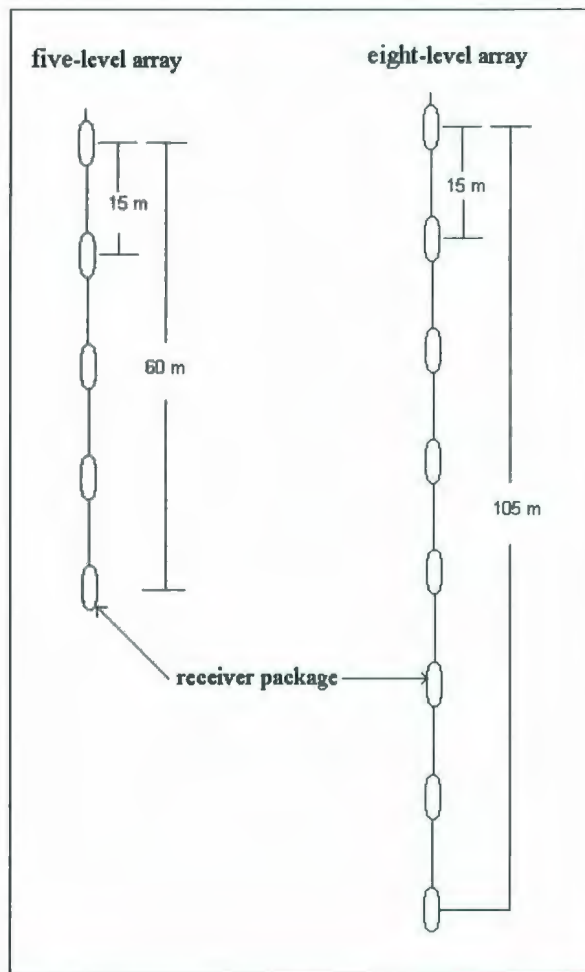
**b):** Well trajectory, with receiver locations for zero-offset VSP. Sources were placed above the receivers to obtain vertical incidence rays.

## **2.2 EQUIPMENT**

### **2.2.1 Receiver**

For the zero-offset and walkaway VSPs, the receivers consisted of packages of three-component geophones configured in a string of five packages (five-level array) with a spacing of 15.0 m between packages. Each package was composed of three orthogonally orientated and gimbal-mounted geophones to enable recording the three orthogonal components of motion.

For the walkaround VSP, the receivers consisted of an eight-level string of three-component geophones, spaced 15.0 m apart. Figure 2.3 depicts the receiver array configurations.



**Figure 2.3:** Receiver array configurations. The five-level array has a total length of 60 m. The eight-level array has a total length of 105 m. Both arrays consisted of three-component receiver packages sensitive to recording three orthogonal components of motion.

### **2.2.2 Source**

For the zero-offset and walkaway VSPs, the source consisted of a four-gun array, composed of two 100 cc plus two 150 cc air-guns, placed 6.0 m below sea level. A reference hydrophone was positioned 3.5 m above the source array for timing and monitoring purposes.

For the walkaround VSP, the source consisted of an eight-gun array, composed of four 150 cc plus four 300 cc air-guns, placed 6.0 m below sea level. A reference hydrophone was positioned 1.0 m above the source array for timing and monitoring purposes.

## **2.3 DATA ACQUIRED**

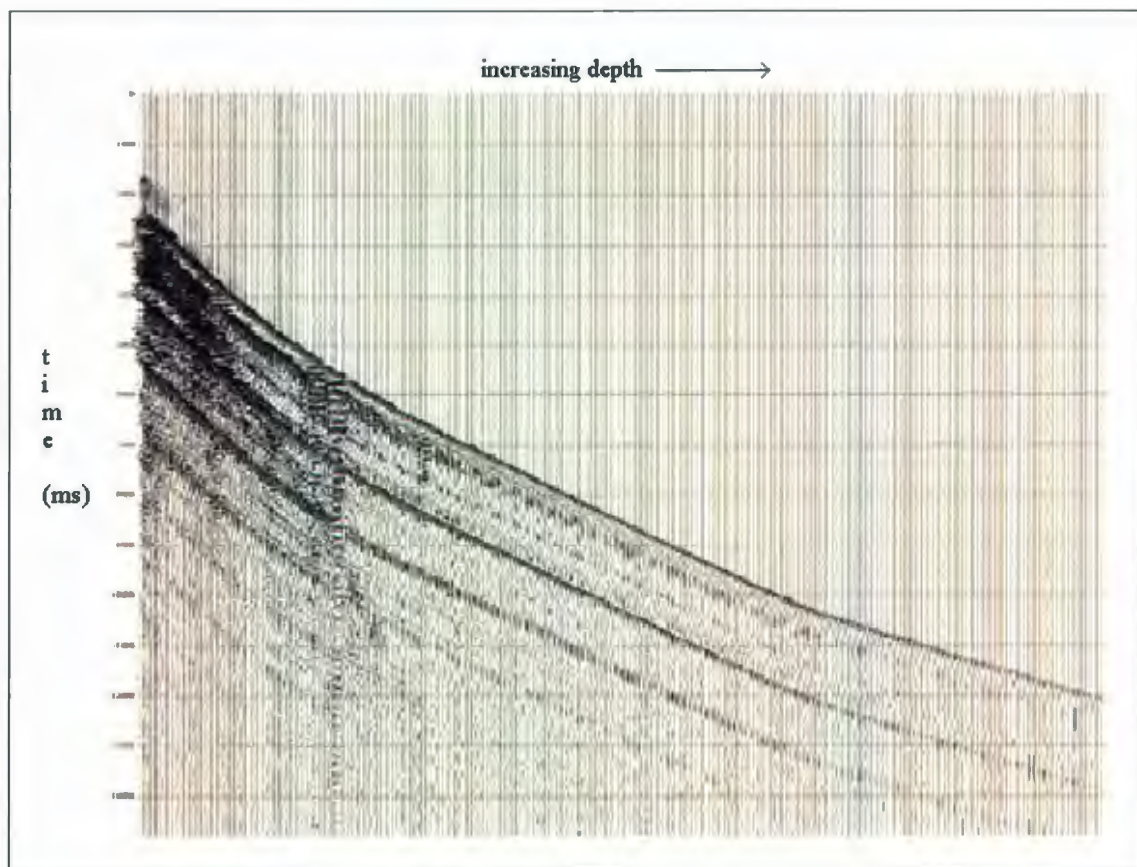
Three different types of VSP data sets were acquired in the same well: a zero-offset VSP (or walkabove VSP), a walkaround VSP, and a walkaway VSP.

### **2.3.1 Zero-offset VSP**

For the zero-offset VSP, data were acquired at 15 m intervals from the bottom of the well to the sea floor. This was achieved by pulling the receiver string up the well



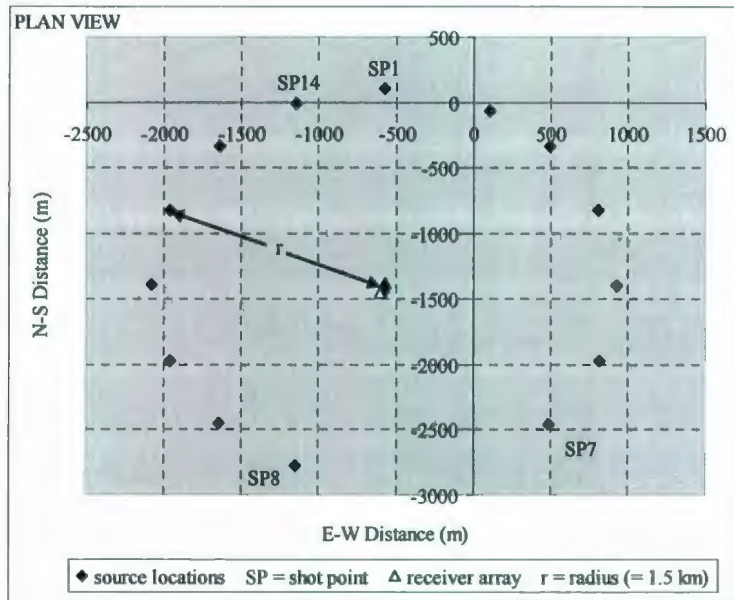
with source locations being positioned above the center receiver of the five-level array for each position. An average of seven shots were recorded for each depth level. The geophone traces within each level were subsequently aligned and stacked to produce a single trace for each depth level. Figure 2.4 shows the stack response for the z-component geophone.



**Figure 2.4:** Vertical (z-)component stacked data for zero-offset VSP.

### 2.3.2 Walkaround VSP

Data were acquired in a circular pattern, with a nearly constant radius of 1.5 km, at sea level, as shown in Figure 2.5, for the walkaround VSP. The center of the circle was positioned so as to be above the middle of the central geophone of the eight-geophone array string. Table 2.1 gives the shot and center receiver positions relative to the sea-level position of the well. The geophone string was positioned, at a fixed depth, set to be just above the base of the desired 'effective medium'. A single shot was acquired at source each location. Sixteen shot locations were planned. Fourteen were successfully acquired. The acquisition was aborted due to tool failure and impending severe weather conditions. Figure 2.6 shows the raw geophone traces for each of the shots. The raw data were rotated to obtain the responses in each of the three axes, i.e., vertical  $z$  (in the plane of the source-receiver) and horizontal  $x$  and  $y$  (orthogonal to each other). Figure 3.1 shows the oriented trace responses for each shot.

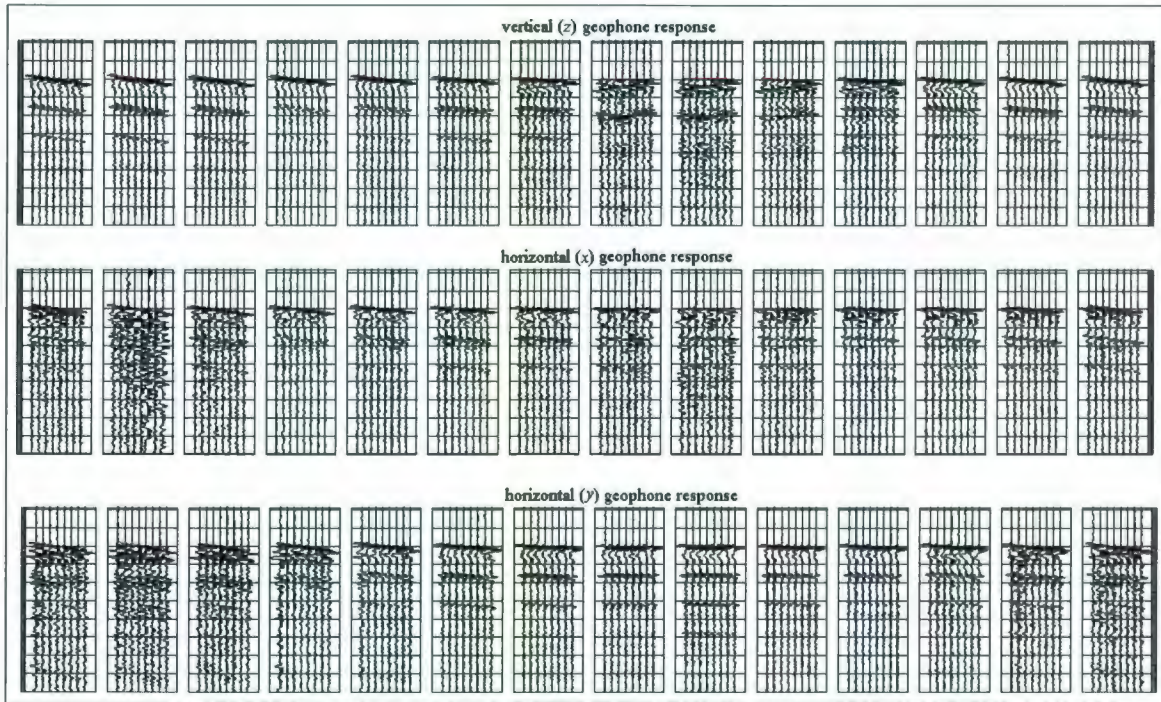


**Figure 2.5:** Walkaround VSP acquisition geometry. Sources were placed radially around the geophone array at sea level. Distances are as shown in Table 2.1.

**Table 2.1:** Walkaround VSP acquisition geometry. Sources were placed radially around the geophone array as illustrated in Figure 2.5. Distances are from the sea-level position of the well (0, 0) to each sea-level shot point (SP) position.

SHOT POINT	RECEIVER POSITION		SOURCE POSITION		SOURCE-RECEIVER
	E-W (m)	N-S (m)	E-W (m)	N-S (m)	Radial Distance (m)
SP1	-585.59	-1418.64	-574.84	104.61	1523.29
SP2	-585.59	-1418.64	107.22	-63.39	1522.07
SP3	-585.59	-1418.64	492.22	-333.39	1529.53
SP4	-585.59	-1418.64	810.22	-821.39	1518.22
SP5	-585.59	-1418.64	926.22	-1398.39	1511.95
SP6	-585.59	-1418.64	814.22	-1967.39	1503.53
SP7	-585.59	-1418.64	489.22	-2456.89	1494.38
SP8	-585.59	-1418.64	-1152.78	-2778.39	1473.30
SP9	-585.59	-1418.64	-1644.84	-2450.39	1478.69
SP10	-585.59	-1418.64	-1962.78	-1968.39	1482.86
SP11	-585.59	-1418.64	-2077.78	-1391.89	1492.43
SP12	-585.59	-1418.64	-1960.84	-822.39	1498.94
SP13	-585.59	-1418.64	-1637.78	-334.89	1510.50
SP14	-585.59	-1418.64	-1145.78	-10.39	1515.58
Sea-level position of well $x = 0.00$ , $y = 0.00$					





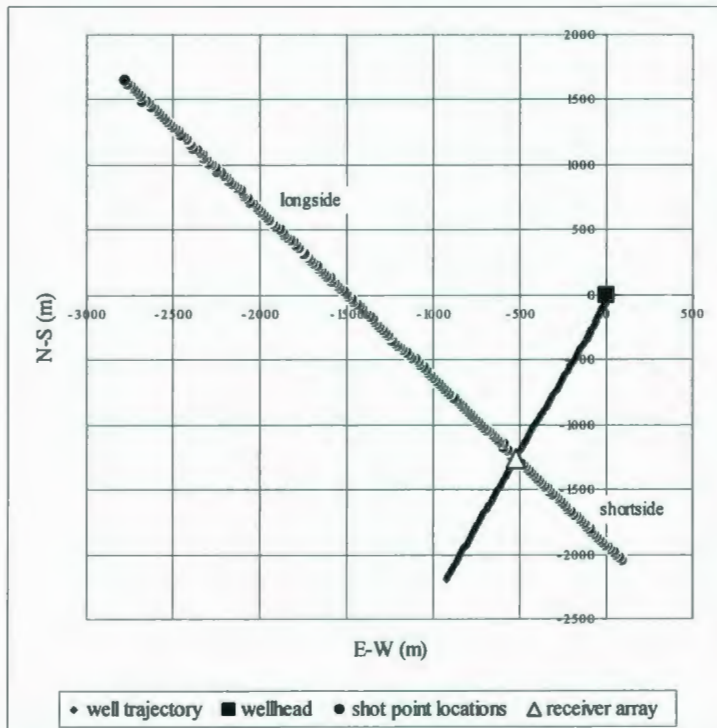
**Figure 2.6:** Walkaround VSP raw traces for each shot. The receiver array is comprised of an eight-string array, thus, eight traces are obtained for each shot. Each receiver package is composed of three orthogonally orientated geophones. Responses for all three geophones for each shot are shown above. Fourteen sources were placed radially around the receiver array,

### 2.3.3 Walkaway VSP

A plan view of the walkaway survey geometry is shown in Figure 2.7. The surveyed well was deviated  $46^\circ$  from vertical at the array center and aligned with the structural dip. A source line was positioned such as to be centered over the receiver array depth range. The source line was oriented  $61^\circ$  from the well trajectory. The source line consisted of 200 source locations with an interval of 25 m, with maximum source-receiver offsets from the center of the receiver array of 4000 m and 1000 m, in opposing



directions as shown. The source consisted of a four-gun array, composed of two 100 cc plus two 150 cc air-guns, placed 6.0 m below sea level. Receivers were comprised of three-component (3C) geophones configured in a five-level array, with a spacing of 15 m between the geophones. The five-level receiver array covered a vertical depth range from 1980 m to 2020 m (MSL). Table 2.2 provides the depths for each receiver and the source-receiver spread for both source offset directions, i.e., the longside and the shortside.



**Figure 2.7:** Walkaway VSP survey geometry, plan view. The angle between the well trajectory and source line is  $60.7^\circ$ . The wellbore inclination is  $46.4^\circ$  at the center of the receiver array. The source line consisted of 200 shot point locations with an interval of 25 m, with maximum source-receiver offsets from the center of the receiver array of 4000 m (longside) and 1000 m (shortside), in opposing directions.

**Table 2.2:** Receiver depths and spreads for walkaway VSP line. Vertical depths are to each of the five receivers of the receiver array. Maximum source-receiver offset from the center of the receiver array was 4000 m for the longside and 1000 m for the shortside.

Receiver (#)	Vertical depth (m, from source )	Source-Receiver spread (m, offset)			
		Shortside		Longside	
		Far offset	Near offset	Near offset	Far offset
1	1973.92	1014.08	76.92	74.74	3964.13
2	1983.81	1008.35	66.46	66.31	3969.12
3	1993.70	1002.71	61.00	56.20	3974.14
4	2003.76	997.09	50.09	46.36	3979.26
5	2013.93	991.55	39.17	37.13	3984.40

## CHAPTER 3: DATA ACQUISITION RESULTS AND PROCESSING

### 3.1 ZERO-OFFSET VSP

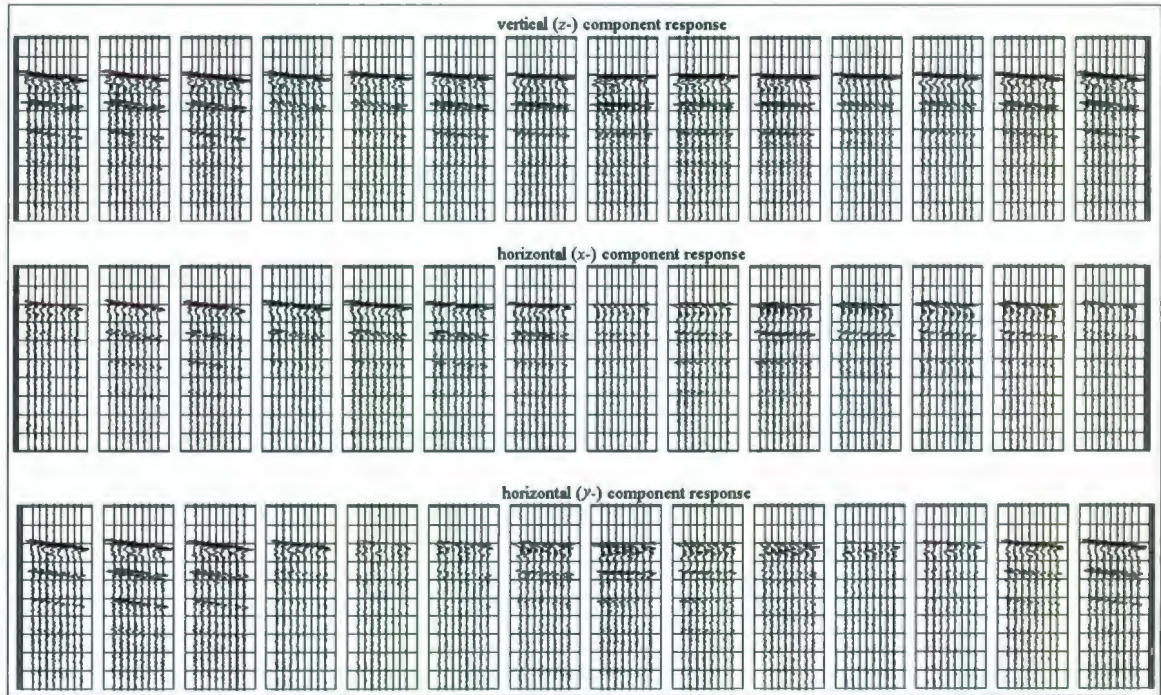
Figure 2.4 shows the stack response for the z-component geophone. Only the z-component data were utilized, since the source is always nearly vertically above the receivers, rays are nearly vertically incident and most of the particle motion for compressional or P waves lies in the vertical plane containing the source and receiver. For P waves, particle motion is longitudinal, i.e., parallel to the direction of propagation. It consists of alternating compression and extension (dilatation), along the ray and perpendicular to the wavefront.

Each trace was corrected to account for the time from the source reference hydrophone to source position (distance between reference hydrophone and source position divided by the velocity of water: 3.5 m/1524.0 m/s). An additional time correction of 1.7 ms was applied to account for instrument delay.

First-break time picks at each depth were converted to vertical times and then referenced to the datum of mean sea level (MSL), using a correction velocity of 1524 m/s (velocity of water). Table A.1 in Appendix A, lists the depths and vertical times obtained (these traveltimes will be referred to as observed times for the zero-offset VSP).



### 3.2 WALKAROUND VSP



**Figure 3.1:** Walkaround VSP, oriented trace responses after two co-ordinate rotations. First rotation was in the direction of maximum P-wave energy in the horizontal plane and the second, in the vertical plane towards the source allowing for the separation of the P-wave component from other components and establishing the arrival direction.

The raw walkaround data, Figure 2.6, were rotated to obtain the responses in each of the three axes, i.e., vertical  $z$  (in the plane of the source-receiver) and horizontal  $x$  and horizontal  $y$  (orthogonal to each other). Two co-ordinate rotations were performed: first, in the direction of maximum P-wave energy in the horizontal plane and second, in the vertical plane towards the source allowing for the separation of the P-wave component from other components, namely shear horizontal (SH) and shear vertical (SV) and



establishing the arrival direction. The methodology used is as described by DiSiena et al. (1984). Figure 3.1 shows the oriented trace responses for each shot.

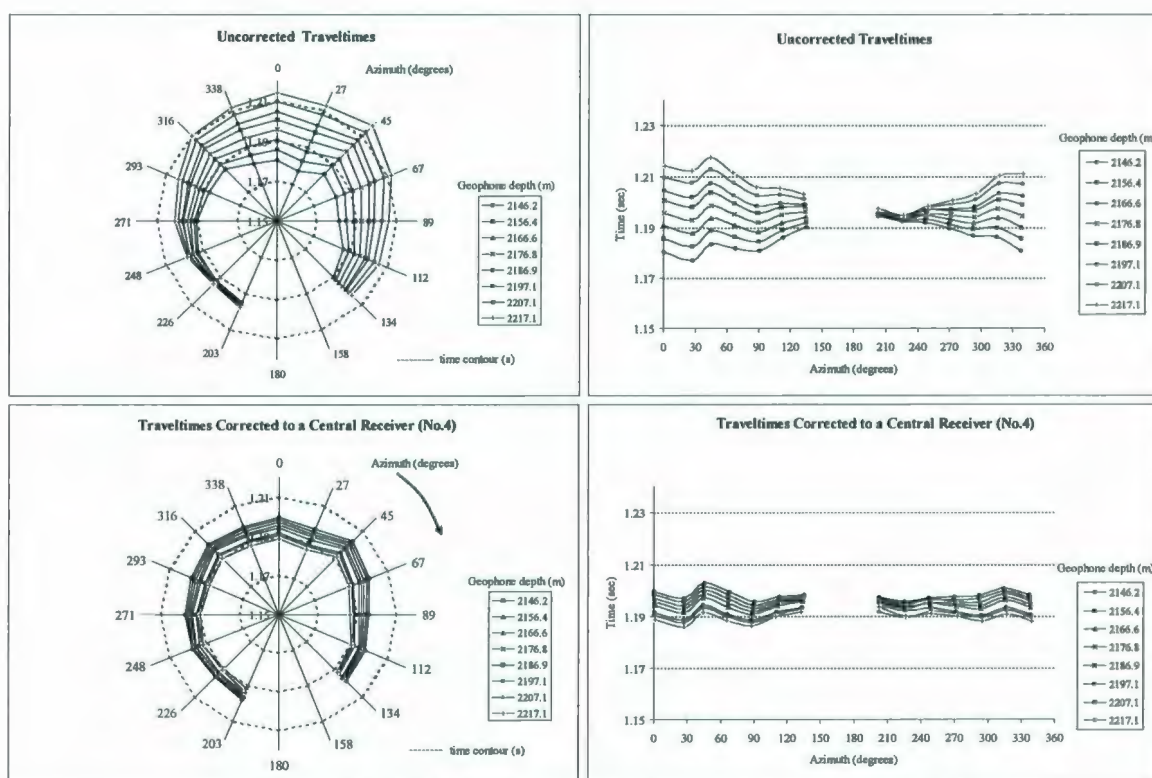
Appendix B, Table B.1, provides geophone depths and corresponding traveltimes, where the measured traveltime is the traveltime from source position to receiver position, picked as the first-break time on the oriented z-component traces. The measured traveltimes were corrected for geometry by considering the following issues:

a) Difference in traveltimes due to length of receiver array and well deviation. Each receiver is at a slightly different position giving a different source-to-receiver distance for the same shot. Traveltimes for the same shot, therefore, vary, based on the source-to-receiver distance. A central receiver (Receiver No. 4, depth = 2176.8 m VD) was selected as reference, and the raw times corrected to a fixed source-receiver distance for each source. Figure 3.2a is a plot of the uncorrected traveltimes and the traveltimes after correction to the central receiver.

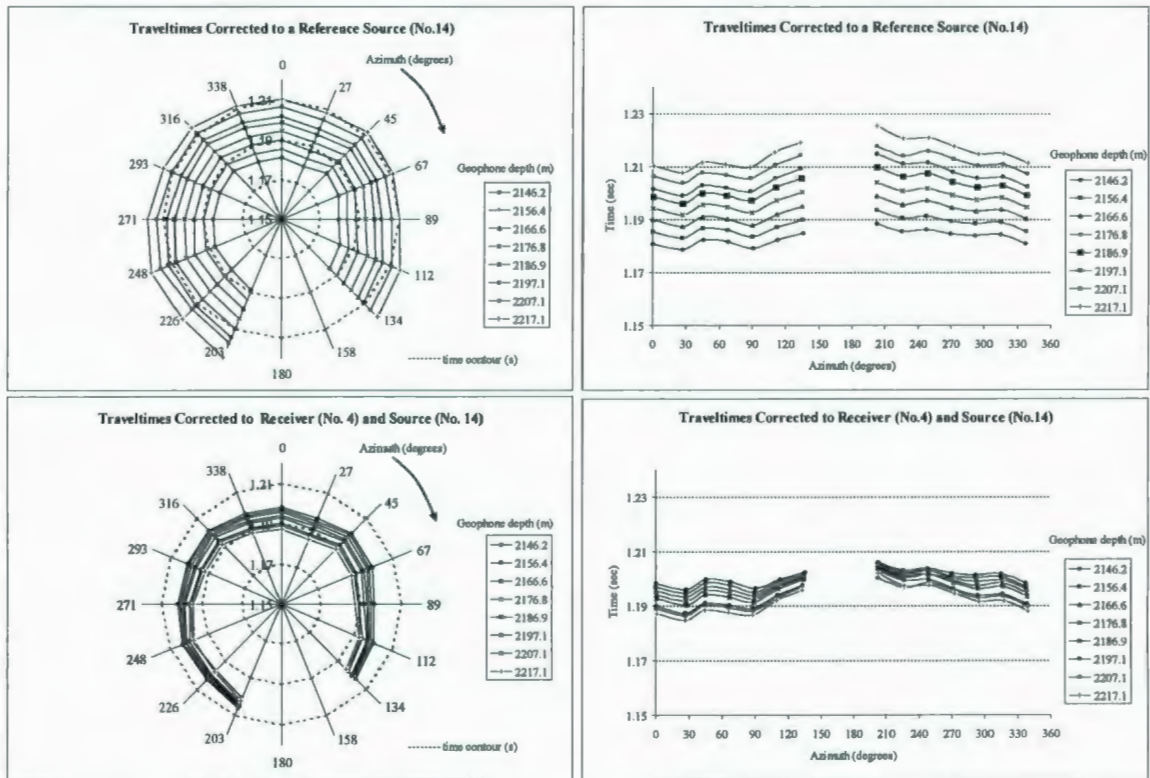
b) Each shot is also at a different physical location with a varying distance from the reference receiver. A correction was thus applied to 'normalize' the data to a fixed source-receiver distance, common to all the sources. Source No. 14 was selected for reference. Figure 3.2b is a plot of traveltimes normalized

to the source and traveltimes after correction to both the central receiver and the reference source.

Appendix B shows a sample calculation for both of the above and includes a table of measured and corrected traveltimes showing the times for all shots and associated receivers.



**Figure 3.2a:** Walkaround VSP data, traveltimes uncorrected (above) and corrected for geometry to a central receiver (below). Traveltimes were corrected for variations arising from differences between source and receiver positions due to the length of the receiver array and deviation of the well.

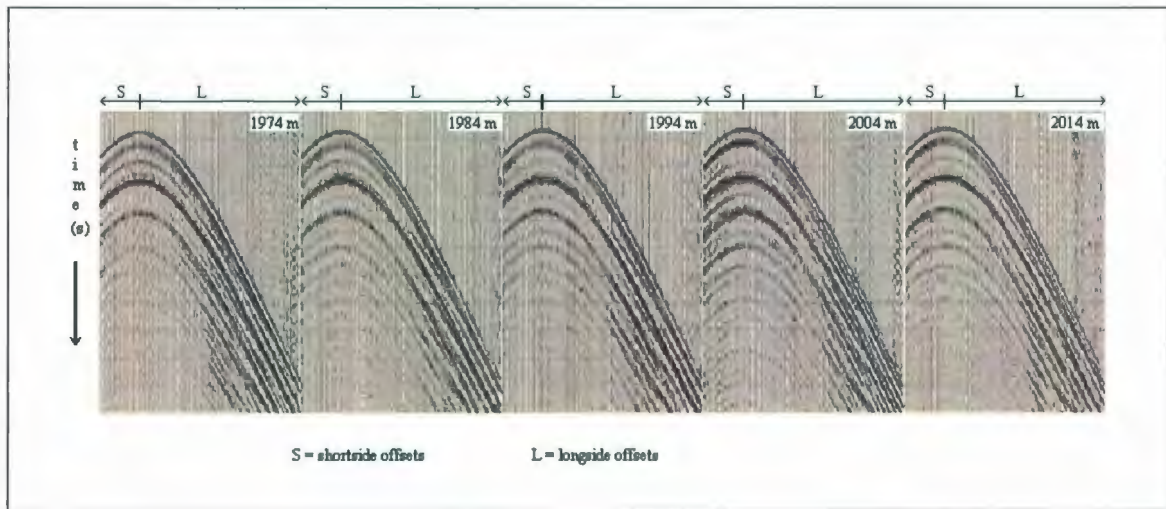


**Figure 3.2b:** Walkaround VSP data, normalized to a source to correct the traveltimes to a fixed source-receiver distance (above). Traveltimes were normalized to both a reference receiver (see Figure 3.2a) and subsequently to a reference source to obtain fully corrected traveltimes (below).

### 3.3 WALKAWAY VSP

Direct P-wave arrival times were picked at the first breaks after rotation of the vertical and horizontal components of the 3C trace data to obtain the direct P-wave component in the source-receiver plane. Data thus obtained are shown in Figure 3.3.

Appendix C shows the traveltimes obtained for each of the five receivers.

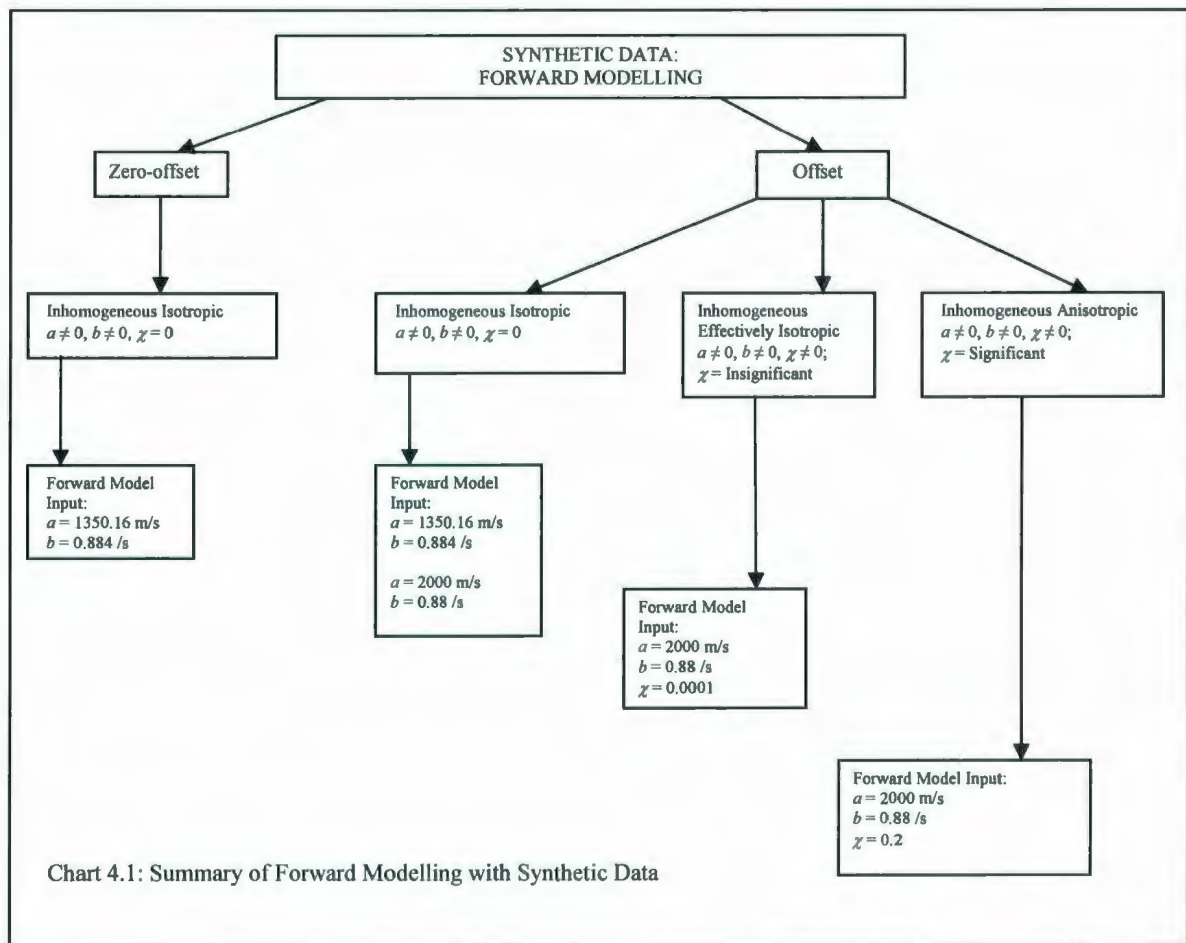


**Figure 3.3:** Direct P-wave component response in source-receiver plane for the walkaway VSP. Receiver depths are indicated at the top right of each panel. The maximum shortside offset was 1014 m, the maximum longside offset was 3984 m.



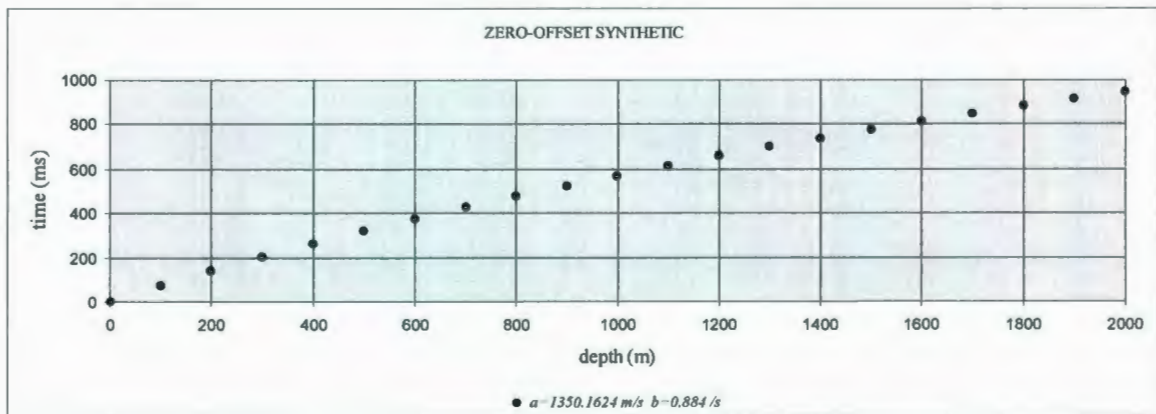
## CHAPTER 4: SYNTHETIC DATA GENERATION

In order to gain confidence in the algorithm, evaluate its limitations and understand the results obtained using real data, synthetic data sets were generated. Some of the synthetic data sets generated and used are described in this chapter and discussed in Chapter 5 and Chapter 6. Chart 4.1 provides a summary. Traveltimes obtained from forward modelling for the synthetic data sets were used as inputs to the program to confirm that the program was able to estimate  $a$ ,  $b$  and  $\chi$ .



## 4.1 ZERO-OFFSET DATA

Data were modelled using arbitrary, but ‘realistic’ values for  $a$  and  $b$  ( $a = 1350.1624$  m/s and  $b = 0.884$  /s). In order to compute the traveltimes, depths were set in the range of 1 m to 2000 m, with offset set at 1.0 m. For each depth, the ray parameter  $p$  was calculated and subsequently, the traveltime computed, as shown in Appendix D, Table D.1. Figure 4.1 displays the traveltimes obtained for the synthetic data.



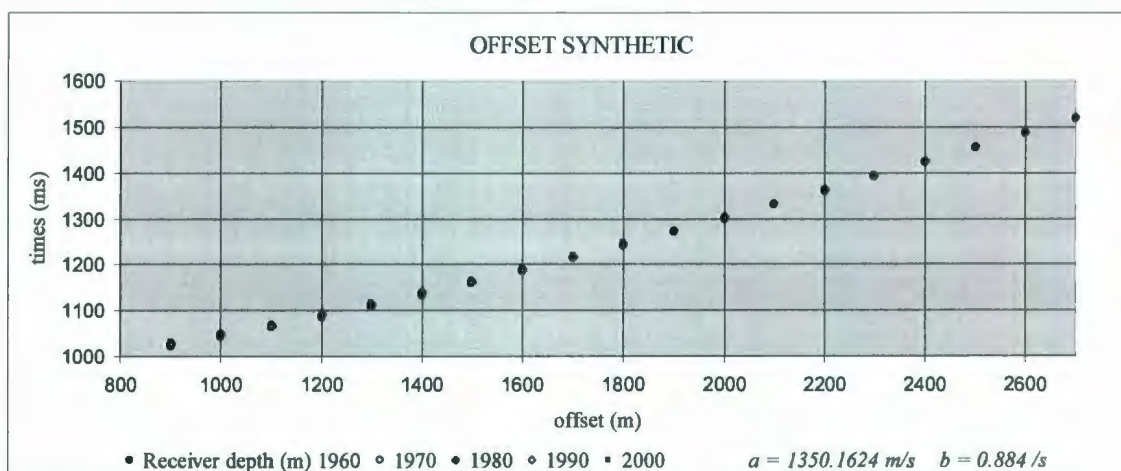
**Figure 4.1:** Zero-offset synthetic data. Traveltimes were computed using ‘realistic’ values for parameters  $a$  and  $b$ , with depths set in the range of 1 m to 2000 m, and offset set at 1.0 m. For each depth, the ray parameter  $p$  was calculated and subsequently, the traveltime computed.

## 4.2 OFFSET DATA

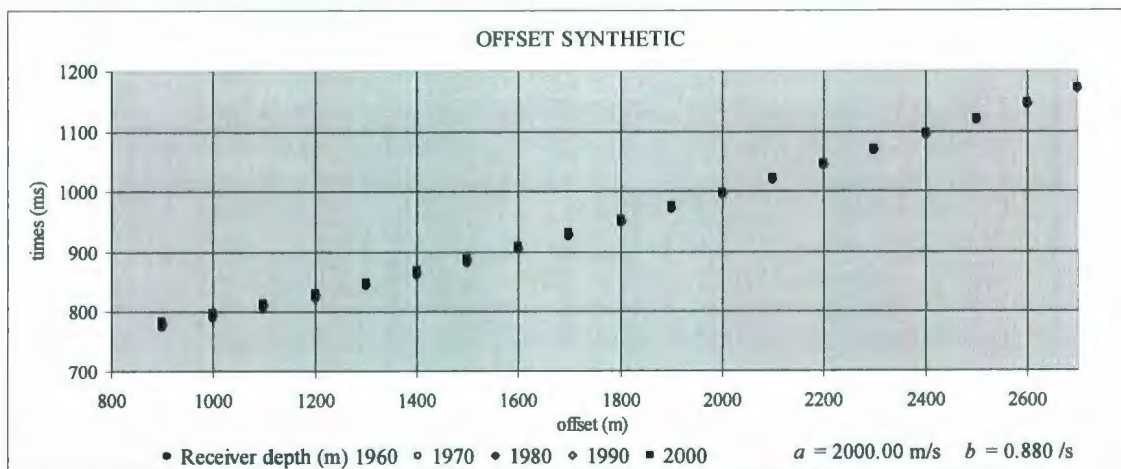
Several synthetic offset data sets were generated with values for  $a$ ,  $b$  and  $\chi$  as below:

1.  $\chi = 0$ . The same values as above for  $a$  and  $b$  ( $a = 1350.1624$  m/s and  $b = 0.884$  /s). And,  $a = 2000$  m/s,  $b = 0.88$  /s.
2. Introduction of insignificant  $\chi$ ,  $a = 2000$  m/s,  $b = 0.880$  /s and  $\chi = 0.0001$ .
3. Introduction of significant  $\chi$ ,  $a = 2000$  m/s,  $b = 0.880$  /s and  $\chi = 0.2$ .

Depths were fixed at 1960 m, 1970 m, 1980 m, 1990 m, and 2000 m. Offsets ranged from 900 m to 2700 m at 100 m intervals. For each receiver depth and offset pair, the ray parameter  $p$  was calculated and subsequently, the traveltimes computed. Appendix D, Tables D.2 to D.5, show the synthetic data traveltimes with offset obtained at each of the receiver depths. Figures 4.2 to 4.4 display the traveltimes with offset for each of the above cases.

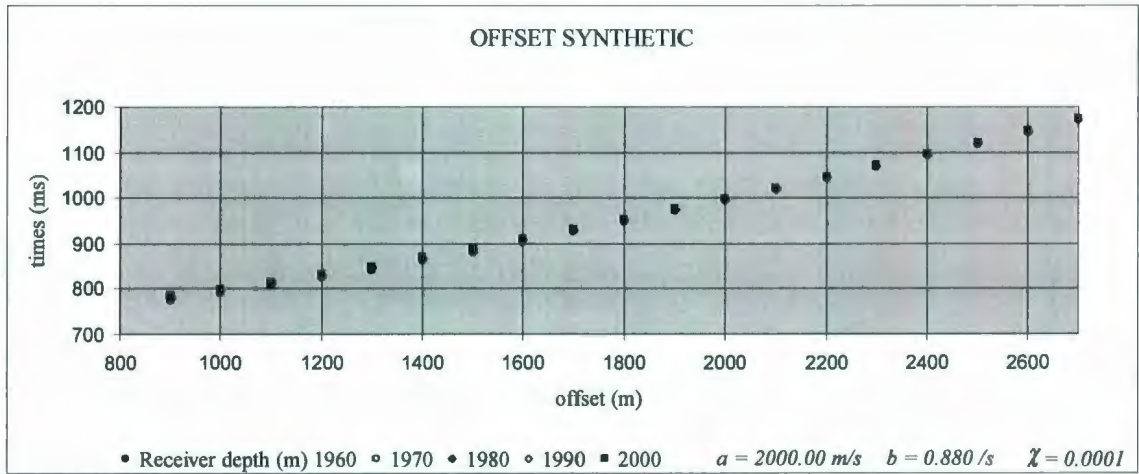


**Figure 4.2a:** Offset synthetic data. Traveltimes were computed using 'realistic' values for parameters  $a$  and  $b$  for isotropic conditions:  $\chi = 0$ ,  $a = 1350.1624 \text{ m/s}$  and  $b = 0.884 /s$ .

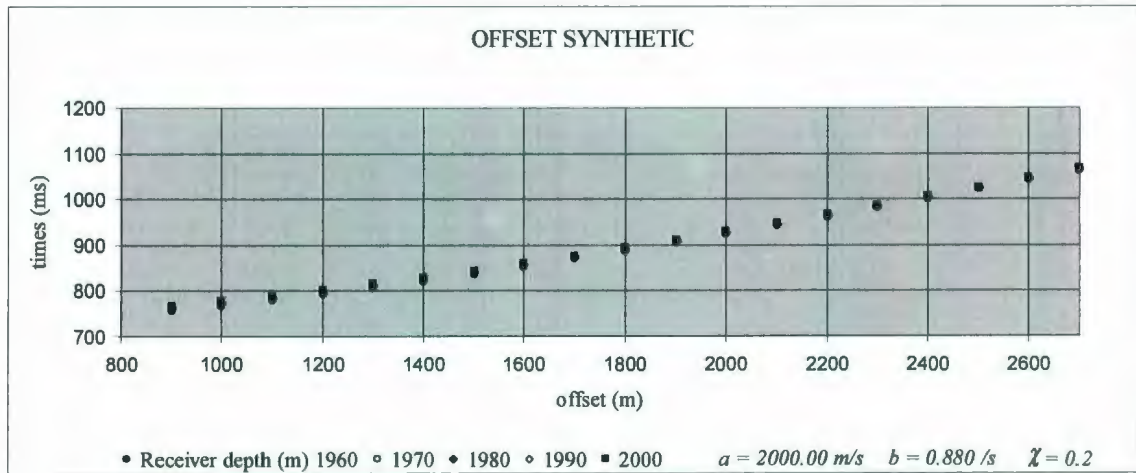


**Figure 4.2b:** Offset synthetic data. Forward modelling for traveltimes expected. Isotropic conditions:  $\chi = 0$ ,  $a = 2000.00 \text{ m/s}$  and  $b = 0.880 /s$ .





**Figure 4.3:** Offset synthetic data, with  $\chi$  set to a very small value. Insignificant  $\chi$ ,  $a = 2000.00 \text{ m/s}$ ,  $b = 0.880 \text{ /s}$  and  $\chi = 0.0001$ .



**Figure 4.4:** Offset synthetic data, with  $\chi$  set to a large value. Significant  $\chi$ ,  $a = 2000.00 \text{ m/s}$ ,  $b = 0.880 \text{ /s}$  and  $\chi = 0.2$ .

## CHAPTER 5: PROGRAM APPLICATION

### 5.1 PROGRAM DESCRIPTION

The algorithm is based on the traveltime expression derived by integrating along the  $z$ -axis. As explained in Sections 1.1 and 1.3.5, and as shown by the results, this expression was found to be valid up to the turning points of rays.

The direct-arrival traveltime between a source at the origin,  $(0, 0)$ , and a receiver located at  $(X, Z)$  in an elliptically anisotropic medium with inhomogeneity given by a constant velocity gradient, and obtained by integration along the  $z$ -axis, as described by expression (1.2), is:

$$t = \frac{1}{b} \ln \left[ \frac{a + bz}{a} \frac{1 + \sqrt{1 - p^2 a^2 (1 + 2\chi)}}{1 + \sqrt{1 - p^2 (a + bz)^2 (1 + 2\chi)}} \right].$$

An algorithm developed, by Slawinski (2003), to determine the values of  $a$ ,  $b$ , and  $\chi$  using the analytic traveltime expression above was applied to synthesized and observed field data and the results evaluated.

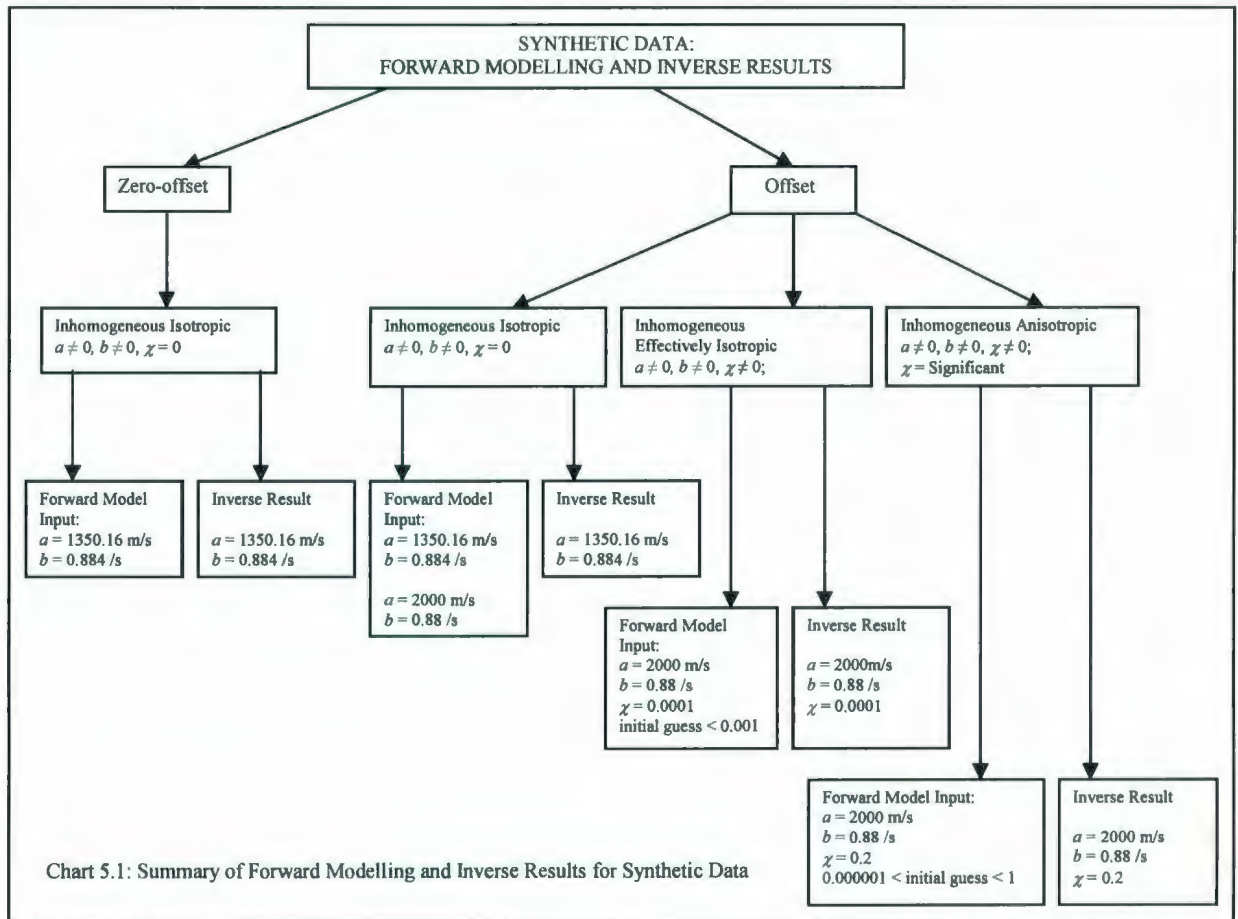
The procedure involves the regression analysis to solve for the vector composed of the model parameters to be estimated  $[a, b, \chi]$ . The objective in estimating this vector

is to minimize the sum of squared residuals for a number of observations. The residuals are defined as  $\varepsilon_i = T_i - t_i(P)$ , where  $T_i$  indicates the observed traveltime,  $t_i$  indicates the modelled traveltime and where  $P = [a, b, \chi]$  is the vector composed of the model parameters to be estimated. The traveltime expression is a nonlinear function with respect to the parameters  $a$ ,  $b$  and  $\chi$  given by  $t_i = t(X_i; a, b, \chi)$ , for a given receiver,  $X_i = [X, Z]_i$ .

The expression is linearized about initial guesses for  $a$ ,  $b$ ,  $\chi$  to enable the use of Gauss-Newton optimization. If the initial parameter estimates is denoted  $P^0$ , linearization is achieved by taking the first-order Taylor series expansion of the model centred on  $P^0$  and collecting the partial derivatives as elements of the Jacobian matrix,  $J_{ij}$ , with  $i = 1 \dots n$ , for  $n$  observations and  $j = 1, 2, 3$ , since there are three parameters. The Jacobian matrix is orthogonalized and the squared residuals are set to be minimized in solving for  $P$ . This value for  $P$  is used as the starting point for a new minimization, i.e., setting  $P = P^0$  and solving for  $P$  again. The process is iterated until an acceptable difference between two consecutive estimates is obtained giving the final estimate of  $P$ .

## 5.2 PROGRAM EXECUTION WITH SYNTHETIC DATA

Results obtained using synthetic data are summarized in Chart 5.1.





### 5.2.1 Zero-offset Data

Traveltimes computed as described in section 4.1 from forward modelling, for zero-offsets, were used as inputs. Results obtained are shown in Table 5.1. The inverse obtained is a very close estimate of the forward parameters used. This verifies that in an isotropic medium or two-parameter case, using traveltimes that vary with increasing depth, the program is able to determine the correct values.

**Table 5.1:** Forward model parameters and corresponding inverse result, isotropic medium, zero-offset data.

Forward Model:		Inverse:		Std error
$a =$	1350.1624	$a =$	1350.1623982	0.0000002179
$b =$	0.8840081182	$b =$	0.8840081172	0.0000000004

### 5.2.2 Offset Data. Isotropic Case ( $a$ and $b$ only)

Traveltimes from forward modelling for the two-parameter case, with the same values of  $a$  and  $b$  as for the zero-offset synthetic, but with fixed depth points and with offset varying as described in section 4.2, were used for the first offset synthetic generated. Results obtained are shown in Table 5.2. Again, the inverse obtained is a very close estimate of the forward parameters used. This verifies that in an isotropic medium,

or two-parameter case, using traveltimes that vary with increasing depth and varying offsets, the program is able to determine the correct values.

**Table 5.2:** Forward model parameters and corresponding inverse result, isotropic medium, offset data.

Forward Model:		Inverse:		Std error
$a =$	1350.1624	$a =$	1350.1599999	0.0000000736
$b =$	0.8840081182	$b =$	0.8840000001	0.0000000001
$a =$	2000.0000	$a =$	1999.9999999	0.0000001633
$b =$	0.8800000000	$b =$	0.8800000001	0.0000000002

### 5.2.3 Offset Data. Isotropic Case ( $a$ and $b$ with $\chi = 0.0001$ )

We now introduce  $\chi$  into the computation by setting  $\chi$  to be very small,  $\chi = 0.0001$ , so that effectively the medium can still be considered to be isotropic. Forward model parameters used and traveltimes computed are shown in Table D.4 (Appendix D).

It was found that to get the correct estimate of  $\chi$ , the initial guess must be close to the real value of  $\chi$ . Results obtained with different initial guesses used for  $\chi$  are shown in Table 5.3. If the initial guess for  $\chi$  is set at the program's default value of 0.15 or is more than an order of a magnitude larger than the true value, then erroneous estimates of

$\chi$  are obtained. To test this further,  $\chi$  was set to 0.2 in the forward model and inverses with different initial guesses for  $\chi$  were determined as described in the next section.

**Table 5.3:** Isotropic case. Forward model parameters and corresponding inverse results. Initial guess must be close to the real value of  $\chi$  otherwise erroneous estimates of  $\chi$  are obtained.

Forward Model: $a = 2000$ m/s $b = 0.88$ /s $\chi = 0.0001$						
Initial guess for $\chi$	Inverse					
	$a$	$b$	$\chi$	$a$	Std error $b$	$\chi$
0.00001	2000.0000000000	0.8800000000	0.00010000000000	0.000000000036605	0.000000000000050	0.000000000000006
0.0001	2000.0000000000	0.8800000000	0.00010000000000	0.000000000036745	0.000000000000050	0.000000000000006
0.0002	2000.0000000000	0.8800000000	0.00010000000000	0.000000000036407	0.000000000000049	0.000000000000006
0.001	2000.0000000000	0.8800000000	0.00010000000000	0.000000000036534	0.000000000000050	0.000000000000006
0.01	1999.0452425635	1.0214756716	0.02000000000000	1072.636572541470	1.502230009405290	0.187355079856705
0.1	2011.3831762326	0.9960483381	0.20000000000000	3301.455476564300	4.462177461117350	0.596034792545728
0.15	2027.0340674882	0.9727653926	0.30000000000000	4623.930334625430	6.155176718867170	0.848081928220989
0.2	2045.5807848963	0.9465424877	0.40000000000000	5897.423768138920	7.745744511062770	1.096957680275070
0.5	2143.3370118166	0.8149485213	1.00000000000000	11075.53712588560	13.82534253533750	2.298159089249880
1	2164.3678578951	0.7853808634	2.00000000000001	14618.80359180340	18.02044964526430	4.392562185311780

#### 5.2.4 Offset Data. Anisotropic Case ( $a$ and $b$ with $\chi = 0.2$ )

Forward model parameters used and traveltimes computed are shown in Table D.5 (Appendix D). Results obtained with different initial guesses used for  $\chi$  are shown in Table 5.4. Again we see that if the initial guess is either too small or too large, then erroneous estimates of  $\chi$  are obtained. However, given a reasonable initial guess of  $\chi$ , the program is able to determine the correct values for  $a$ ,  $b$  and  $\chi$ .



**Table 5.4:** Anisotropic case. Forward model parameters and corresponding inverse results. Initial guess must be close to the real value of  $\chi$  otherwise erroneous estimates of  $\chi$  are obtained.

Forward Model: $a = 2000 \text{ m/s}$ $b = 0.88 \text{ /s}$ $\chi = 0.2$						
Initial guess for $\chi$	Inverse			Std error		
	$a$	$b$	$\chi$	$a$	$b$	$\chi$
0.0000001	1980.85500451360	0.950111938958272	0.0524288000000000	747.11440007743400	1.0234886649109900	0.1285695465059010
0.000001	1999.87784299206	0.880131810360523	0.1999664526225400	0.3610355752542300	0.0004755848421768	0.0000616644396682
0.00001	1999.99999999996	0.8800000000000047	0.1999999999999950	0.0000000000395533	0.0000000000000521	0.0000000000000068
0.0001	1999.99999999997	0.8800000000000038	0.1999999999999960	0.0000000000380363	0.00000000000000501	0.0000000000000065
0.0002	1999.99999999997	0.8800000000000041	0.1999999999999960	0.0000000000387517	0.00000000000000510	0.0000000000000066
0.001	1999.99999999997	0.8800000000000045	0.1999999999999950	0.0000000000388022	0.00000000000000511	0.0000000000000066
0.01	1999.99999999997	0.8800000000000045	0.1999999999999950	0.0000000000384542	0.00000000000000507	0.0000000000000066
0.1	1999.99999999997	0.8800000000000045	0.1999999999999950	0.0000000000383812	0.00000000000000506	0.0000000000000066
0.15	1999.99999999997	0.8800000000000039	0.1999999999999960	0.0000000000385914	0.00000000000000508	0.0000000000000066
0.2	1999.99999999997	0.8800000000000044	0.1999999999999950	0.0000000000386759	0.00000000000000509	0.0000000000000066
0.5	1999.99999999997	0.8800000000000045	0.1999999999999950	0.0000000000385627	0.00000000000000508	0.0000000000000066
1	2102.84204264970	0.874725470565358	2.0000000000000100	10769.320593084400	13.596359035753300	3.5233547281249900

## 5.3 PROGRAM EXECUTION WITH REAL DATA

As mentioned earlier, and shown in Figure 2.7, the walkaway source line consisted of 200 source locations with an interval of 25 m, with maximum source-receiver offsets from the center of the receiver array of approximately 4000 m and 1000 m, in opposing directions. In total, for this source line, there are 1000 observations (5000 m/ 25 m x 5 = 1000), since the data were simultaneously acquired in five geophones. For convenience, we will call the data with source positions out to 4000 m, in the northwest direction, as the ‘longside’ and in the southeast directions with offsets to 1000 m, as the ‘shortside’, see Figures 2.7 and 5.1. The full data set was considered as comprised of six (6) segments for convenience, as follows, and as sketched in Figure 5.1:



Segment A: Offsets on the 'longside' from 0 to 3398 m

Segment B: Offsets on the 'shortside' from 0 to 1014 m

Segment B': Offsets on the 'longside' from 0 to 1014 m, i.e., complement to Segment B

Segment C: Offsets on the 'longside' greater than 3398 m and up to 3984 m

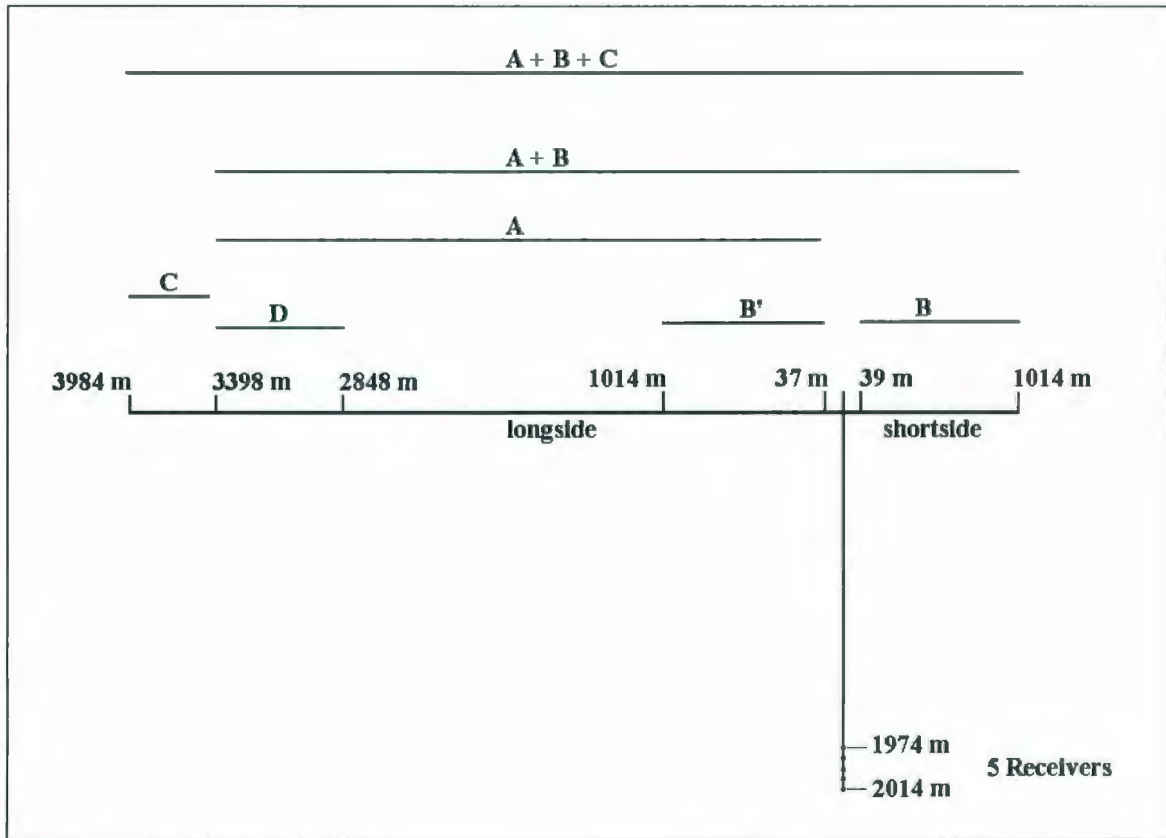
Segment D: Offsets on the 'longside' greater than 2848 m and up to 3398 m

Various permutations of the data and combinations of the above were utilized as sub-sets of the full data set as listed below:

1. Full data set:  $A+B+C$ .
2. Very far offsets omitted:  $A+B$ .
3. Longside only, shortside omitted:  $A+C$ .
4. Shortside and very far offsets omitted:  $A$ .
5. Shortside only:  $B$ .
6. Shortside complement on longside:  $B'$ .
7. Limited offset range:  $D$ .
8. Longside, longoffsets:  $D+C$ .

The full data set,  $A+B+C$ , has maximum source offset of 3984 m. Offsets greater than 3398 m, segment C in Figure 5.1, were considered as very far offsets due to the possibility of having near-horizontal arrivals or refracted arrivals from these offsets. The parameters  $a$ ,  $b$  and  $\chi$  were determined for the above segments with systematically

increasing offsets. The parameters  $a$  and  $b$  were also determined with  $\chi$  set to zero ( $\chi = 0$ ).



**Figure 5.1:** Sketch of data permutations used based on source offsets.  $A+B+C$  = full data set.  $A+C$  = longside,  $B$  = shortside.

### 5.3.1 Zero Offset

Using depths and traveltimes for the zero-offset VSP, as per Table A.1 (Appendix A), with offset set to 0.1 m, results obtained for the two-parameter case ( $a$  and  $b$  only) are shown in Table 5.5.

**Table 5.5:** Inverse result for zero-offset (vertical incidence) VSP.

		std error
$a =$	1592.258651185210	5.310555822212610
$b =$	0.575514064006845	0.007231503177721

### 5.3.2 Offset

Results obtained are tabulated and displayed as listed below. The results are discussed in Chapter 6 in the sections indicated.

#### 5.3.2.1 Isotropic Cases: Inverse Results for $a$ , $b$ , with $\chi = 0$

1. Table E.1 and Figure 5.2:  $a$ ,  $b$ , and  $\chi = 0$ , with maximum offsets increasing from 47.9 m to 3984.4 m, for all receivers, includes the longside and shortside (A+B+C). Results are discussed in section 6.3.1.

2. A subset of this data, the longside was used because of dip considerations as discussed in section 6.3.1. Table E.2 and Figure 5.3:  $a$ ,  $b$ , and  $\chi = 0$ , with maximum offsets increasing from 74.7 m to 3984.4 m, for all receivers, includes the longside only (A+C). Results are discussed in section 6.3.2. Comparing Figure 5.2 with Figure 5.3 and Table E.1 with E.2, it can be seen that values obtained for  $a$ , and  $b$  are slightly different.

3. Table E.3 and Figure 5.4:  $a$ ,  $b$ , and  $\chi = 0$ , with maximum offsets increasing from 2849.9 m to 3984.4 m, for all receivers, for the longside, longoffsets only (D+C). Results are discussed in section 6.3.4.

4. Table E.4 and Figure 5.5:  $a$ ,  $b$ , and  $\chi = 0$ , with maximum offsets increasing from 73.2 m to 1014.1 m, for all receivers, for the shortside only (B). Results are discussed in sections 6.3.1 and 6.3.4.

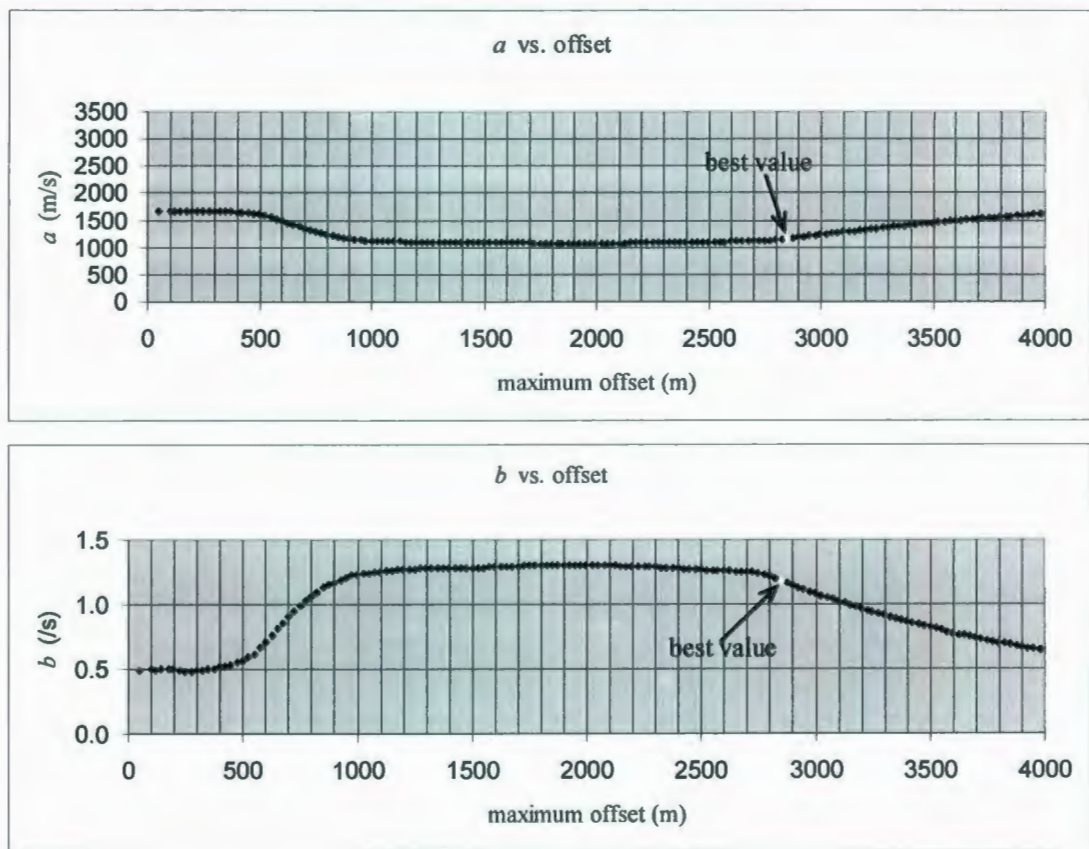
5. Table E.5 and Figure 5.6:  $a$ ,  $b$ , and  $\chi = 0$ , with maximum offsets increasing from 74.7 m to 1014.4 m, for all receivers, for the longside, shortoffsets only (B'). This is the same as Table E.2 and Figure 5.3 (from 2. above) up to the offset of 998.0 m, and is included here so that a direct comparison can be made with results for the shortside only (B). Figures 5.5 and 5.6 are combined as Figure 6.6 and discussed in section 6.3.1 and section 6.3.4.



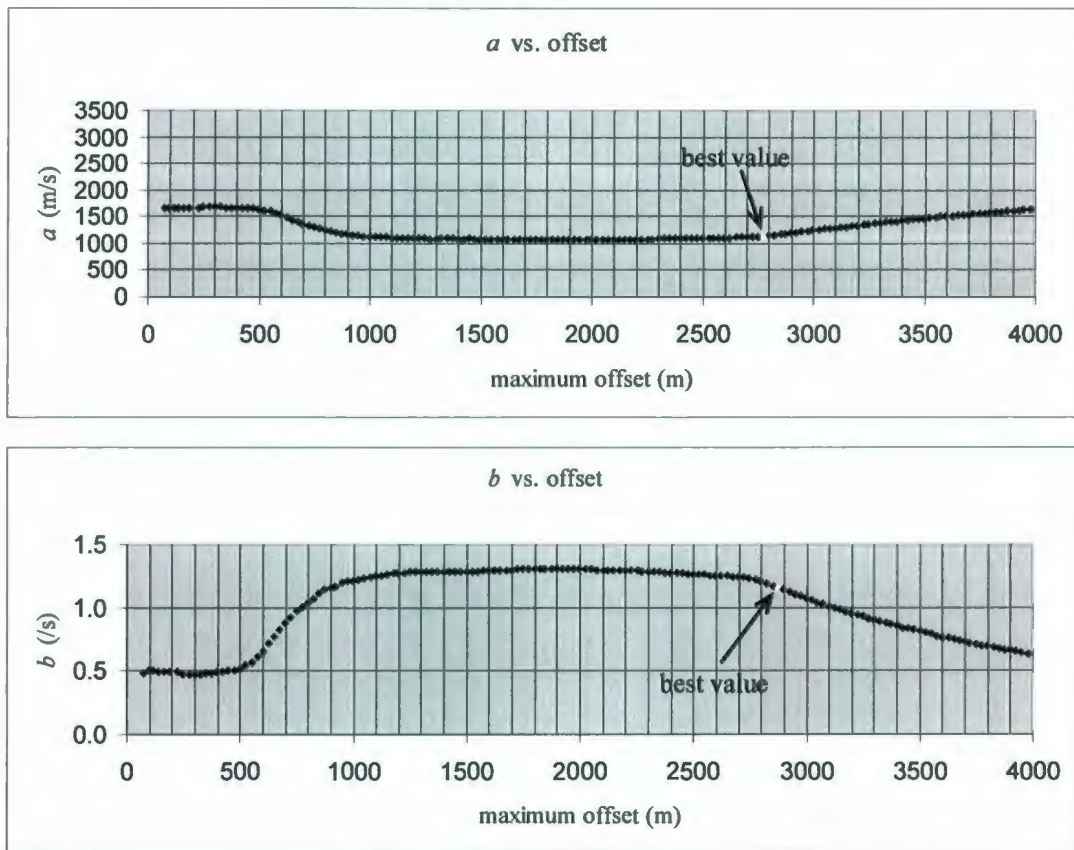
### 5.3.2.2 Anisotropic Cases: Inverse Results for $a$ , $b$ , and $\chi$

1. Table E.6 and Figure 5.7:  $a$ ,  $b$ , and  $\chi$ , for the full data set, all receivers all offsets, longside plus shortside, with maximum offsets increasing from 47.9 m to 3984.4 m (A+B+C).
2. Table E.7 and Figure 5.8:  $a$ ,  $b$ , and  $\chi$ , with maximum offsets increasing from 69.7 m to 3984.4 m, for all receivers, for the longside only (A+C). As for the isotropic case, above, a subset of this data, the longside, was used because of dip considerations. Comparing Figure 5.7 with Figure 5.8 and Table E.6 with E.7, it can be seen that values for  $a$ ,  $b$ , and  $\chi$  obtained are slightly different. Results are discussed further in sections 6.3.1, 6.3.3 and 6.3.4.
3. Table E.8 and Figure 5.9:  $a$ ,  $b$ , and  $\chi$ , with maximum offsets increasing from 2849.9 m to 3984.4 m, for all receivers, for the longside, longoffsets only (D+C). Results are discussed in section 6.3.4.
4. Table E.9 and Figure 5.10:  $a$ ,  $b$ , and  $\chi$ , with maximum offsets increasing from 99.6 m to 1014.1 m, for all receivers, for the shortside only (B). Figures 5.10 and 5.11 are combined as Figure 6.7 and discussed in section 6.3.1.

5. Table E.10 and Figure 5.11:  $a$ ,  $b$ , and  $\chi$ , with maximum offsets increasing from 69.7 m to 1014.4 m, for all receivers, for the longside, shortoffsets only (B'). This is the same as Table E.2 and Figure 5.3 (from 2. above) up to the offset of 998.0 m, and is included here so that a direct comparison can be made with results for the shortside only (B). Figures 5.10 and 5.11 are combined as Figure 6.7 and discussed in section 6.3.1.

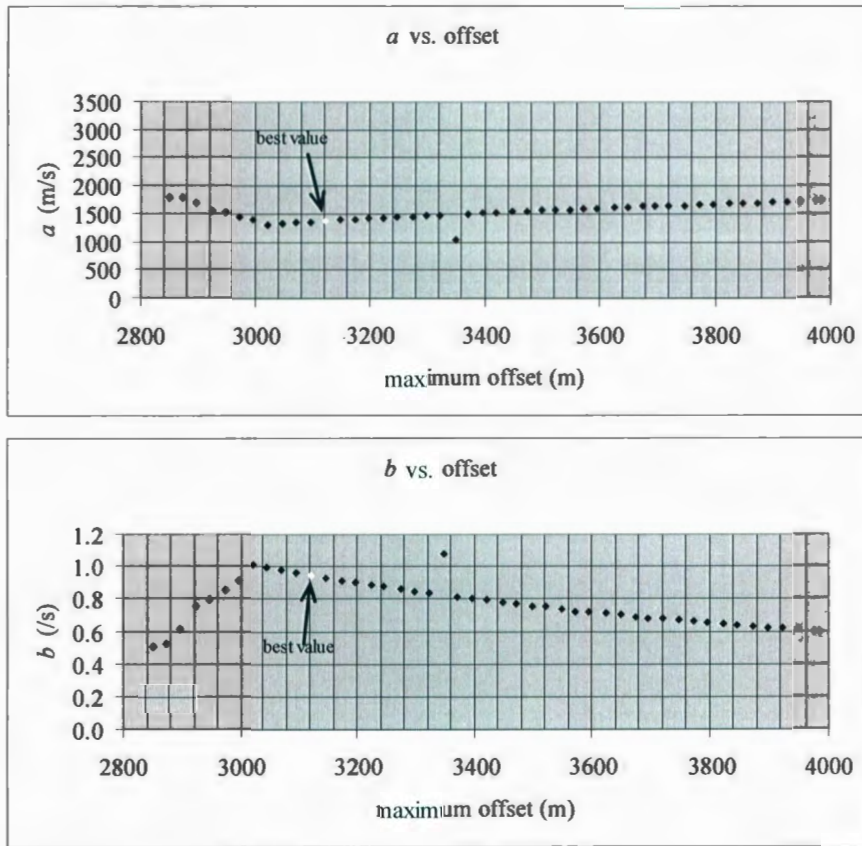


**Figure 5.2:** Display of results (from Table E.1) of  $a$ ,  $b$ , and  $\chi = 0$ , with maximum offsets increasing from 47.9 m to 3984.4 m, for all receivers, includes the longside and shortside, (A+B+C). Best values (minimum standard error) are as indicated.

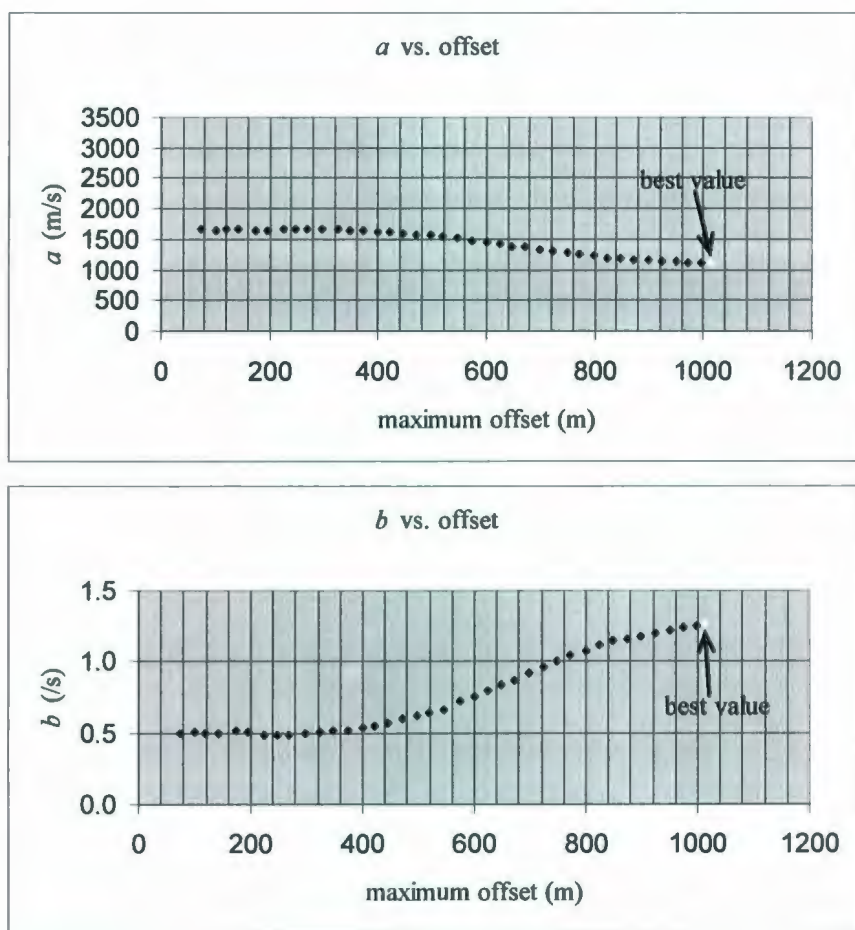


**Figure 5.3:** Display of results (from Table E.2) of  $a$ ,  $b$ , and  $\chi = 0$ , with maximum offsets increasing from 74.7 m to 3984.4 m, for all receivers, includes the longside only, (A+C). Best values (minimum standard error) are as indicated.

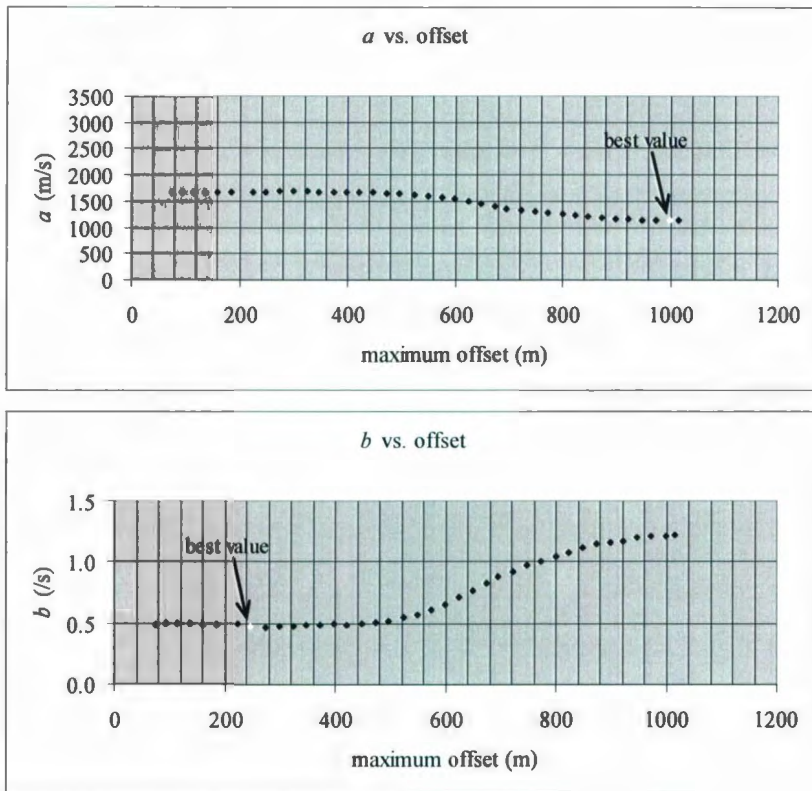




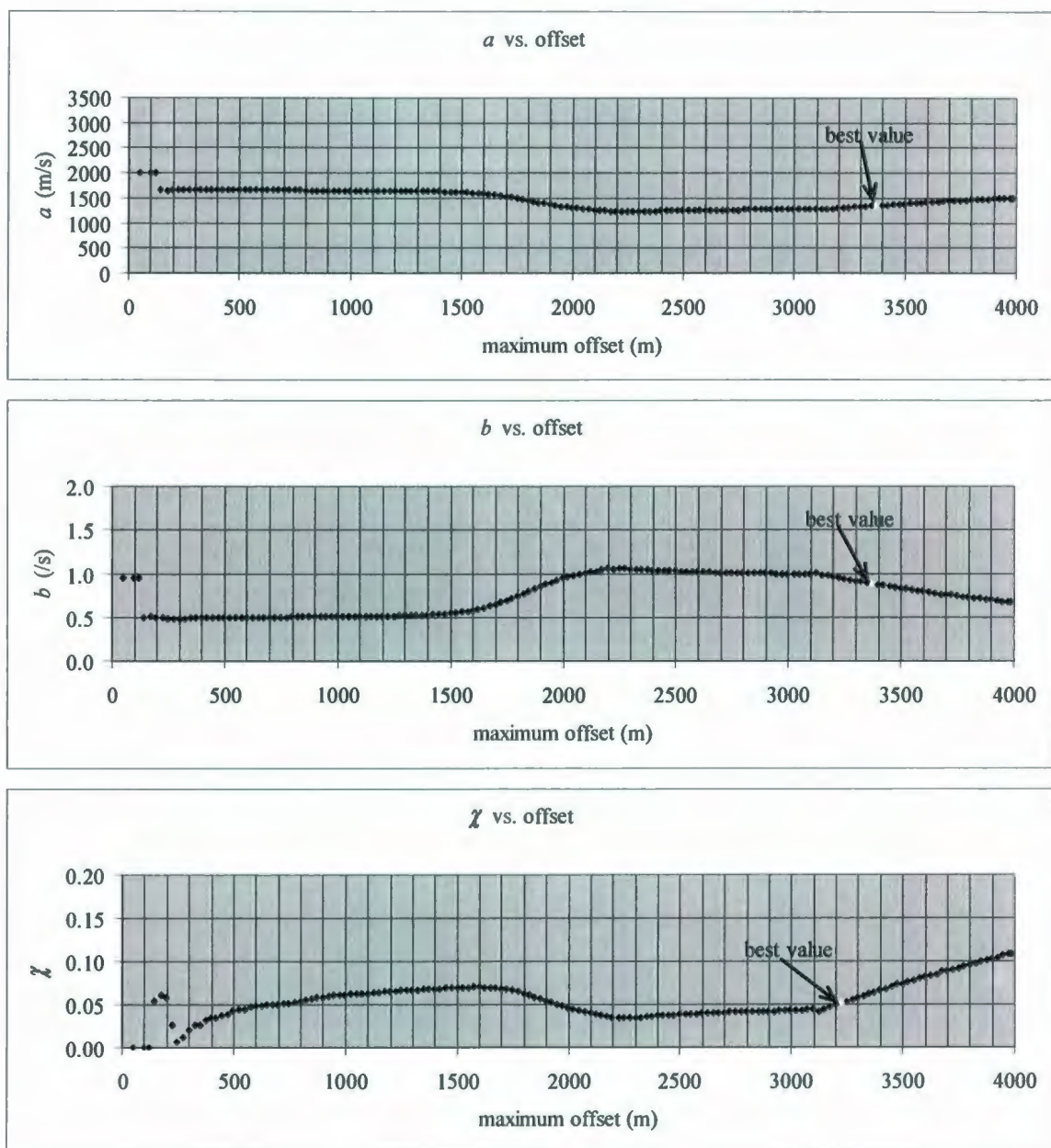
**Figure 5.4:** Display of results (from Table E.3) of  $a$ ,  $b$ , and  $\chi = 0$ , with maximum offsets 2849.9 m to 3984.4 m, for all receivers, for the longside, longoffsets only, (D+C). Best values (minimum standard error) are as indicated.



**Figure 5.5:** Display of results (from Table E.4) of  $a$ ,  $b$ , and  $\chi = 0$ , with maximum offsets increasing from 73.2 m to 1014.1 m, for all receivers, for the shortside only, (B). Best values (minimum standard error) are as indicated.

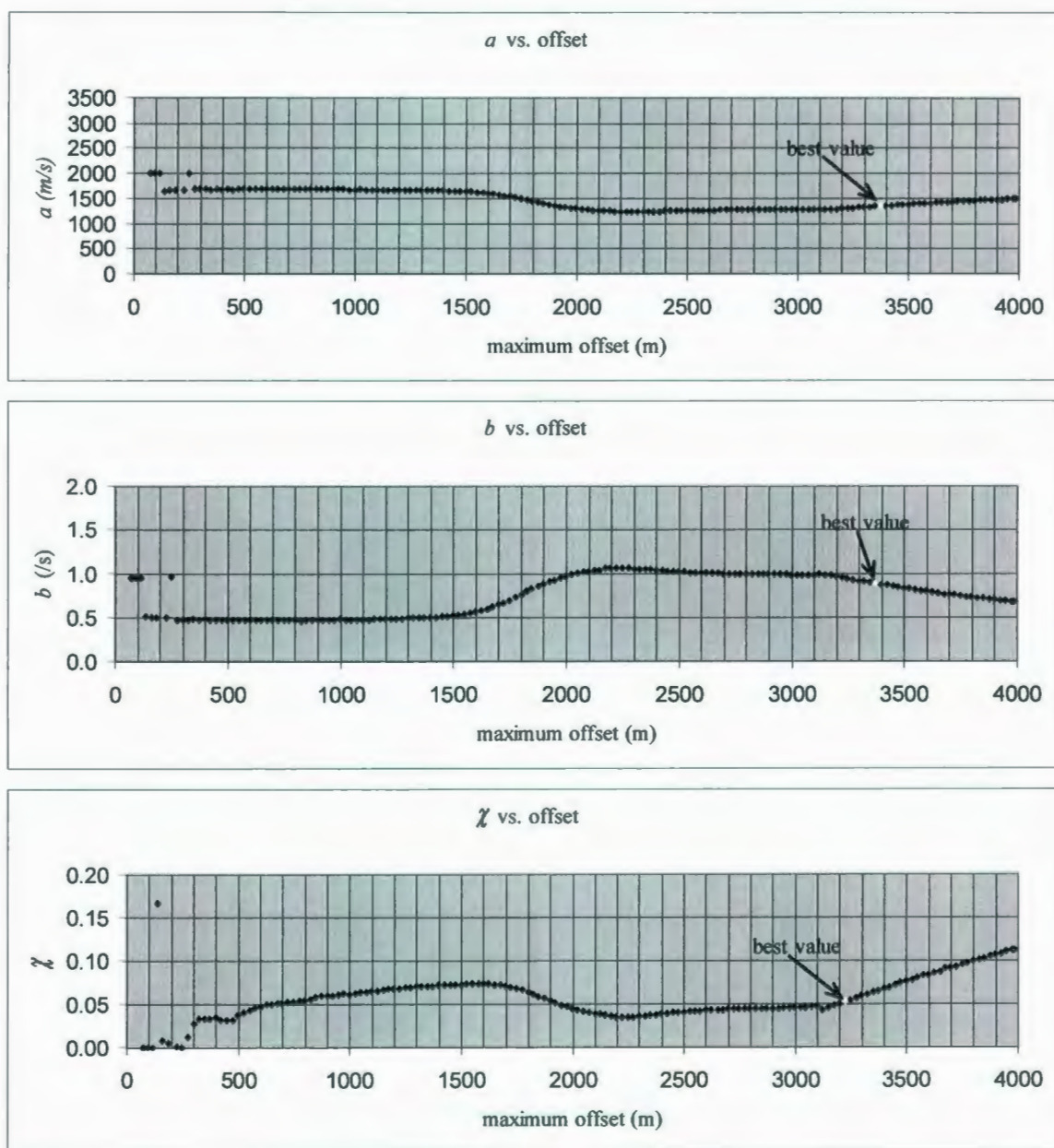


**Figure 5.6:** Display of results (from Table E.5) of  $a$ ,  $b$ , and  $\chi = 0$ , with maximum offsets increasing from 74.7 m to 1014.4 m, for all receivers, for the longside, shortoffsets only (B'). This is the same as Figure 5.8 up to the offset of 998.0 m, and is included here for comparison with results for the shortside only (B), Figure 5.10. Best values (minimum standard error) are as indicated.

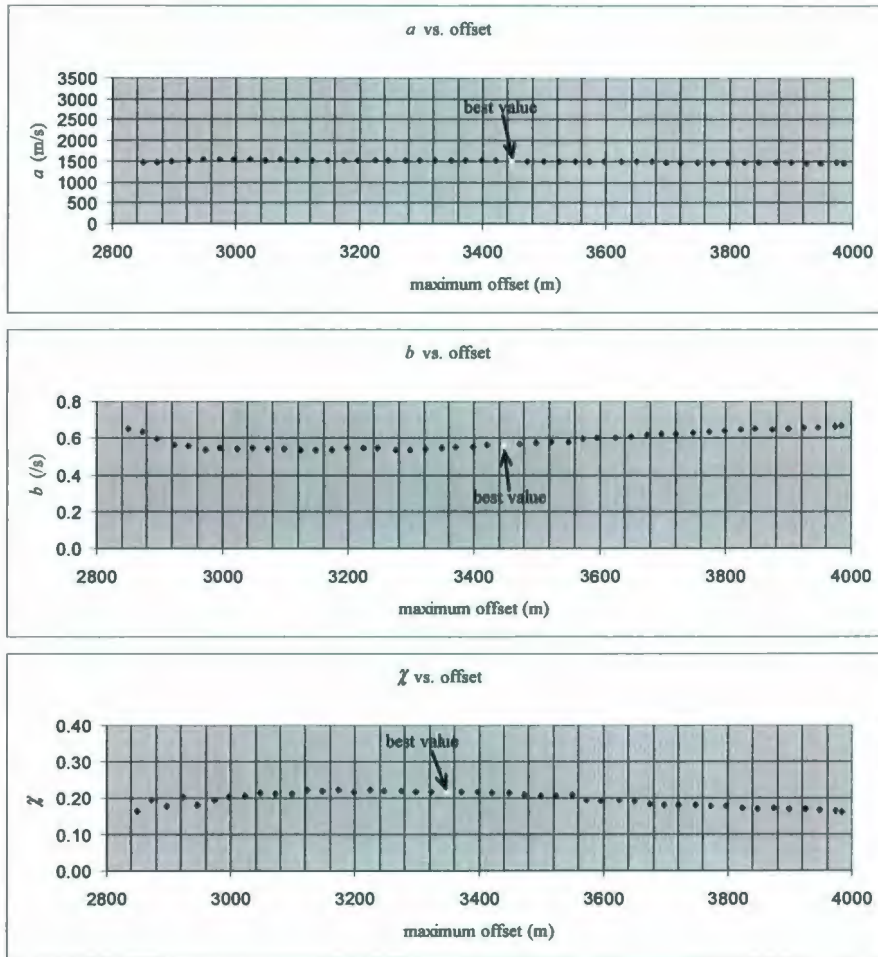


**Figure 5.7:** Display of results (from Table E.6) of  $a$ ,  $b$ , and  $\chi$ , with maximum offsets increasing from 47.9 m to 3984.4 m, includes longside and shortside, (A+B+C). Best values (minimum standard error) are as indicated.

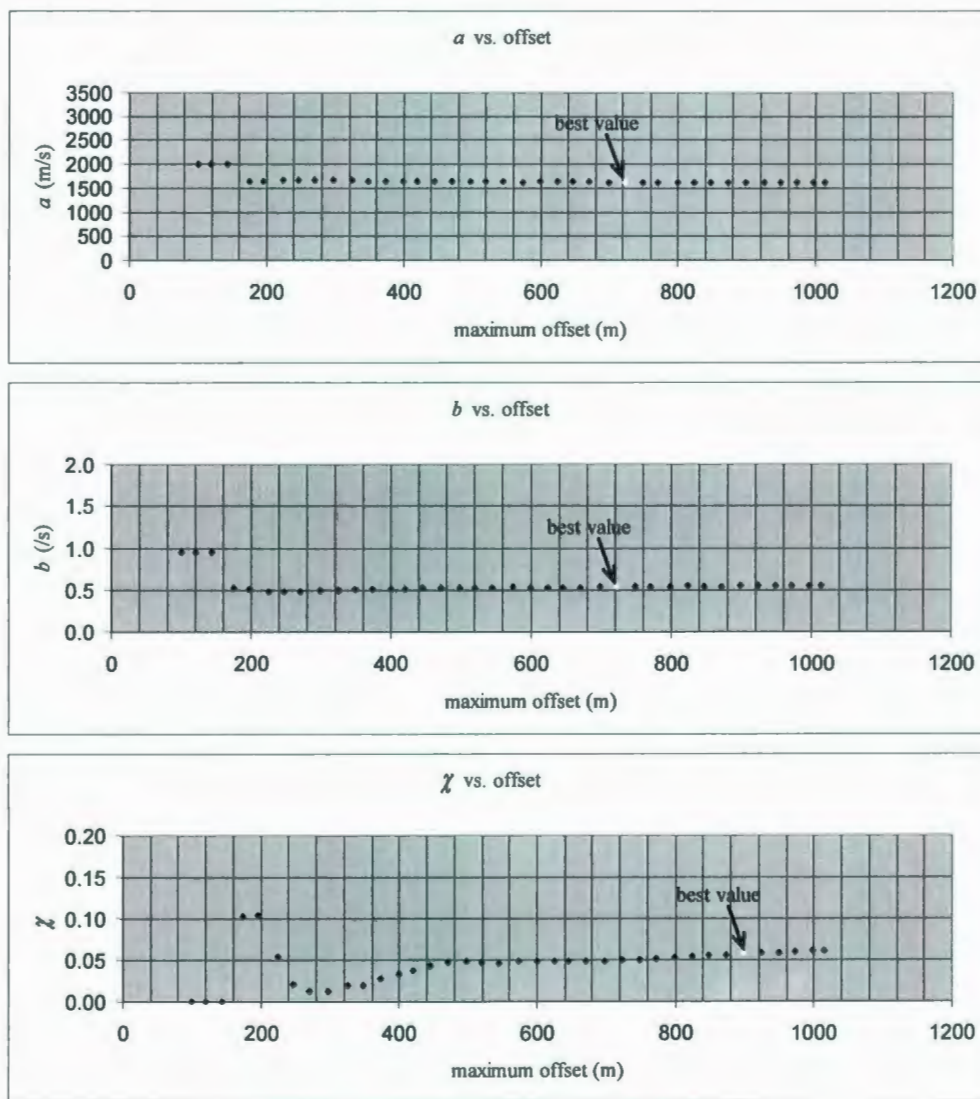




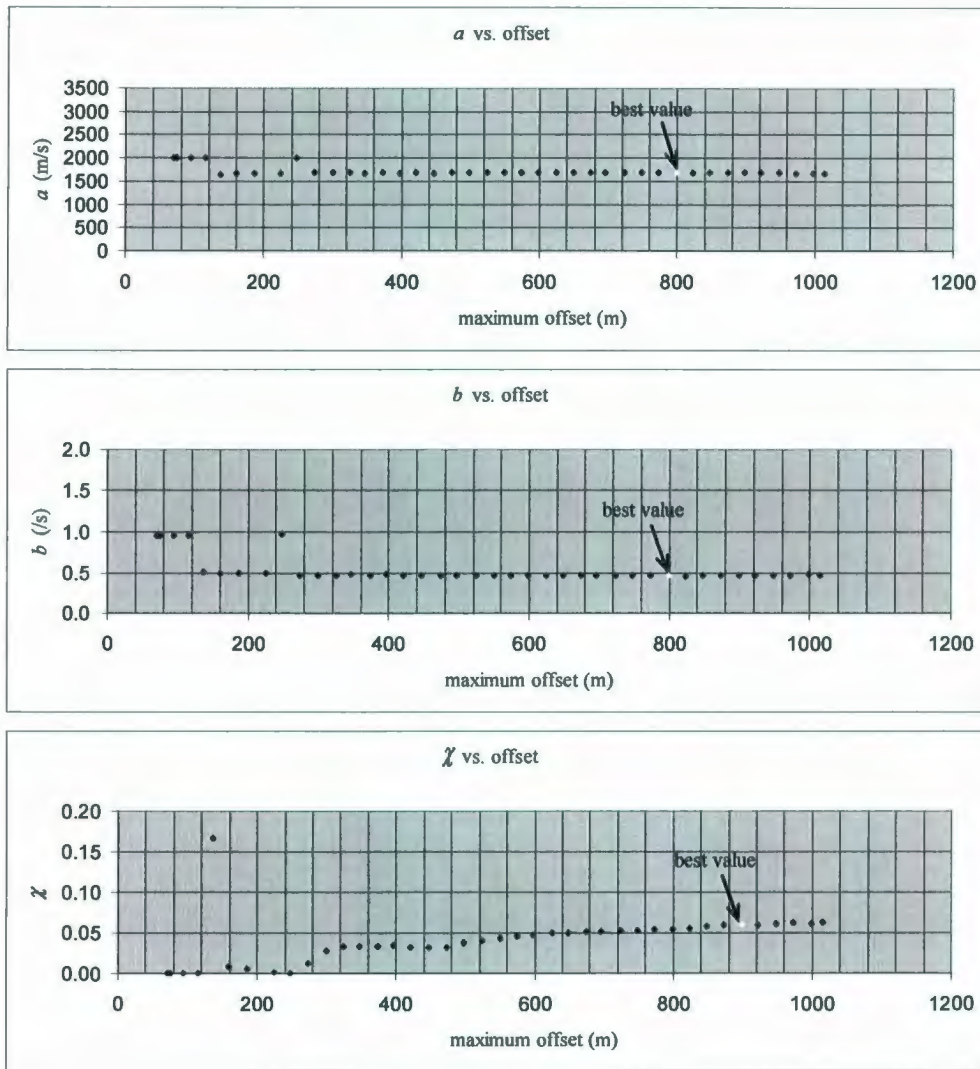
**Figure 5.8:** Display of results (from Table E.7) of  $a$ ,  $b$ , and  $\chi$ , with maximum offsets increasing from 69.7 m to 3984.4 m, for all receivers, for the longside only, (A+C). Best values (minimum standard error) are as indicated.



**Figure 5.9:** Display of results (from Table E.8) of  $a$ ,  $b$ , and  $\chi$ , with maximum offsets increasing from 2849.9 m to 3984.4 m, for all receivers, for the longside, longoffsets only, (D+C). Best values (minimum standard error) are as indicated.



**Figure 5.10:** Display of results (from Table E.9) of  $a$ ,  $b$ , and  $\chi$ , with maximum offsets increasing from 99.6 m to 1014.1 m, for all receivers, for the shortside only, (B). Best values (minimum standard error) are as indicated.



**Figure 5.11:** Display of results (from Table E.10) of  $a$ ,  $b$ , and  $\chi$ , with maximum offsets increasing from 69.7 m to 1014.4 m, for all receivers, for the longside, shortoffsets only, (B'). This is the same as Figure 5.8 up to the offset of 1014.4 m, and is included here for comparison with results for the shortside only (B), Figure 5.10. Best values (minimum standard error) are as indicated.



## **CHAPTER 6: DISCUSSION**

### **6.1 Walkaround VSP - Evaluation of Azimuthal Anisotropy and Other Factors**

The walkaround VSP served several purposes. It showed that there is little azimuthal variation in traveltimes after geometry corrections are applied, as can be seen from Figure 3.2b. We concluded that transverse isotropy can be considered as a model.

We infer that any dip or tilt effect is minimal. The medium can thus be considered to be vertically transversely isotropic (VTI). Having accepted such a model of the medium, one can proceed with quantification of the VTI anisotropy parameters by acquisition of a walkaway VSP.

The data quality in the region is good in nearly any direction and for an offset of up to 1.5 km, as can be seen from Figures 2.6 and 3.1. Few offset-VSP data sets existed in the region, and they were of poor quality. Thus, it was important to establish the quality of data expected before embarking on the acquisition of far-offset data.

Another purpose of the walkaround VSP was to address and resolve any operational issues. Walkaway VSPs are considerably more costly and require more resources than other types of data acquired in a well. Doing the walkaround VSP set the

stage for the successful acquisition, both technically and operationally, of the walkaway VSP.

## **6.2 Synthetic Data - Forward Modelling**

Synthetic data were used to establish that the program was working as expected and to get familiarized with its limitations. Chart 5.1 summarizes the inputs to the forward modelling and the inverse results obtained.

### **6.2.1 Fit and Residuals**

As a means of evaluating the results, traveltimes computed can be compared to the traveltimes observed. A quantitative fit is obtained by examining the residuals, i.e., the difference between the computed traveltimes and the actual traveltimes. Examining the residuals allows for a better determination of the accuracy of the data. For ideal values of  $a$ ,  $b$  and  $\chi$ , the residuals should all be zero.

### 6.2.2 Initial Guesses

Working with the synthetic data, it was realized that the program was sensitive to the initial guess; in particular for  $\chi$ . Sensitivities to initial guesses for  $a$ ,  $b$  and  $\chi$  were examined. Since  $\chi$  was the most sensitive of the three parameters, only results for  $\chi$  are shown and discussed in Section 5.2.3 and 5.2.4. Default program parameters were not suitable for all situations, for example; if  $\chi$  was very small or very large. In such situations, the program had computational problems.

### 6.2.3 Zero Offset

The zero-offset, which is a vertical-incidence case is an isotropic situation, and requires only two parameters, since there is no horizontal velocity component. The forward model assumed a linearly increasing velocity with depth in the medium, where  $v = a + bz$ . Using this synthetic data for the determination of  $a$  and  $b$  gave the correct values, confirming the algorithm could be applied to zero-offset data as discussed in Sections 5.2.1 and 5.2.2. Using real data (see Section 5.3.1), values obtained,  $a = 1592.27$  m/s and  $b = 0.576$  /s, appear reasonable. Using these values, traveltimes were computed and compared to actual traveltimes as shown in Table 6.1 and Figure 6.1. In the zero-offset case, since we only have the vertical component of the velocity, determining  $\chi$  is impossible.

The modelled traveltimes, using the inverse parameters for  $a$  and  $b$ , are satisfactory. However, the residuals in Figure 6.1 show that at shallow depths the discrepancy is significant. This is possibly due to the zero-offset assumption not being valid for shallow depths, i.e., the source is significantly offset relative to depth, and so the actual path deviates significantly from vertical and may be subject to a lateral variation in velocity. Also, the first depth point used is at the sea bed (130.8 m depth) and the arrival time is computed from setting the velocity of water (1524 m/s). This point is atypical of the rest of the medium where velocities are higher and thus may introduce a small error at shallow depths. At depths below 1800 m there seems to be a trend of the residuals becoming more positive. Interval velocities computed from the depths and traveltimes, Table 6.2 and Figure 6.2, show the velocity to be increasing slightly more rapidly than our assumption that velocity increases linearly with depth, and on which the travel-time formula is based, thus giving rise to the pattern of residuals observed.

There is a fair amount of scatter in the interval velocities, with the interval velocity increasing or decreasing rapidly. This is a result of the depth sampling being too fine relative to the observed traveltime. By taking coarser sampling (larger depth intervals) the velocities would have less scatter. This scatter may influence the regression analyses. Overall, however, the results of the inverse modelling are good with most of the residuals at  $\pm 3$  ms.

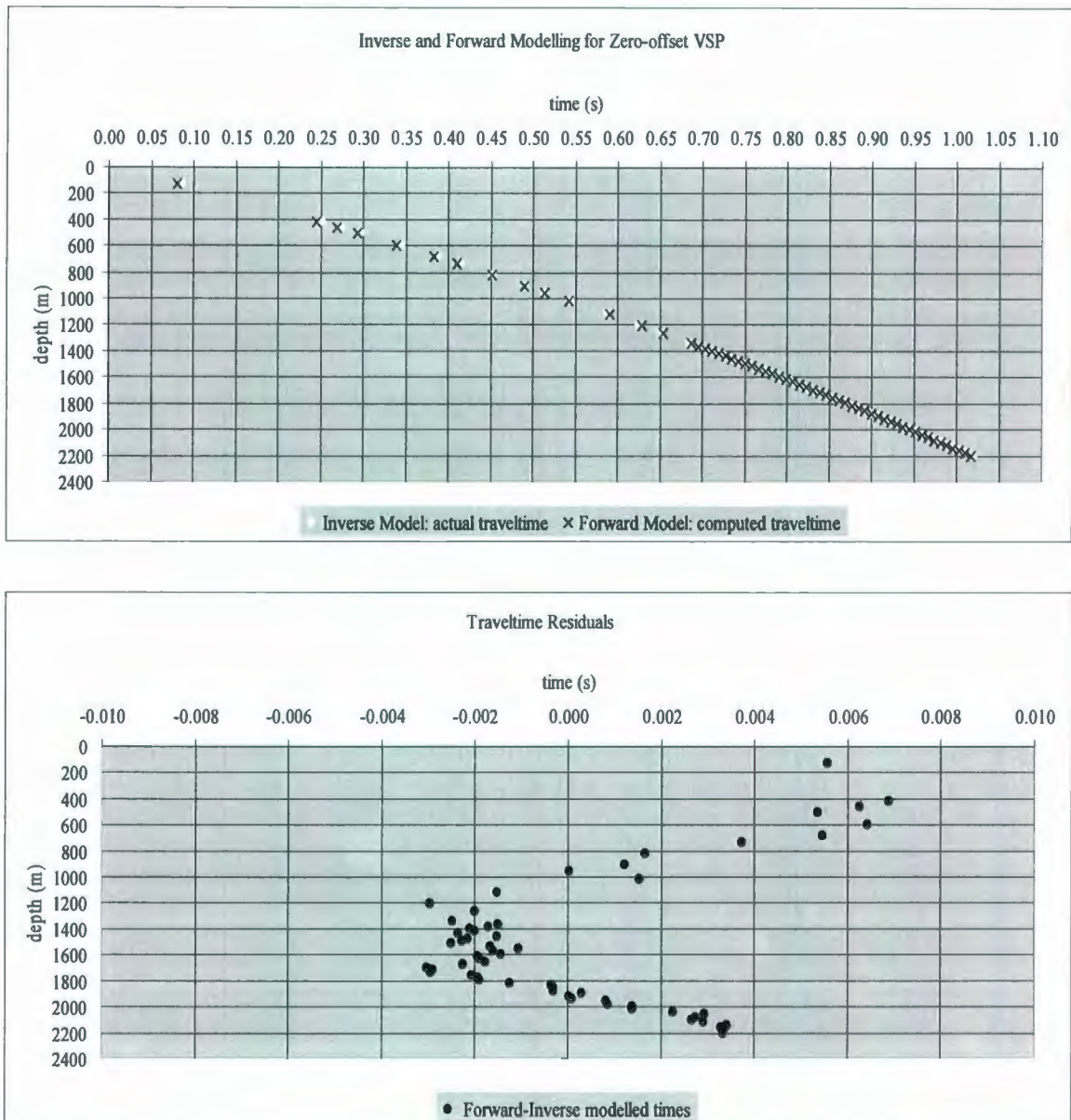


**Table 6.1:** Actual traveltimes and forward modelled traveltimes for the zero-offset VSP. Traveltimes are displayed in Figure 6.1 for comparison. Depths are referenced from mean sea level. The sea floor is at a depth of 130.8 m.

Vertical Depth z (m)	Vertical Travel Time (s)	Travel Times from Forward Modelling (s)	Residual (s)	Vertical Depth z (m)	Vertical Travel Time (s)	Travel Times from Forward Modelling (s)	Residual (s)
130.80	0.08583	0.08026	0.00556	1635.40	0.80507	0.80698	-0.00191
418.60	0.25169	0.24481	0.00688	1655.50	0.81313	0.81490	-0.00177
463.10	0.27517	0.26892	0.00625	1675.60	0.82052	0.82278	-0.00226
507.40	0.29794	0.29259	0.00535	1695.90	0.82767	0.83070	-0.00303
595.10	0.34494	0.33852	0.00642	1716.10	0.83564	0.83855	-0.00291
681.50	0.38807	0.38261	0.00546	1736.20	0.84338	0.84632	-0.00295
738.10	0.41464	0.41090	0.00373	1756.40	0.85203	0.85410	-0.00207
820.90	0.45313	0.45148	0.00165	1776.40	0.85982	0.86177	-0.00194
901.30	0.49119	0.48999	0.00121	1796.60	0.86757	0.86947	-0.00190
953.00	0.51432	0.51431	0.00002	1816.90	0.87594	0.87719	-0.00125
1014.70	0.54442	0.54289	0.00153	1837.10	0.88448	0.88483	-0.00035
1119.90	0.58904	0.59057	-0.00153	1857.30	0.89212	0.89243	-0.00031
1205.00	0.62524	0.62821	-0.00297	1877.60	0.89973	0.90005	-0.00032
1264.00	0.65182	0.65383	-0.00201	1897.80	0.90789	0.90759	0.00030
1343.40	0.68524	0.68772	-0.00248	1917.80	0.91504	0.91502	0.00001
1362.80	0.69441	0.69591	-0.00150	1938.00	0.92258	0.92250	0.00009
1381.90	0.70222	0.70393	-0.00171	1958.10	0.93072	0.92991	0.00081
1400.90	0.70976	0.71187	-0.00211	1977.90	0.93803	0.93717	0.00086
1419.60	0.71764	0.71964	-0.00201	1997.70	0.94579	0.94441	0.00138
1438.10	0.72494	0.72731	-0.00237	2017.90	0.95314	0.95176	0.00138
1456.60	0.73341	0.73493	-0.00152	2038.50	0.96149	0.95923	0.00226
1475.20	0.74042	0.74257	-0.00215	2059.20	0.96963	0.96669	0.00293
1494.20	0.74806	0.75034	-0.00227	2079.80	0.97683	0.97410	0.00273
1513.90	0.75584	0.75835	-0.00251	2100.30	0.98409	0.98143	0.00266
1534.10	0.76486	0.76653	-0.00168	2120.80	0.99164	0.98873	0.00290
1554.60	0.77372	0.77479	-0.00107	2141.20	0.99939	0.99597	0.00342
1574.90	0.78132	0.78294	-0.00161	2161.50	1.00642	1.00314	0.00328
1595.10	0.78957	0.79100	-0.00143	2181.80	1.01363	1.01029	0.00334
1615.20	0.79704	0.79899	-0.00195	2202.00	1.02068	1.01736	0.00332
$a = 1592.25865118521 \text{ m/s}$							
$b = 0.575514064006845 \text{ /s}$							

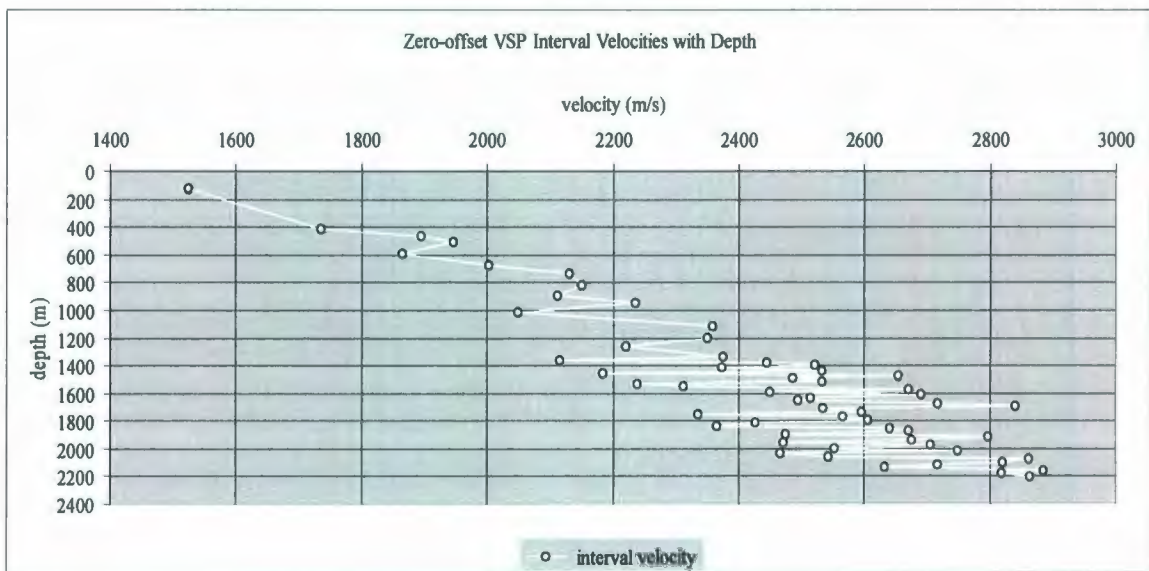
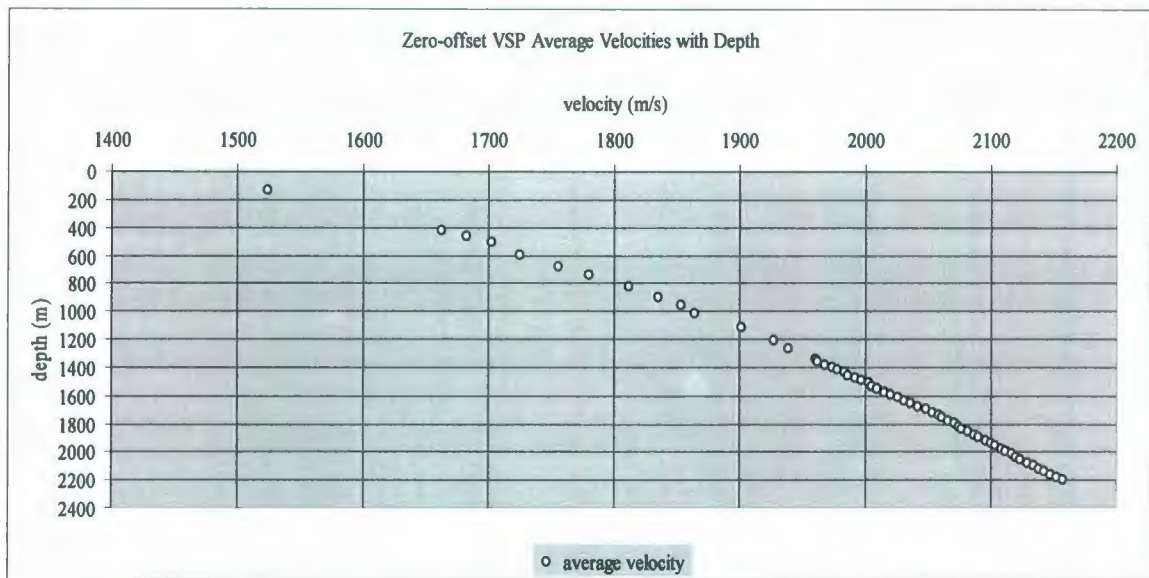
**Table 6.2:** Average and interval velocities for the zero-offset VSP. Velocities are displayed in Figure 6.2 for comparison. Depths are referenced from mean sea level. The sea floor is at a depth of 130.8 m, the velocity of water is 1524 m/s.

Vertical depth (m)	Average velocity (m/s)	Interval velocity (m/s)	Vertical depth (m)	Average velocity (m/s)	Interval velocity (m/s)
130.80	1524.00	1524.00	1635.40	2031.38	2514.68
418.60	1663.17	1735.19	1655.50	2035.97	2495.18
463.10	1682.95	1894.92	1675.60	2042.12	2717.52
507.40	1703.05	1945.93	1695.90	2049.01	2841.10
595.10	1725.21	1865.70	1716.10	2053.64	2534.51
681.50	1756.12	2003.29	1736.20	2058.63	2596.86
738.10	1780.12	2130.76	1756.40	2061.43	2335.00
820.90	1811.63	2151.04	1776.40	2066.01	2565.79
901.30	1834.92	2112.25	1796.60	2070.83	2606.41
953.00	1852.92	2235.11	1816.90	2074.24	2427.09
1014.70	1863.82	2050.03	1837.10	2077.05	2365.11
1119.90	1901.24	2357.85	1857.30	2081.89	2641.73
1205.00	1927.26	2350.67	1877.60	2086.86	2670.66
1264.00	1939.20	2219.96	1897.80	2090.35	2475.48
1343.40	1960.47	2375.35	1917.80	2095.87	2796.57
1362.80	1962.53	2116.23	1938.00	2100.62	2676.58
1381.90	1967.90	2445.60	1958.10	2103.86	2471.49
1400.90	1973.78	2521.19	1977.90	2108.56	2706.50
1419.60	1978.16	2373.00	1997.70	2112.20	2552.25
1438.10	1983.75	2533.24	2017.90	2117.11	2749.51
1456.60	1986.06	2183.78	2038.50	2120.15	2466.83
1475.20	1992.39	2654.73	2059.20	2123.70	2542.64
1494.20	1997.43	2485.96	2079.80	2129.14	2861.52
1513.90	2002.95	2533.33	2100.30	2134.25	2821.07
1534.10	2005.74	2239.72	2120.80	2138.69	2718.02
1554.60	2009.25	2312.11	2141.20	2142.51	2632.48
1574.90	2015.68	2670.84	2161.50	2147.70	2884.64
1595.10	2020.22	2449.99	2181.80	2152.47	2818.83
1615.20	2026.51	2691.06	2202.00	2157.38	2863.17



**Figure 6.1:** Actual traveltimes vs. forward modelled traveltimes for the zero-offset VSP (above) and residuals (below). At very shallow depths the discrepancy seen from the residuals is possibly due to oblique rays. Results of the inverse modelling are good; most of the residuals are within  $\pm 3$  ms.



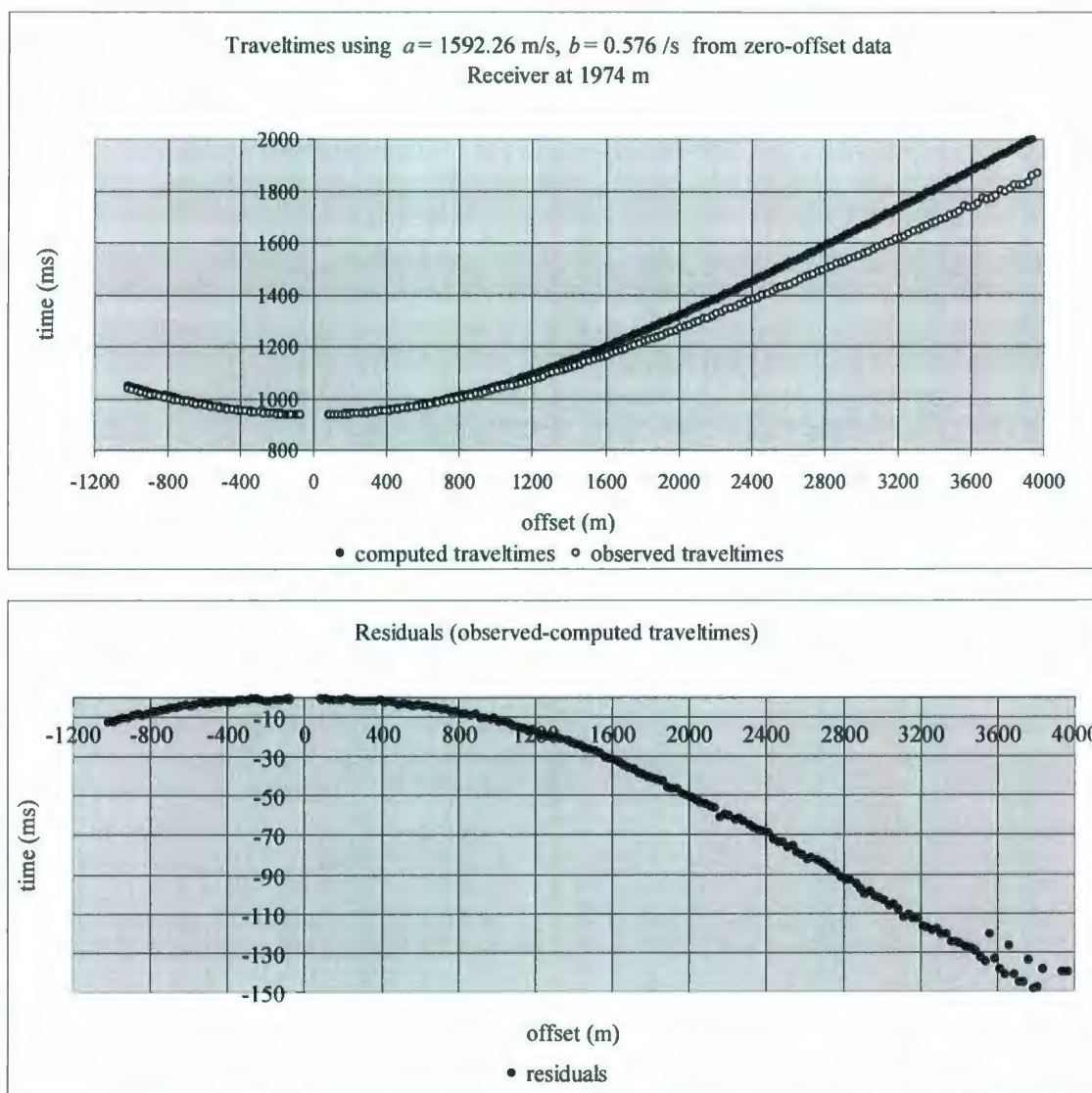


**Figure 6.2:** Average (top) and interval (below) velocities for the zero-offset VSP. The scatter in the interval velocities may be because of the depth sampling being too fine relative to the observed traveltime. By taking coarser or larger depth intervals, the velocities would appear to have less scatter.

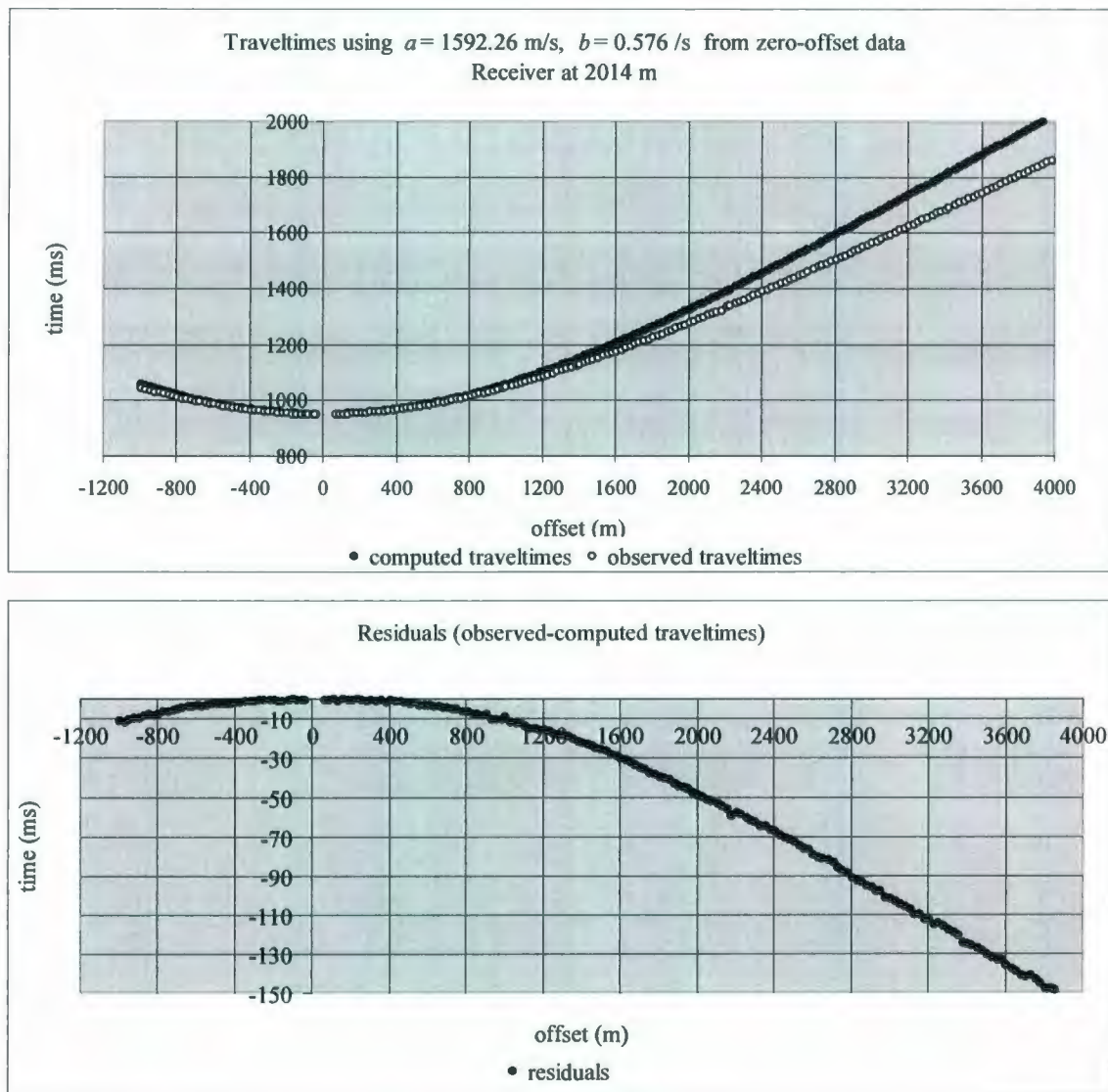


#### 6.2.4 Offset

Using the values obtained for  $a$  and  $b$  from the zero-offset VSP, discussed above and shown in Table 5.5, traveltimes were modelled for the same offsets and depths as the offset-VSP data. Traveltimes versus offset for the isotropic case were thus obtained. Tables F.1a and F1b and Figures 6.3a and 6.3b depict the results of the forward modelling and the observed times for receivers at depths 1974 m and 2014 m. The difference in the actual observed traveltimes and the modelled traveltimes, or residuals, can be considered due to anisotropy or lateral inhomogeneity. For the receiver at depth 1974 m, scatter can be seen at offsets greater than 3400 m. This is likely due to rays that are near horizontal or from refracted arrivals.



**Figure 6.3a:** Isotropy vs. anisotropy, forward modelling with isotropic parameters for receiver at 1974 m depth. The difference between the observed traveltimes and modelled traveltimes, the residual, shows the possible effect of anisotropy.



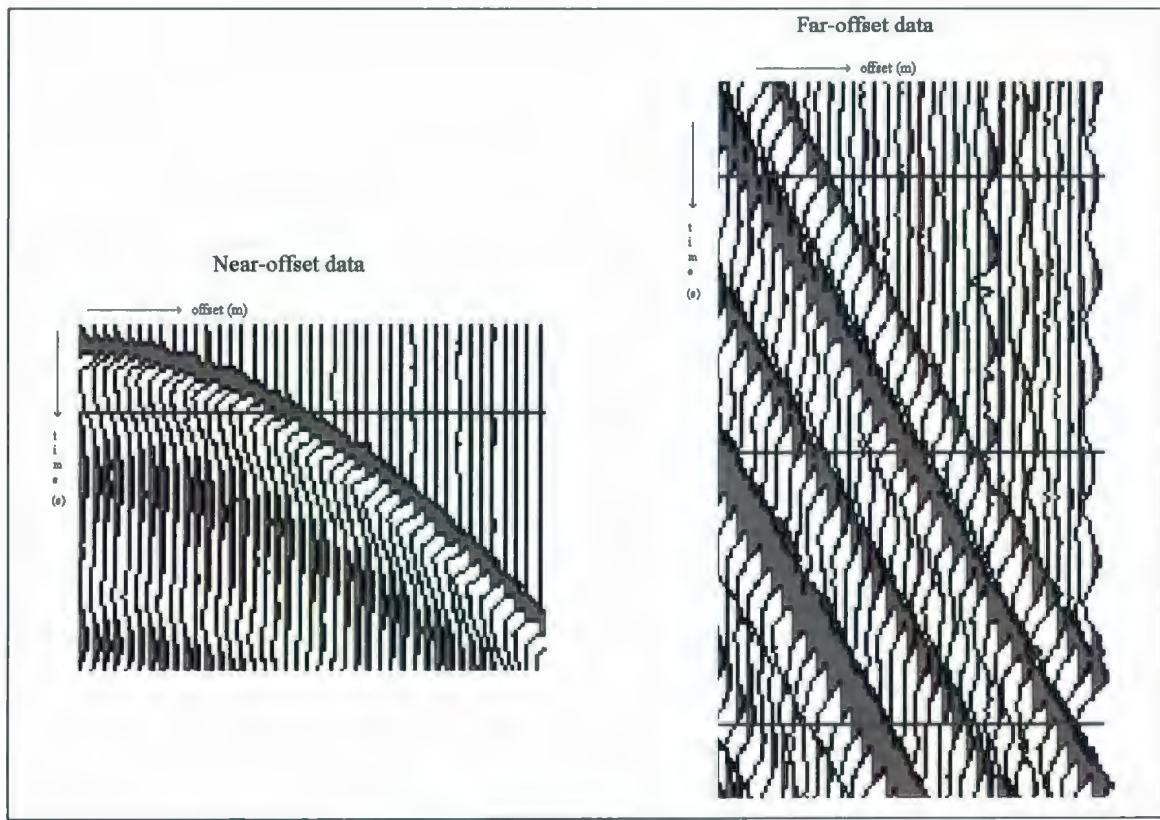
**Figure 6.3b:** Isotropy vs. anisotropy, forward modelling with isotropic parameters for receiver at 2014 m depth. The difference between the observed traveltimes and modelled traveltimes, the residual, shows the possible effect of anisotropy.

#### 6.2.4.1 Traveltime Picks

The traveltime picks are a source of error. Traveltimes were obtained from the VSP data, by picking the 'first-break'. This is where the first deflection is observed on a trace and is considered to be the direct arrival time of the P wave.

Figure 3.3 shows the walkaway VSP data used. As can be seen, the data are generally of good quality - 'clean'. With increasing offset, two effects are observed. The signal-to-noise ratio decreases, and the seismic wavelet exhibits stretching due to frequency dispersion, i.e., higher frequencies are attenuated or absorbed faster than lower frequencies, causing the wavelet to broaden. Hooke's law of elasticity, for a linearly elastic continuum, assumes no attenuation or dispersion. In an idealized material described by Hooke's Law, the signal would propagate unaffected through the medium. However, in practice we always deal with limitations as observed here. Thus, the picking of first arrivals becomes less reliable with increasing offset. Figure 6.4 shows some far-offset traces compared to near-offset traces to illustrate the picking difficulty at the far offset. This may be the cause of some of the scatter observed in the residuals at the far offsets.





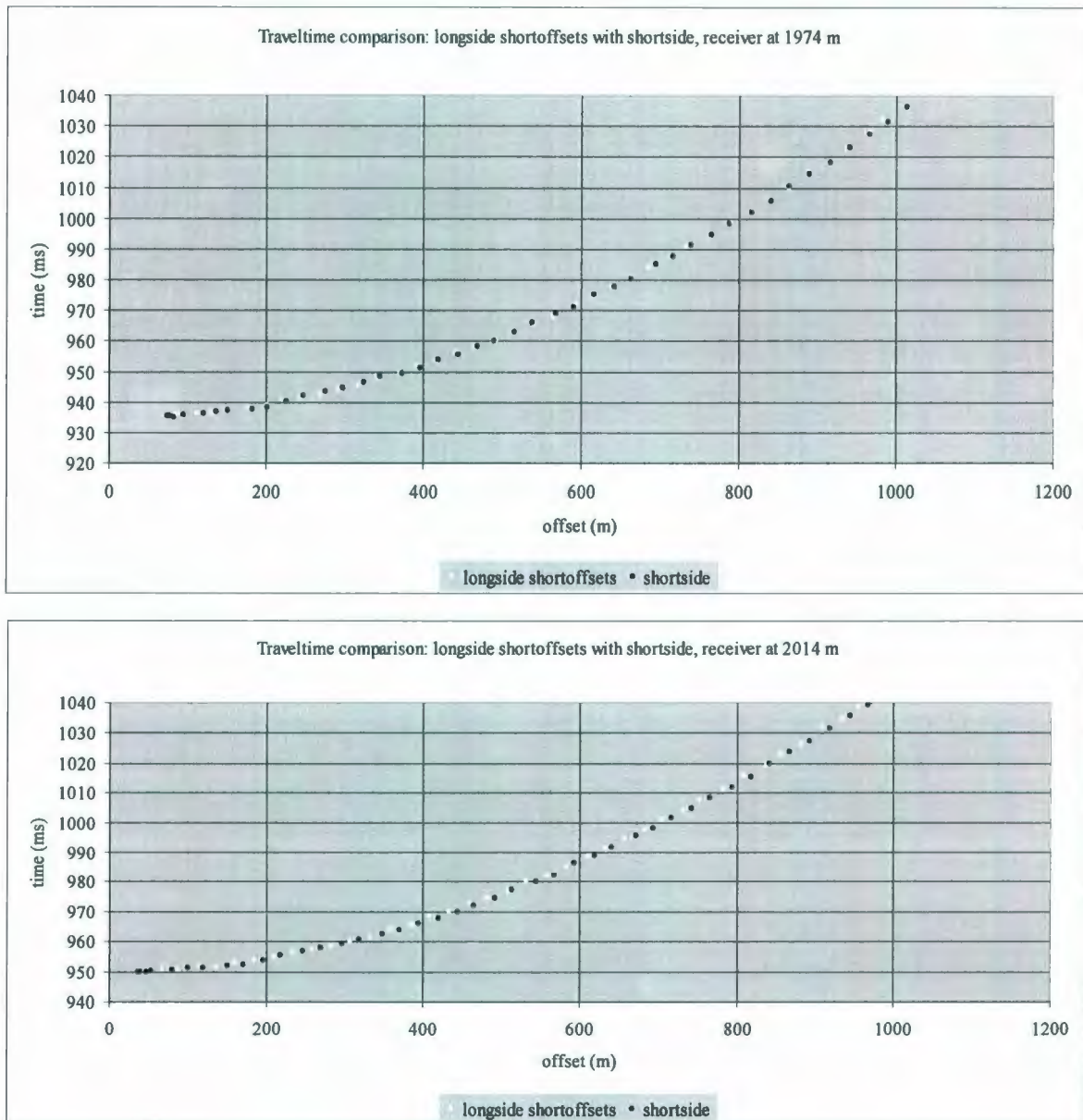
**Figure 6.4:** Near- and far-offset VSP data. With increasing offset, the background noise level increases and the seismic wavelet broadens due to frequency dispersion. Thus, picking of first arrivals is less reliable with offset.

## 6.3 Real data – Inverse Modelling

### 6.3.1 Dip Considerations

From observations on seismic data and an understanding of the regional geology of the area, a mild dip of approximately  $2^\circ$  was estimated in the acquisition direction of the walkaway line. The effect of the dip can be assessed by examining the traveltimes in

opposite directions. Figure 6.5 shows the traveltimes observed for longside shortoffsets (B') vs. shortside (B) for receivers at depth 1974 m and 2014 m, respectively. Only a slight difference in traveltimes can be seen.

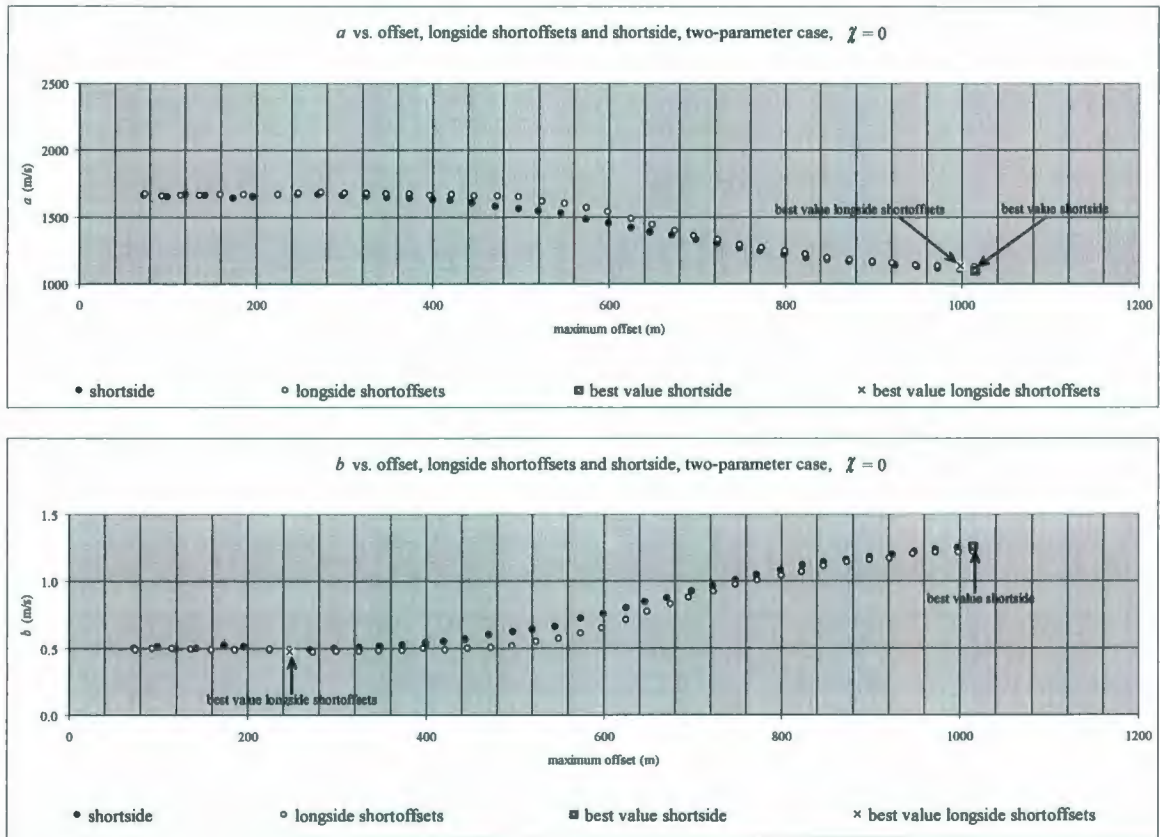


**Figure 6.5:** Dip considerations. Traveltimes for longside shortoffsets (B') vs. shortside (B). Only a slight difference in traveltimes is observed due to the regional dip of  $2^\circ$  estimated in the area.

Figure 6.6 combines Figures 5.5 and 5.6, the results as obtained for  $a$  and  $b$  only, with  $\chi = 0$ , for the shortside (B) and the longside shortoffsets (B'). Values obtained show a small difference between the two sides.

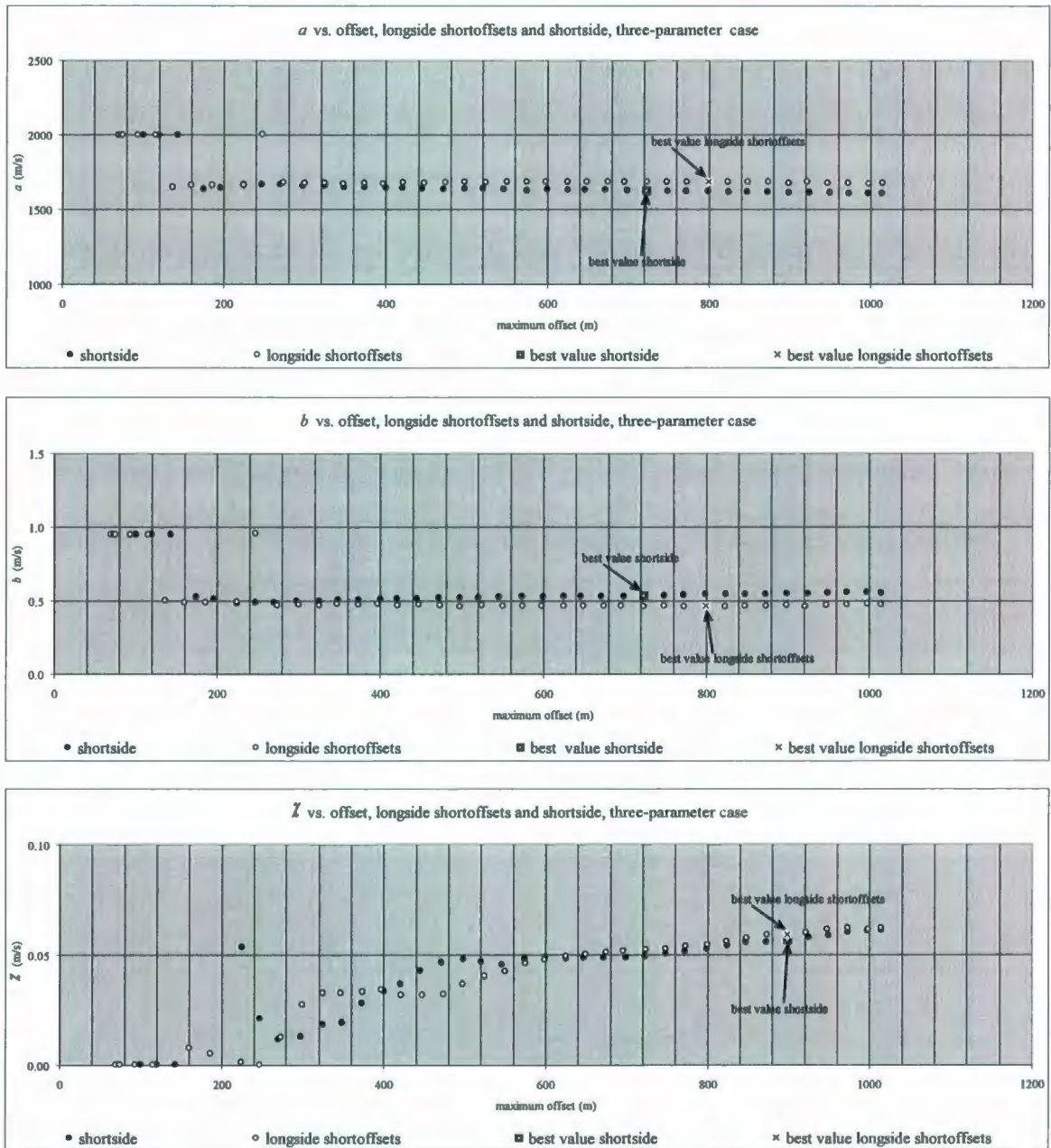
Figure 6.7 combines, for comparison, the results obtained for  $a$ ,  $b$  and  $\chi$  shown in Figures 5.10 and 5.11, i.e., shortside (B) with longside shortoffsets (B'). As above, values obtained show a small difference between the two sides. The scatter observed in the values of  $\chi$  are at near offsets, where the offsets may not be sufficiently long to be able to adequately discriminate between horizontal and vertical velocities.

The traveltime difference is small, but sufficient to affect the values obtained for  $a$ ,  $b$  and  $\chi$  for the three-parameter case and also  $a$ , and  $b$  for the two-parameter case. It would seem, therefore, appropriate, to only consider data from the longside (A+C) for the estimations of  $a$ ,  $b$  and  $\chi$ .



**Figure 6.6:** Comparison of  $a$  and  $b$ ,  $\chi = 0$ , obtained for longside shorfoffsets (B') with shortside (B). Values obtained show a small difference between the two sides.



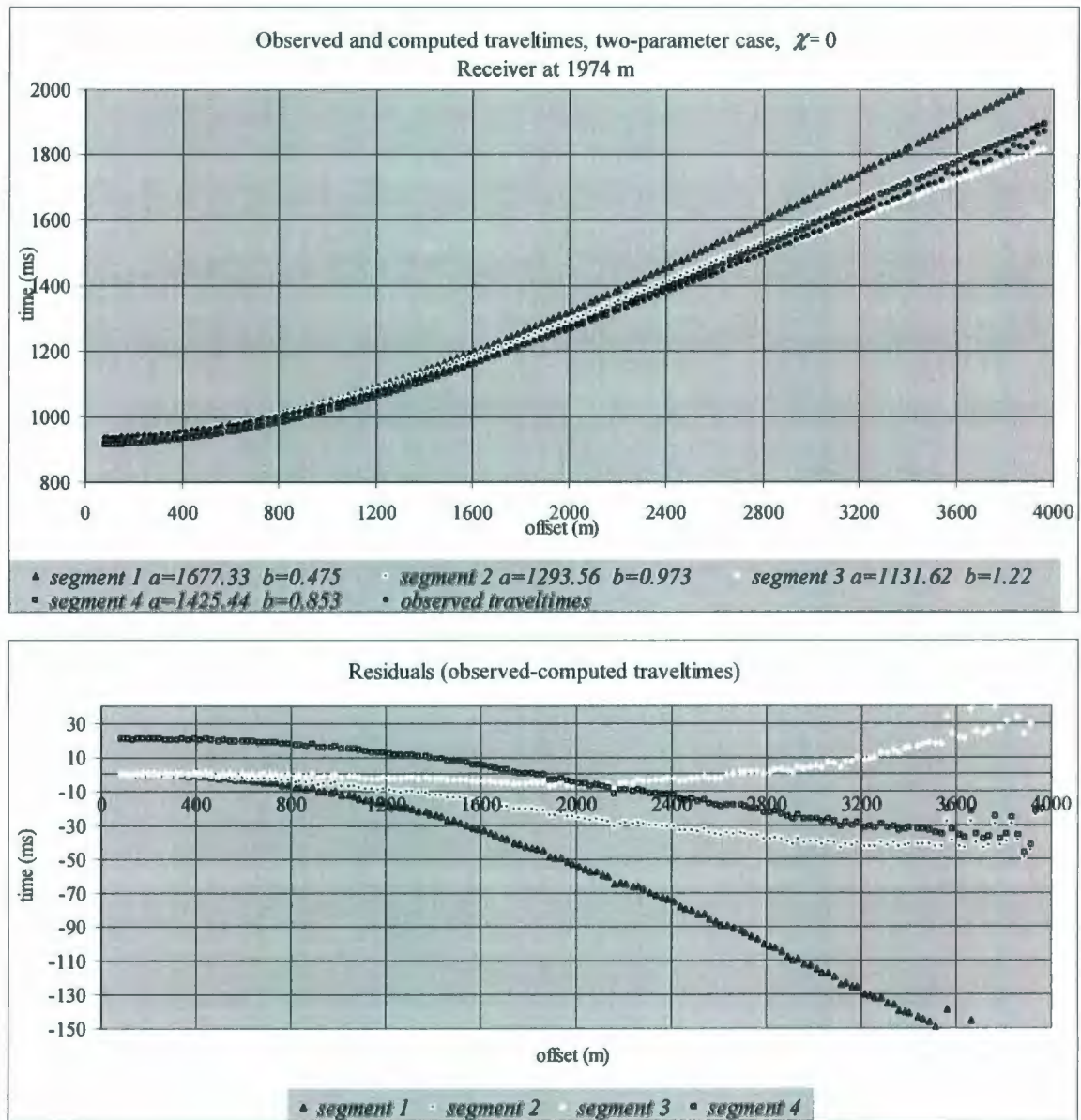


**Figure 6.7:** Comparison of  $a$ ,  $b$  and  $\chi$  obtained for longside shortoffsets (B') with shortside (B). Values obtained show a small difference between the two sides. Scatter observed in the values of  $\chi$  are at offsets which may not be sufficiently long for discrimination between horizontal and vertical velocities.

### 6.3.2 Two-parameter Case (Inhomogeneous Isotropic), $\chi = 0$ , Longside

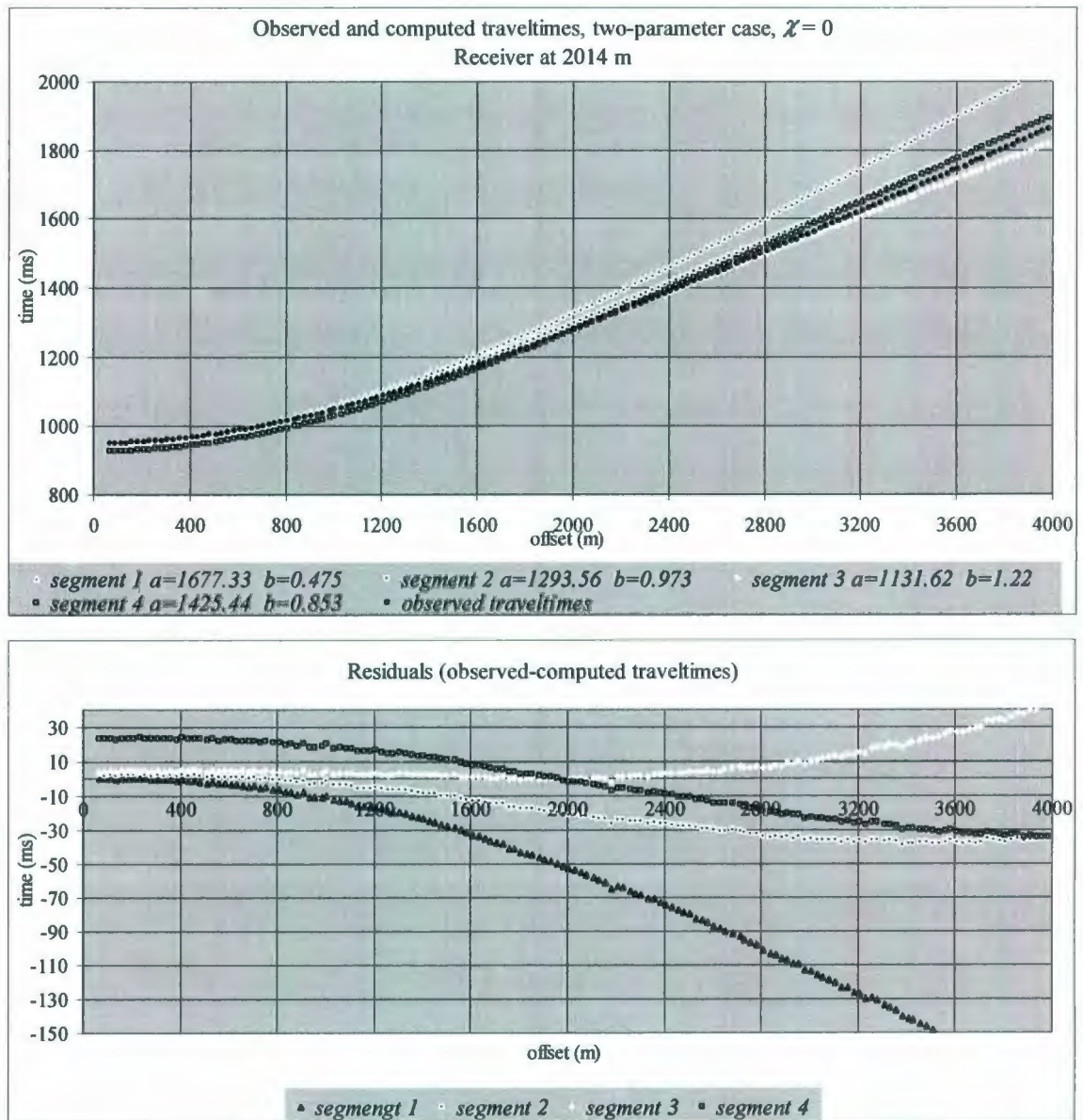
For the offset data, setting  $\chi = 0$ , implies the medium is inhomogeneous, but isotropic. This means that we are looking for a solution that does not consider anisotropy and can be defined by the two parameters  $a$  and  $b$ . Figure 5.3 and Table E.2 show the results for  $a$  and  $b$  with  $\chi = 0$  for the longside (A+C). The results can be viewed as four segments: (a) offsets less than 500 m, where  $a$  and  $b$  are nearly constant with  $a \approx 1600$  m/s and  $b \approx 0.5$  /s, (b) from about 500 m to about 1000 m, where  $a$  decreases and  $b$  increases, (c) from about 1000 m to about 2600 m, where  $a$  and  $b$  stay relatively constant at  $a \approx 1100$  m/s and  $b \approx 1.3$  /s, and (d) from about 2600 m to about 4000 m, where  $a$  increases and  $b$  decreases.

In order to evaluate which segment provides the best estimated combination of  $a$  and  $b$ , we compare the traveltimes and residuals obtained from representative values for  $a$  and  $b$  from each segment, see Figure 6.8a and Figure 6.8b, and Tables F.2a to F.5b, for receivers at 1974 m and 2014 m, respectively. The curve for segment 3, in both cases, shows the smallest residuals. The residuals vary close to zero ( $|\text{residuals}| < 10$  ms) up to offsets of about 3000 m. From offset data then, the isotropic ‘best’ solution is  $a = 1131.62$  m/s and  $b = 1.22$  /s. The fit with these parameters to the observed data is good up to 3000 m, as expected, since this is the value obtained by inversion at an offset of 2773.23 m (see Table E.2).



**Figure 6.8a:** Comparison of traveltimes and residuals from four segments of the inverse results obtained for the 'longside' with receiver at 1974 m. The curve for segment 3 shows the least amount or best residuals. The residuals vary close to zero ( $|\text{residuals}| < 10$  ms) up to offsets of about 3000 m. From offset data, the isotropic 'best' solution is  $a = 1131.62$  m/s and  $b = 1.22$  /s.





**Figure 6.8b:** Comparison of traveltimes and residuals from four segments of the inverse results obtained for the 'longside' with receiver at 2014 m. As in Figure 6.8a, the curve for segment 3 shows the smallest residuals.



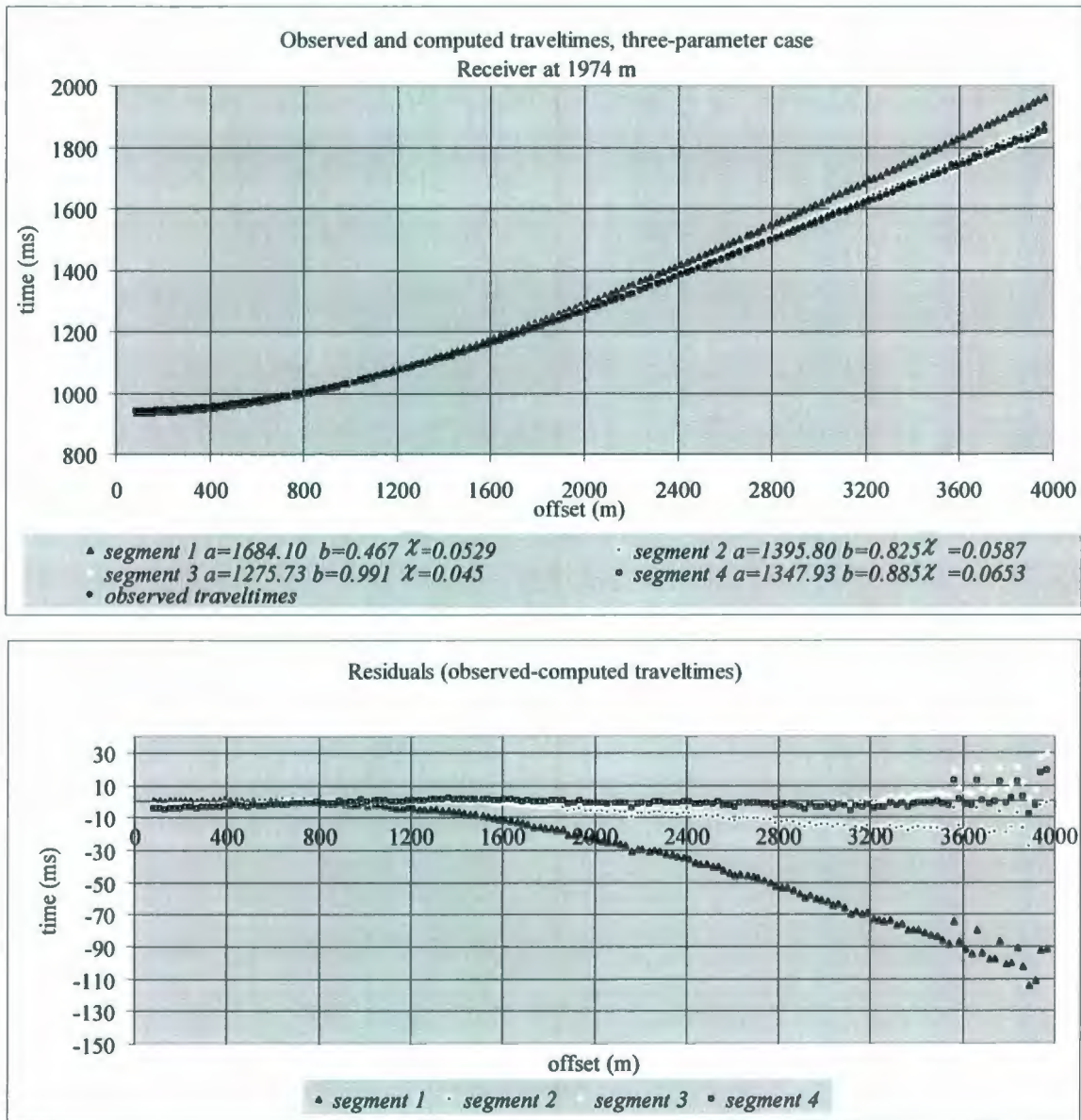
### 6.3.3 Three-parameter Case (Inhomogeneous Anisotropic), Longside

Figure 5.8 shows the results obtained for  $a$ ,  $b$  and  $\chi$  with  $\chi \neq 0$ , longside (A+C). Again, four segments can be seen: (a) up to about 1500 m, where  $a$  and  $b$  are nearly constant with  $a \approx 1600$  m/s and  $b \approx 0.5$  /s and  $\chi$  increasing to 0.07, (b) from about 1500 m to about 2100 m, where  $a$  and  $\chi$  are decreasing and  $b$  is increasing, (c) from about 2100 m to about 3200 m, where  $a \approx 1300$  m/s and  $b \approx 1.0$  /s and  $\chi \approx 0.45$  and there is little change in  $a$ ,  $b$  and  $\chi$ , and (d) from about 3200 m to about 4000 m, where  $a$  and  $\chi$  increase to  $\approx 1500$  m/s and 0.11 and  $b$  decreases to  $\approx 0.675$  /s .

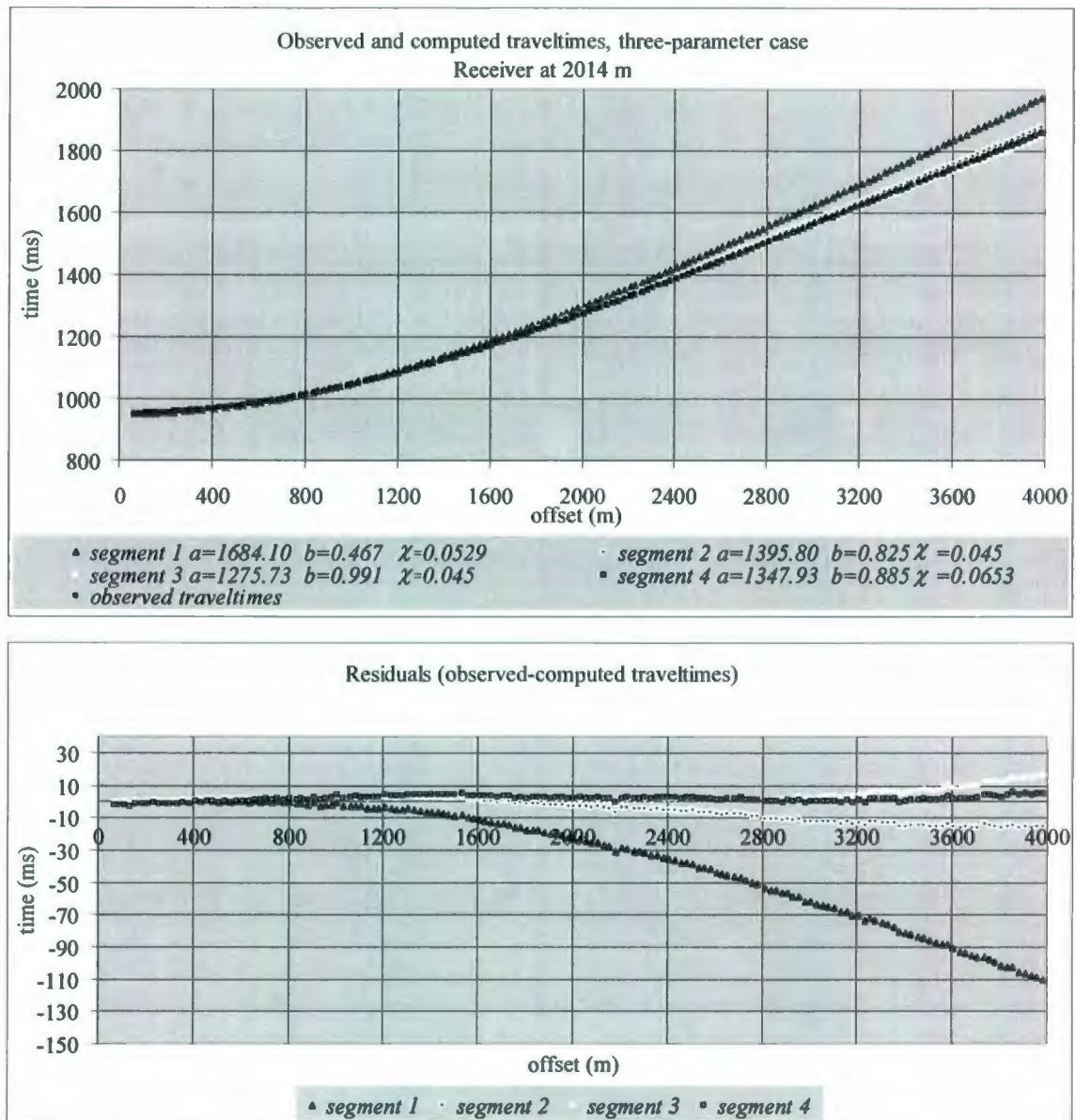
For each of these segments we compare the traveltimes and residuals obtained from representative values for  $a$ ,  $b$  and  $\chi$  from each segment, Figure 6.9a and 6.9b, Tables F.6a to F.9b, for receivers at 1974 m and 2014 m, respectively. This time, the values of  $a$ ,  $b$  and  $\chi$  from two of the segments, segments 3 and 4 (see Figures 6.9a and 6.9b), give traveltimes with a very good fit to the observed traveltimes, the segment 4 fit being slightly better. The residuals are better than the isotropic solution. They are even closer to zero ( $|\text{residuals}| < 5$  ms) than the isotropic residuals, and for offsets up to 3400 m, which is farther than for the isotropic solution.

Figure 6.10 compares the residuals obtained using  $a$  and  $b$  with those obtained using  $a$ ,  $b$  and  $\chi$ . The three-parameter case gives a better solution than the two-parameter

case. Although the two-parameter solution is comparable up to about 2600 m, the three-parameter solution encompasses farther offsets.

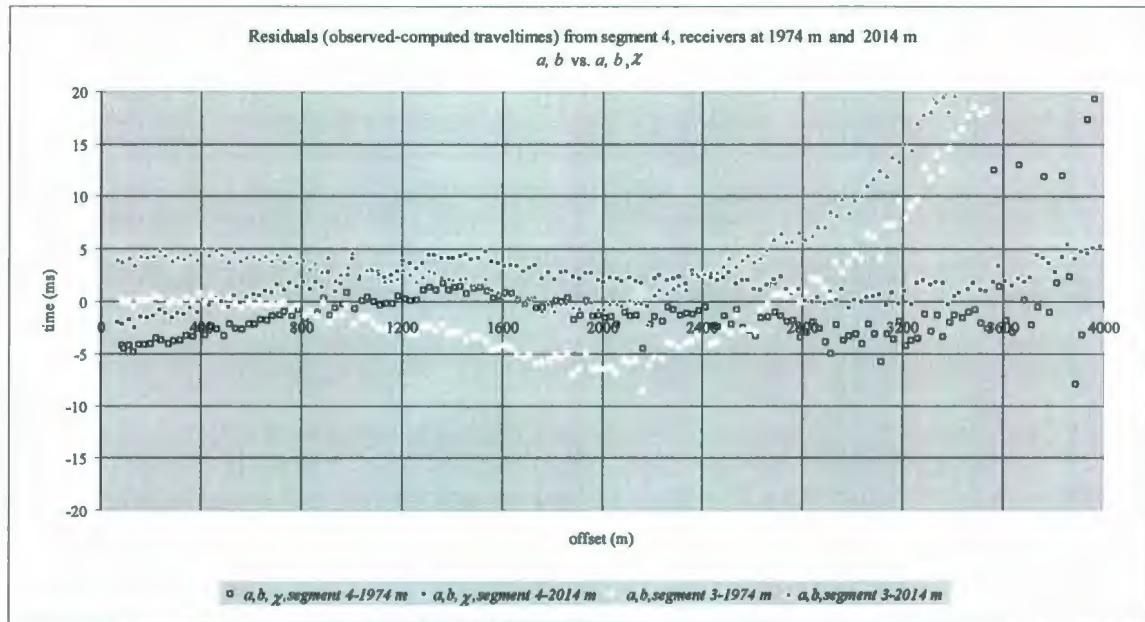


**Figure 6.9a:** Comparison of traveltimes and residuals from four segments of the inverse results obtained for the 'longside' with receiver at 1974 m. Values of  $a$ ,  $b$  and  $\chi$  from segments 3 and 4 give traveltimes with a very good fit to the observed traveltimes. The residuals are better than the isotropic solution (see Figures 6.8a and 6.8b). They are even closer to zero ( $|\text{residuals}| < 5$  ms) than the isotropic residuals, and for offsets up to 3400 m, which is farther than for the isotropic solution.



**Figure 6.9b:** Comparison of traveltimes and residuals from four segments of the inverse results obtained for the 'longside' with receiver at 2014 m. As in Figure 6.9a, the curves for segments 3 and 4 show the least amount or best residuals.





**Figure 6.10:** Comparison of residuals from two-parameter (isotropic) case vs. three-parameter (anisotropic) case. The two-parameter solution is comparable to the three-parameter solution up to about 2600 m. The three-parameter solution encompasses farther offsets and gives a better solution than the two-parameter case.

### 6.3.4 Offset Considerations: Longside, Longoffsets

Subtle geological changes in the medium may be the cause of the results appearing in four segments. The  $ab\chi$  model does not take into account such heterogeneities. Also contributing to the results appearing in four segments may be the way the regression analysis attempts to find the 'best fit'. For near offsets, the traveltime differential relative to the change in offset between shots is not large enough to be detected. The segment where  $a$  decreases and  $b$  increases, segment 2, could be considered as a transition zone where the traveltimes are beginning to show variations with offset,



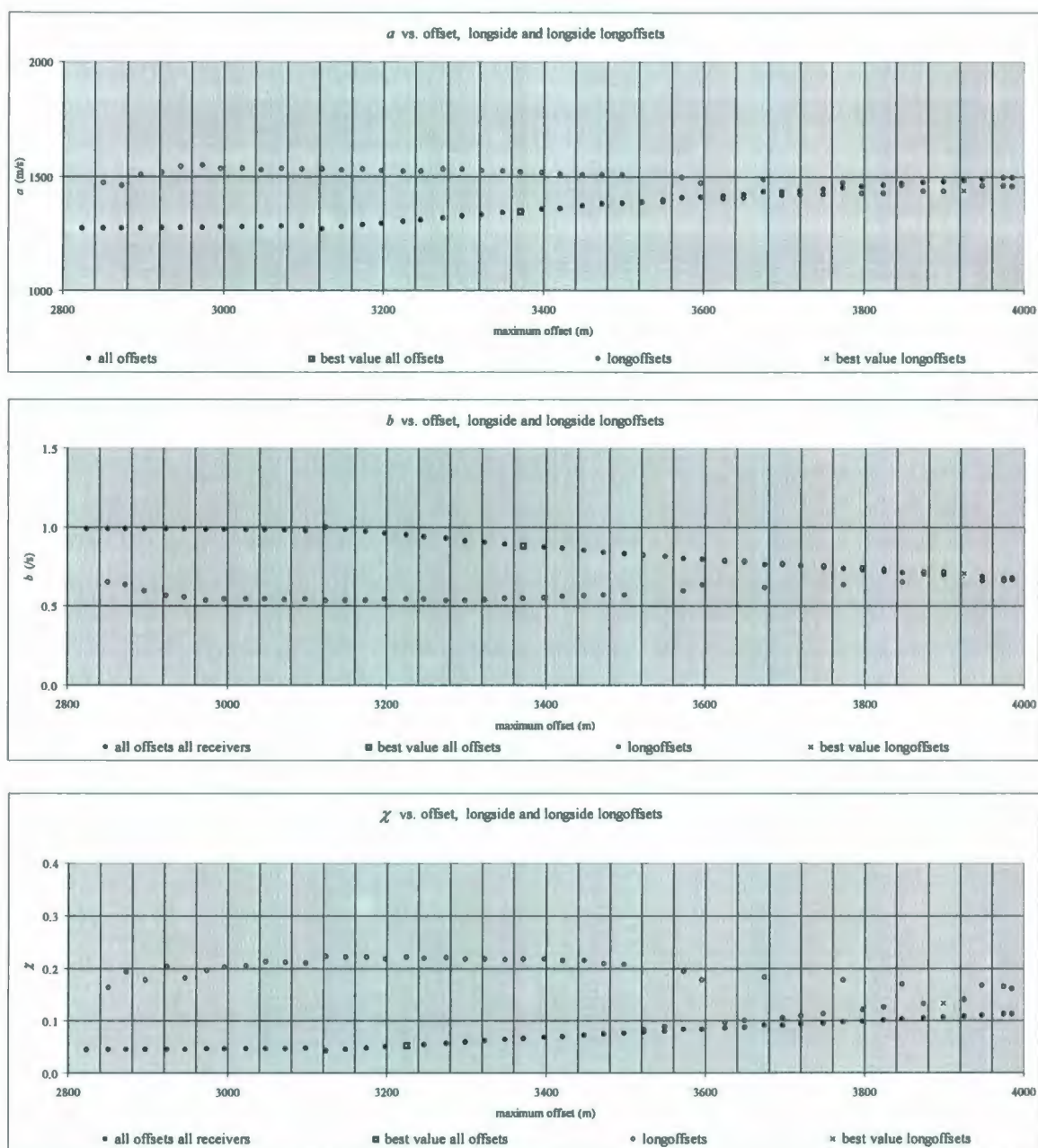
but the regression analysis is affected by the input of the near-offset data. For segment 3, the regression analysis has sufficient data points to be less influenced by the near offsets and, thus, may be giving a truer value of the inverse parameters. Segment 4, which includes very far offsets, is unreliable, due to the possible inclusion of near horizontal or upturned rays or even refracted arrivals.

In order to investigate if not using the near-offset range would give more reliable and better estimates of parameters, offsets were limited to the range: 2849.9 m to 3984.4 m. Results obtained are shown in Table E.8 and Figure 5.9 for  $a$ ,  $b$  and  $\chi \neq 0$  and Table E.3 and Figure 5.4 for  $a$ ,  $b$  and  $\chi = 0$ .

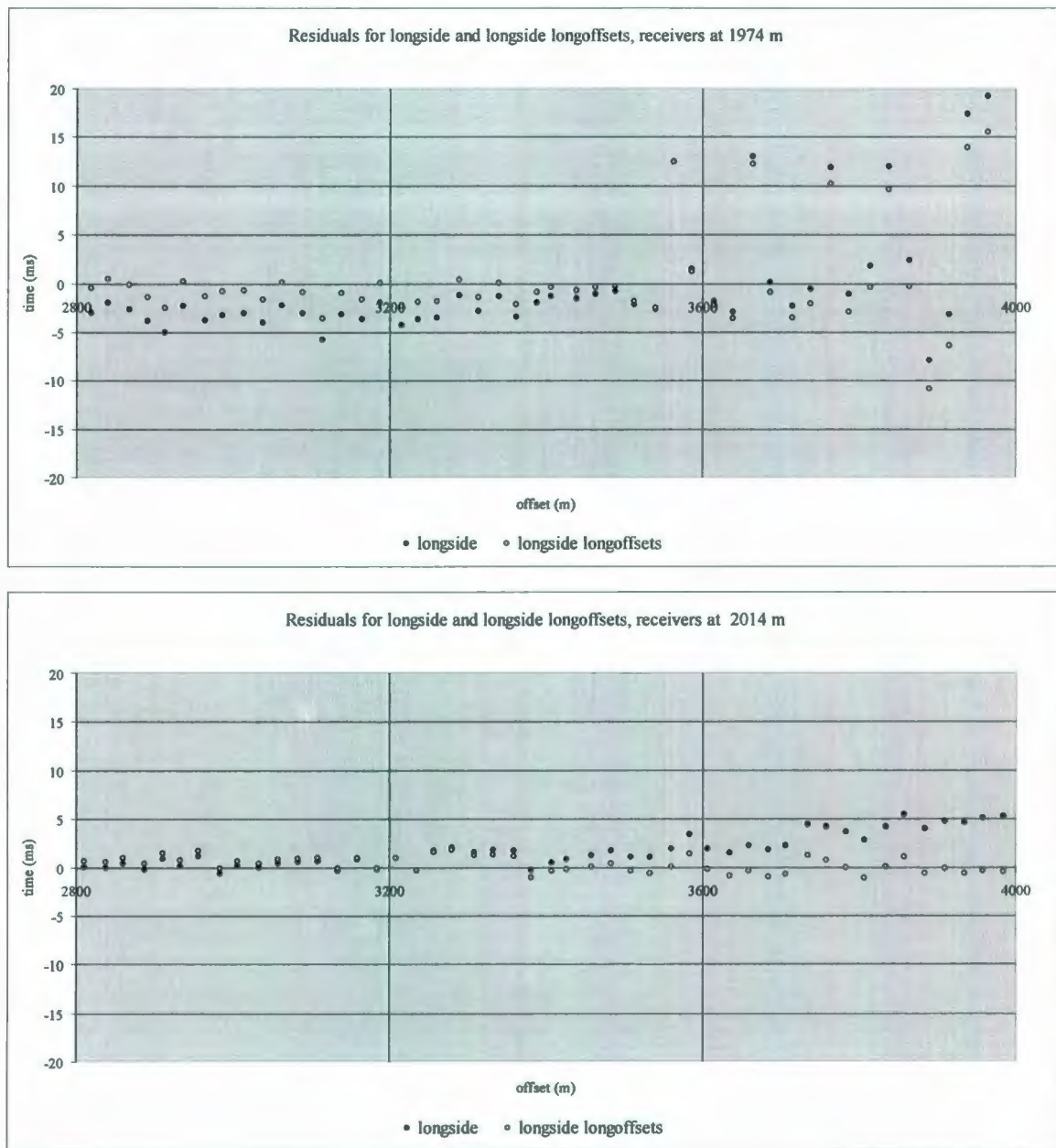
For the isotropic case, Figure 5.4, we see that  $a$  increases as  $b$  decreases correspondingly with offset, for offsets greater than 3000 m, as was observed in this range before in Figure 5.3. For the anisotropic case,  $a$ ,  $b$  and  $\chi$  stay within a small range of values, i.e., are nearly constant as shown in Figure 5.9.

To see the influence that the near data have, values obtained using all offsets and limiting the offsets, are displayed in Figure 6.11. Using only the limited offset range gives more consistent values of  $a$ ,  $b$  and  $\chi$  for the interval. We compute the traveltimes and residuals as before for representative values of  $a$ ,  $b$  and  $\chi$ , and display them for comparison in Figure 6.12.

For the shallow receiver, at 1974 m, the fit using values from the longoffsets only is better (white-dotted curve) than that obtained using all offsets (black-dotted curve), most of the white points lie close to the 0 axis. For the deeper receiver, there is little difference, up to about 3200 m offset and then the white-dotted curve is a better fit, i.e., the longoffsets only again.



**Figure 6.11:** Using all offsets vs. limiting the offsets to longoffsets only. Using only the limited offset range more consistent values for  $a$ ,  $b$  and  $\chi$  are obtained.



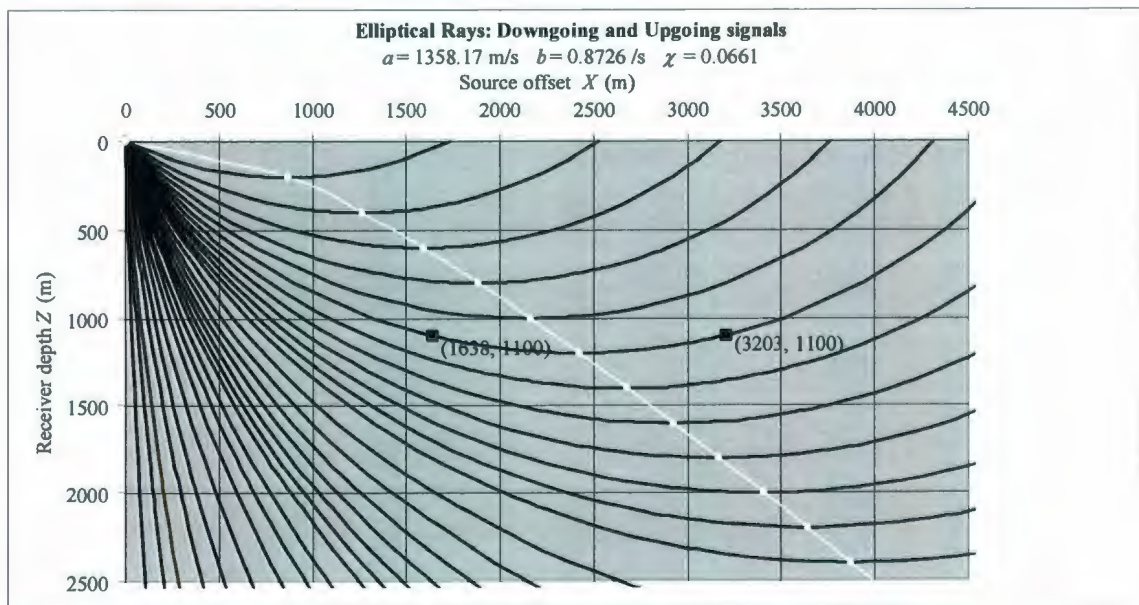
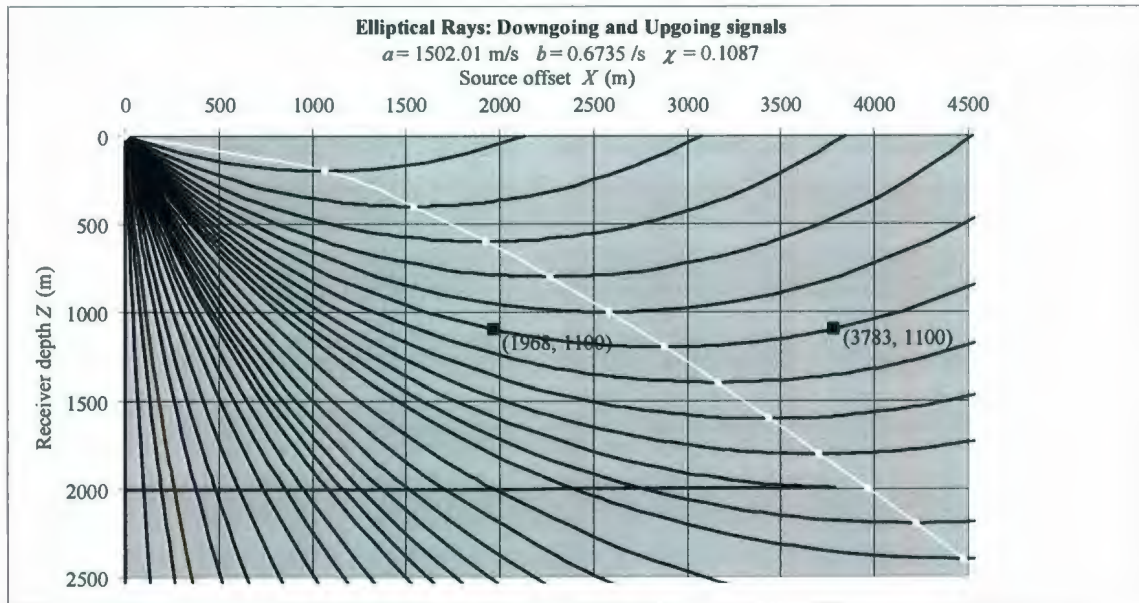
**Figure 6.12:** Comparison of residuals using all offsets vs. limiting the offsets to longoffsets only. For the shallow receiver, at 1974 m (above), the fit using values from the longoffsets only is better, white-dotted curve, than that obtained using all offsets, black-dotted curve; most of the points lie close to the axis. For the deeper receiver, at 2014 m (below) there is little difference, up to about 3200 m offset and then the white-dotted curve, the longoffsets only, is a better fit.



## 6.4 Forward-modelling Equations and Modification

### 6.4.1 Downgoing and Upgoing Signals (Turning Points)

Figures 6.13a and 6.13b show whether receivers in the borehole, for respective values of  $a$ ,  $b$ , and  $\chi$ , are reached by downgoing or upgoing signals. The signals travel along an elliptical arc and depending on the position of the receiver, the signal arriving is either upgoing or downgoing. The black curves are elliptical rays. The white curve in the  $xz$ -plane demarks the separation in locations,  $(x, z)$ , reached by the downgoing signal from those reached by the upgoing signals, i.e., the turning point. The curve is a hyperbola. In Appendix G, we show an example computation. If the receiver position is such that it lies on the left of the white curve, it receives a downgoing signal. If the receiver position is to the right of the curve it receives an upgoing signal. For example, for a location with a source offset of 1968 m and receiver at depth 1100 m, the signal arriving would be downgoing. For a location with a source offset of 3783 m and receiver at depth 1100 m, the signal arriving would be upgoing for  $a = 1502.014$  m/s,  $b = 0.6735$  /s,  $\chi = 0.1087$ . This is useful information in the planning and designing of VSP surveys, since with a reasonable guess of  $a$ ,  $b$  and  $\chi$  one can determine the appropriate depths for receiver placements. Figure 6.13b shows the elliptical rays and turning points computed for a different set of values for  $a$ ,  $b$  and  $\chi$  ( $a = 1358.17$  m/s,  $b = 0.8726$  /s,  $\chi = 0.0661$ ).

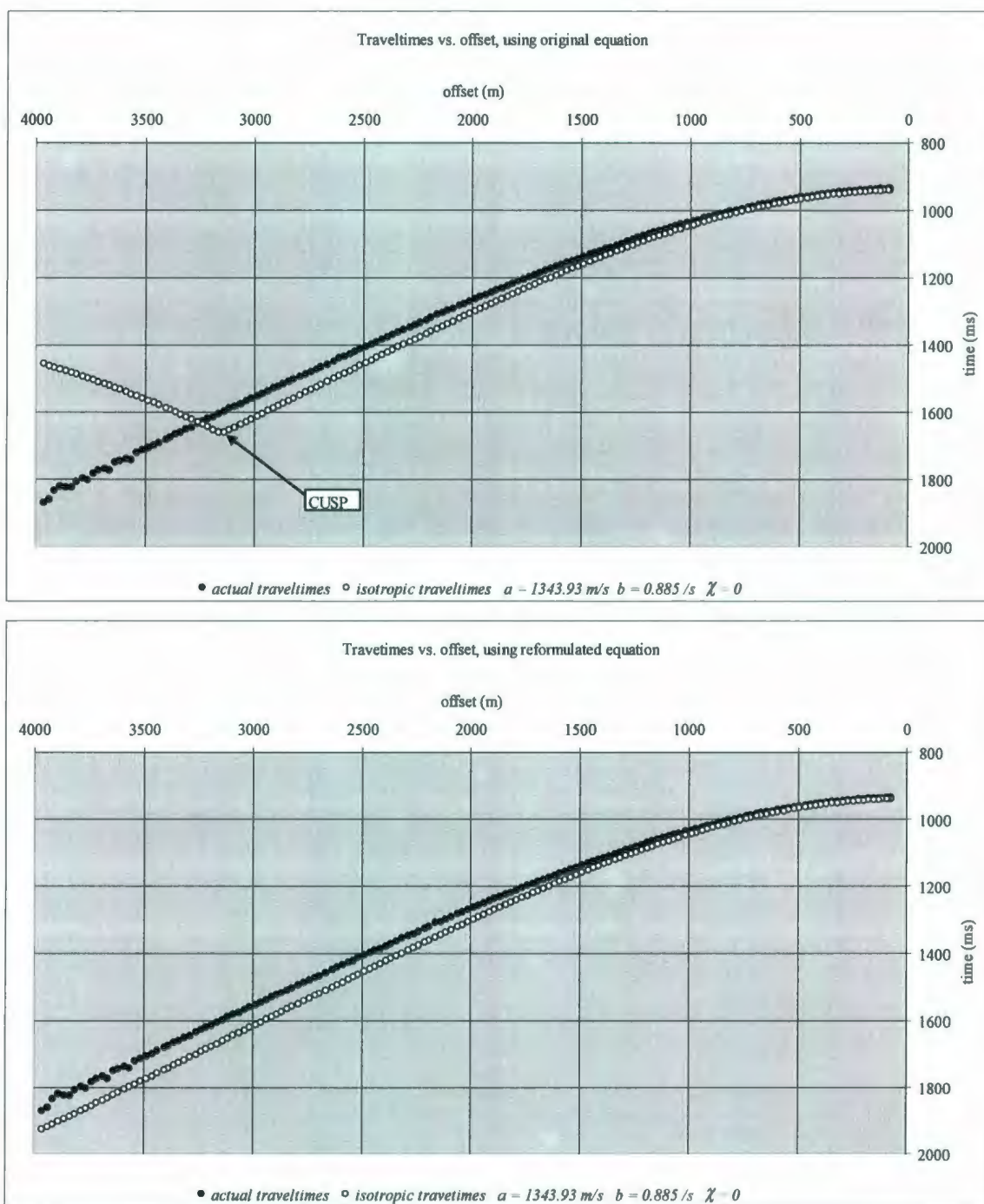


**Figure 6.13a and 6.13b:** Elliptical Rays (black curves) and turning points (white curve). Signals between sources and receivers travel along elliptical arcs. The white curve demarks the separation in locations, reached by the downgoing signal from those reached by the upgoing signals, (the turning point). If the receiver position is to the left of the white curve, it receives a downgoing signal. If the receiver position is to the right of the curve it receives an upgoing signal.

#### 6.4.2 Original Equation and Reformulated Equation

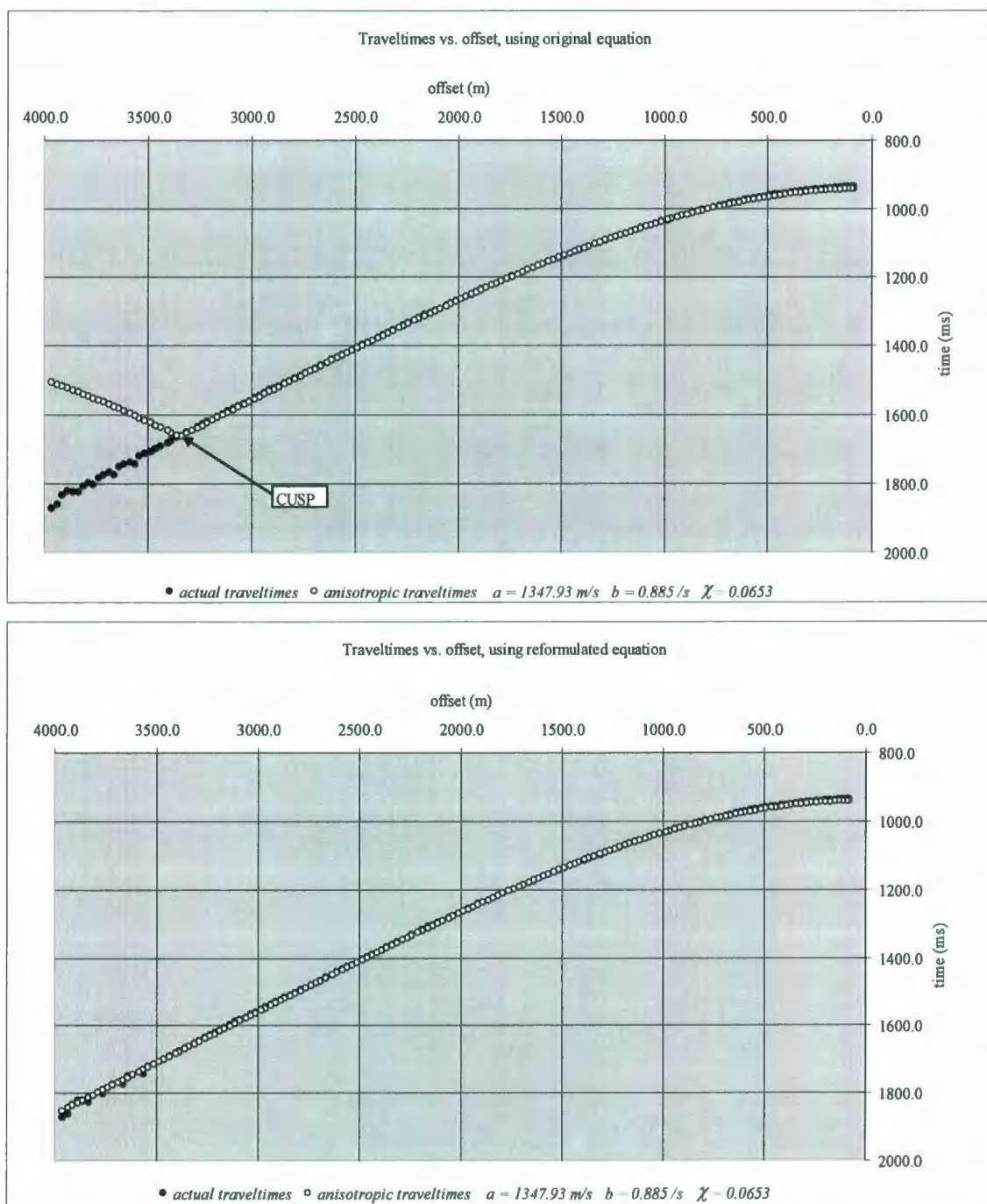
Using expression (1.2) for forward modelling it was found that, depending on the values of  $a$ ,  $b$  and  $\chi$ , a cusp was observed at some offset after which the traveltimes decreased as shown in Figures 6.14a and 6.14b. It was realized that the cusp occurred at the 'turning point' of the ray and was as a result of the original traveltime equation being based on integration along the depth ( $z$ )-axis. Up to the turning point, the signal is downgoing and beyond the turning point, it is upgoing. The cusp arises because the traveltime for the upgoing ray is calculated with the opposite sign than that of the traveltime before the cusp, due to the change of the direction of integration that occurs by integrating along the  $z$ -axis. Physically, this is incorrect: this implies that traveltimes start decreasing from a certain point on. Thus, the original expression is valid only for downgoing rays. After reformulation of the traveltime equation to obtain expression (1.3), by integration performed along the offset ( $x$ )-axis, the cusp disappears, a single-valued function for the ray is obtained and the forward modelling can be extended to far offsets.





**Figure 6.14a:** Comparison of traveltimes from forward modelling using original and reformulated equations, for the isotropic case, illustrating cusp obtained with the original traveltime equation. The original equation was based on integration along the depth ( $z$ )-axis, whereas with the reformulated equation integration is performed along the offset ( $x$ )-axis and the cusp is corrected.





**Figure 6.14b:** Comparison of traveltimes from forward modelling using original and reformulated equations, for the anisotropic case, illustrating cusp obtained with the original traveltime equation. The original equation was based on integration along the depth ( $z$ )-axis, whereas with the reformulated equation integration is performed along the offset ( $x$ )-axis and the cusp is corrected.

## CHAPTER 7: CONCLUSION AND RECOMMENDATIONS

Using the modified algorithm, Wheaton (2004), extensively on a large volume of real data to assess the algorithm was a test of the robustness of the methodology. It brought to light some shortcomings and enabled significant corrections that may otherwise have not been realized. The analytic equation for traveltimes originally formulated was found to be applicable for short offsets, but had to be reformulated for long offsets so that only single-valued functions are obtained with offsets beyond the turning-ray offset. After reformulation, forward modelling was reliably attained for all offsets.

The algorithm appears to be fairly robust and is able to determine  $a$  and  $b$  in an isotropic medium and  $a$ ,  $b$ , and  $\chi$  in an anisotropic medium, provided initial guesses are reasonably realistic. Verifying parameters by forward modelling of the inverse results is an essential and necessary, but not sufficient, part of ensuring that reasonable values are obtained.

In our case, the effect of anisotropy is small. The best-fit value of the ellipticity parameter,  $\chi$ , was found to be 0.0653. Although the anisotropy is small, it is sufficient to affect traveltimes, as has been demonstrated.

Because the anisotropy is small, to determine values correctly, the offset must be long, and traveltimes must be ‘pickable’ on the data. Discrepancies between models and reality can hinder any determination of  $\chi$ .

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## **APPENDICES**



## **APPENDIX A**

### **Zero-offset (Vertical-incidence) VSP: Traveltimes**

**Table A.1: Observed traveltimes for zero-offset (vertical-incidence) VSP.**

Measured receiver depth (KB) (m)	Vertical receiver depth (MSL) (m)	First-break traveltime (ms)	Source offset (m)	cos $\theta$	Observed (vertical) traveltime (msec)	Measured receiver depth (KB) (m)	Vertical receiver depth (MSL) (m)	First-break traveltime (ms)	Source offset (m)	cos $\theta$	Observed (vertical) traveltime (msec)
153.80	130.80	100.10	87.80	0.81776	85.83	2542.00	1997.70	941.90	19.85	0.99995	945.79
442.00	418.60	252.20	78.50	0.98236	251.69	2572.00	2017.90	949.20	0.26	1.00000	953.14
487.00	463.10	274.60	72.20	0.98774	275.17	2602.00	2038.50	957.60	20.61	0.99995	961.49
532.00	507.40	296.40	64.20	0.99190	297.94	2632.00	2059.20	965.70	8.39	0.99999	969.63
622.00	595.10	342.00	45.00	0.99709	344.94	2662.00	2079.80	972.90	8.97	0.99999	976.83
712.00	681.50	384.30	19.80	0.99957	388.07	2692.00	2100.30	980.20	19.47	0.99996	984.09
772.00	738.10	410.70	1.90	1.00000	414.64	2722.00	2120.80	987.70	0.90	1.00000	991.64
862.00	820.90	449.20	5.00	0.99998	453.13	2752.00	2141.20	995.50	21.56	0.99995	999.39
952.00	901.30	487.30	12.10	0.99991	491.19	2782.00	2161.50	1002.50	11.18	0.99999	1006.42
1012.00	953.00	510.40	7.00	0.99997	514.32	2812.00	2181.80	1009.70	10.57	0.99999	1013.63
1087.00	1014.70	540.50	8.00	0.99997	544.42	2842.00	2202.00	1016.80	23.21	0.99994	1020.68
1222.00	1119.90	585.10	0.30	1.00000	589.04	2872.00	2222.00	1023.00	1.71	1.00000	1026.94
1342.00	1205.00	621.40	21.20	0.99984	625.24	2902.00	2241.80	1030.50	20.68	0.99996	1034.39
1432.00	1264.00	647.90	10.00	0.99997	651.82	2932.00	2261.60	1036.90	10.50	0.99999	1040.83
1552.00	1343.40	681.40	22.20	0.99986	685.24	2962.00	2281.40	1041.30	8.91	0.99999	1045.23
1582.00	1362.80	690.50	11.90	0.99996	694.41	2992.00	2301.10	1046.30	21.84	0.99995	1050.19
1612.00	1381.90	698.30	9.50	0.99998	702.22	3022.00	2320.90	1050.90	1.34	1.00000	1054.84
1642.00	1400.90	705.90	21.10	0.99989	709.76	3052.00	2340.60	1055.70	21.13	0.99996	1059.59
1672.00	1419.60	713.70	1.00	1.00000	717.64	3082.00	2360.50	1061.40	11.28	0.99999	1065.32
1702.00	1438.10	721.10	23.50	0.99987	724.94	3112.00	2380.40	1066.40	8.85	0.99999	1070.33
1732.00	1456.60	729.50	12.20	0.99996	733.41	3142.00	2400.50	1071.70	20.43	0.99996	1075.60
1762.00	1475.20	736.50	10.60	0.99997	740.42	3172.00	2420.70	1076.30	0.09	1.00000	1080.24
1792.00	1494.20	744.20	21.30	0.99990	748.06	3202.00	2440.70	1082.00	23.22	0.99995	1085.89
1822.00	1513.90	751.90	0.70	1.00000	755.84	3232.00	2460.70	1086.70	1.00000	1.00000	1090.64
1852.00	1534.10	761.00	22.30	0.99989	764.86	3262.00	2480.60	1091.80	9.75	0.99999	1095.73
1882.00	1554.60	769.80	9.60	0.99998	773.72	3292.00	2500.40	1096.80	19.03	0.99997	1100.71
1912.00	1574.90	777.40	9.50	0.99998	781.32	3322.00	2520.30	1101.80	0.56	1.00000	1105.74
1942.00	1595.10	785.70	21.10	0.99991	789.57	3352.00	2540.30	1107.40	18.99	0.99997	1111.31
1972.00	1615.20	793.10	0.40	1.00000	797.04	3382.00	2560.20	1113.50	10.12	0.99999	1117.43
2002.00	1635.40	801.20	21.10	0.99992	805.07	3412.00	2580.20	1117.80	5.51	1.00000	1121.73
2032.00	1655.50	809.20	8.90	0.99999	813.13	3472.00	2620.50	1127.60	0.73	1.00000	1131.54
2062.00	1675.60	816.60	10.20	0.99998	820.52	3502.00	2640.60	1133.00	21.28	0.99997	1136.90
2092.00	1695.90	823.80	22.00	0.99991	827.67	3532.00	2660.90	1137.80	11.78	0.99999	1141.73
2122.00	1716.10	831.70	1.00	1.00000	835.64	3562.00	2681.10	1142.50	9.90	0.99999	1146.43
2152.00	1736.20	839.50	20.69	0.99993	843.38	3592.00	2701.30	1146.60	21.52	0.99997	1150.50
2182.00	1756.40	848.10	8.08	0.99999	852.03	3622.00	2721.70	1151.20	1.52	1.00000	1155.14
2212.00	1776.40	855.90	10.19	0.99998	859.82	3652.00	2742.00	1156.80	18.39	0.99998	1160.71
2242.00	1796.60	863.70	21.81	0.99993	867.57	3682.00	2762.20	1161.50	11.41	0.99999	1165.43
2272.00	1816.90	872.00	1.06	1.00000	875.94	3712.00	2782.10	1165.80	9.39	0.99999	1169.73
2302.00	1837.10	880.60	21.26	0.99993	884.48	3742.00	2802.00	1171.50	22.07	0.99997	1175.40
2332.00	1857.30	888.20	9.95	0.99999	892.12	3772.00	2822.20	1175.40	1.51	1.00000	1179.34
2362.00	1877.60	895.80	9.57	0.99999	899.73	3802.00	2842.70	1181.20	21.27	0.99997	1185.10
2392.00	1897.80	904.00	20.23	0.99994	907.89	3832.00	2863.50	1185.90	8.76	1.00000	1189.83
2422.00	1917.80	911.10	0.62	1.00000	915.04	3862.00	2884.40	1191.50	9.23	0.99999	1195.43
2452.00	1938.00	918.70	20.77	0.99994	922.58	3892.00	2905.40	1196.30	22.88	0.99997	1200.20
2482.00	1958.10	926.80	12.94	0.99998	930.72	3922.00	2926.30	1201.20	1.33	1.00000	1205.14
2512.00	1977.90	934.10	6.21	1.00000	938.03	3952.00	2947.30	1206.00	19.83	0.99998	1209.91

$$\text{Observed (vertical) traveltime} = (\text{First-break traveltime} * \cos \theta) + \left[ \frac{\text{Source depth}}{\text{Water velocity}} \right]$$

$$\theta = \tan^{-1} \left[ \frac{\text{Source offset}}{\text{Vertical receiver depth} - \text{Source depth}} \right]$$

**Example:**

First-break travelttime: 252.2 ms = 0.2522 s

cos $\theta$ : 0.98236

Source depth: 6.0 m

Water velocity: 1524.0 m/s

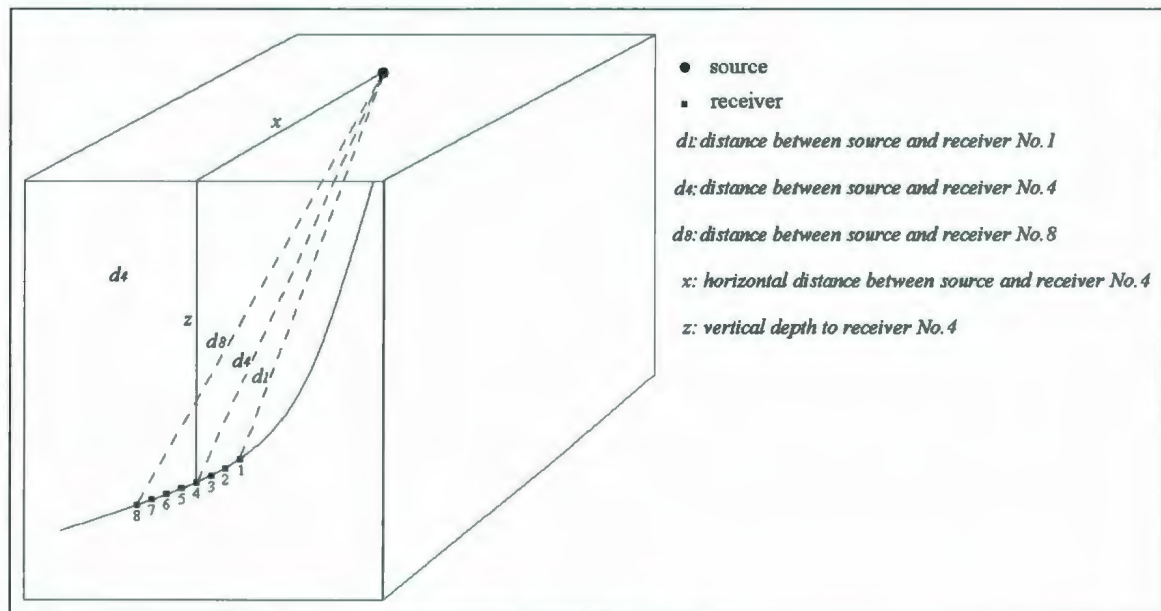
$$\text{Observed (vertical) travelttime} = (0.2522 * 0.98236) + \left[ \frac{6.0}{1524.0} \right] = 0.2517\text{s} = 251.7 \text{ ms}$$

## **APPENDIX B**

### **Walkaround VSP: Traveltimes**



Two adjustments were applied to the traveltimes to remove the effects of variations in source and receiver positions, effectively normalizing the data to a single receiver and single source. The corrections applied are described below and example calculations are shown. Figure B.1 illustrates the layout for a source at surface and the eight-level receiver array in the well. Table B.1 lists corrected traveltimes.



**Figure B.1:** Layout for a source at surface with the eight-level receiver array in the well. The distance from a source position to each receiver varies. Traveltimes were adjusted to account for this variation.

1. Traveltimes recorded were adjusted with respect to a reference receiver (No.4), to account for the difference in source-to-receiver distances due to variations in receiver positioning. The ratio of the distances from a given source position to the reference receiver and to a receiver for which the traveltimes is to be adjusted was applied as shown in expression B.1.

$$t_{an} = \frac{d_4}{d_n} \times t_{rn}, \quad (\text{B.1})$$

where  $t_{an}$  is the adjusted traveltime and  $t_{rn}$  is the recorded traveltime for receiver  $n$ ,

$n = 1 \dots 8$ .

Example:

Distance between source No.1 and receiver No.1 ( $d_1$ ): 2606.37 m.

Distance between source No.1 and receiver No.4 ( $d_4$ ): 2648.90 m.

Distance between source No.1 and receiver No.8 ( $d_8$ ): 2705.89 m.

$$d_1 - d_4 = 2606.37 \text{ m} - 2648.90 \text{ m} = -42.53 \text{ m}$$

$$d_8 - d_4 = 2705.90 \text{ m} - 2648.90 \text{ m} = 57.00 \text{ m}$$

$$t_{a1} = \frac{d_4}{d_1} \times t_{r1}$$

$$t_{a1} = \frac{2648.90 \text{ m}}{2606.37 \text{ m}} \times 1.180576 \text{ s} = 1.199841 \text{ s} = 1.19984 \text{ s}$$

$$t_{a8} = \frac{2648.90 \text{ m}}{2705.89 \text{ m}} \times 1.214355 \text{ s} = 1.188777 \text{ s} = 1.18878 \text{ s}$$

2. Adjusted traveltimes obtained, as described above, were further corrected for the variation in source to receiver distances due to source positioning. Sources were placed radially around the receiver array as shown in Figure 2.5. Source No.14 was used as the reference source for this correction. The ratio of the distances between the reference source and source for which the traveltime is to be corrected was applied as shown in expression B.2.

$$t_{cm} = \frac{s_{14}}{s_m} \times t_{sm}, \quad (\text{B.2})$$

where  $t_{cm}$  is the corrected traveltime and  $t_{sm}$  is the adjusted traveltime, referenced to receiver No.4, for source  $m$ ,  $m = 1 \dots 14$ .

Example:

Distance between source No.1 and receiver No.4: 2648.90 m.

Distance between source No.14 and receiver No.4: 2645.19 m.

Distance between source No.7 and receiver No.4: 2636.58 m.

$$t_{c1} = \frac{s_{14}}{s_1} \times t_{s1}$$

$$t_{c1} = \frac{2645.19\text{m}}{2648.90\text{m}} \times 1.199841\text{s} = 1.198160\text{s} = 1.19816\text{s}$$

$$t_{c7} = \frac{2645.19m}{2636.58m} \times 1.198389s = 1.202302s = 1.20230s$$

Corrections can applied with respect to a reference receiver and then with respect to a reference source or *vice versa*. Table B.1 provides traveltimes adjusted to a reference receiver (No.4), adjusted to a reference source (No.14), and corrected to both the reference receiver and the reference source.



**Table B.1: Traveltimes corrected for variations arising due to source and receiver positioning.** Traveltimes adjusted to a reference receiver (No.4), adjusted to a reference source (No.14), and corrected to both the reference receiver and the reference source are shown.

Source Point No.	Source to receiver azimuth (°)	Source to receiver horizontal distance (m)	Receiver vertical depth from mal (m)	Source to receiver distance (m)	Measured traveltime (s)	Adjusted traveltime referenced to receiver No.4	Adjusted traveltime referenced to SP 14	Corrected traveltime referenced to receiver No.4 and SP 14	Source Point No.	Source to receiver azimuth (°)	Source to receiver horizontal distance (m)	Receiver vertical depth from mal (m)	Source to receiver distance (m)	Measured traveltime (s)	Adjusted traveltime referenced to receiver No.4	Adjusted traveltime referenced to SP 14	Corrected traveltime referenced to receiver No.4 and SP 14
(a)									(b)								
1	359.81	1487.51	2146.20	2606.37	1.180576	1.199841	1.180817	1.198160	8	202.67	1512.36	2146.20	2620.63	1.194752	1.197537	1.188492	1.205948
	-0.02	1497.30	2156.41	2620.45	1.185670	1.198541	1.185268	1.198061		202.66	1501.40	2156.41	2622.68	1.195008	1.196855	1.193587	1.205261
	0.15	1507.31	2166.60	2634.53	1.190809	1.197301	1.189771	1.195623		202.65	1490.44	2166.60	2624.81	1.195382	1.196262	1.198767	1.204664
	0.32	1518.02	2176.78	2648.90	1.195791	1.195791	1.194115	1.194115		202.64	1479.01	2176.78	2626.74	1.195692	1.195692	1.204090	1.204090
	0.49	1528.56	2186.93	2663.25	1.200804	1.194331	1.198499	1.192658		202.64	1467.59	2186.93	2628.74	1.196259	1.195348	1.209640	1.203744
	0.65	1539.10	2197.05	2677.60	1.204522	1.191611	1.201599	1.189941		202.64	1456.17	2197.05	2630.80	1.196324	1.194474	1.214648	1.202864
	0.81	1549.16	2207.12	2691.62	1.209796	1.190593	1.206268	1.188925		202.62	1445.21	2207.12	2633.17	1.196693	1.191776	1.217653	1.200147
	0.98	1559.73	2217.13	2705.89	1.214355	1.188777	1.210216	1.187112		202.62	1433.76	2217.13	2635.29	1.197501	1.193613	1.225391	1.201996
2	27.16	1483.07	2146.20	2603.83	1.177265	1.197211	1.178650	1.195961	9	225.20	1514.99	2146.20	2622.14	1.192519	1.195877	1.185585	1.202998
	27.14	1494.02	2156.41	2618.47	1.182531	1.195847	1.183027	1.194598		225.35	1504.75	2156.41	2624.60	1.192817	1.195055	1.190527	1.202171
	27.12	1504.97	2166.60	2633.09	1.187778	1.194483	1.187395	1.193236		225.50	1494.53	2166.60	2627.13	1.193313	1.194402	1.195633	1.201514
	27.09	1516.37	2176.78	2647.95	1.193021	1.193021	1.191776	1.191776		225.67	1483.96	2176.78	2629.53	1.193739	1.193739	1.200848	1.200848
	27.06	1527.77	2186.93	2662.80	1.198222	1.191539	1.196125	1.190295		225.84	1473.41	2186.93	2631.99	1.194408	1.193289	1.206374	1.200395
	27.03	1539.16	2197.05	2677.64	1.202021	1.188695	1.199087	1.187454		226.01	1462.88	2197.05	2634.52	1.194525	1.192259	1.211109	1.199359
	27.01	1550.12	2207.12	2692.18	1.207618	1.187780	1.203848	1.185560		226.17	1452.70	2207.12	2637.29	1.193010	1.189500	1.214038	1.196583
	26.99	1561.54	2217.13	2706.94	1.212334	1.185915	1.207734	1.184677		226.35	1442.14	2217.13	2639.86	1.194914	1.190235	1.220626	1.197323
3	45.34	1493.13	2146.20	2609.58	1.183625	1.203072	1.182411	1.199777	10	247.20	1510.99	2146.20	2619.84	1.192137	1.197301	1.186250	1.203672
	45.19	1503.36	2156.41	2623.81	1.188667	1.201644	1.186745	1.198353		247.49	1502.98	2156.41	2623.59	1.193144	1.196598	1.191313	1.202965
	45.04	1513.61	2166.60	2638.03	1.193723	1.200248	1.191102	1.196961		247.77	1495.02	2166.60	2627.41	1.194933	1.196651	1.197129	1.203018
	44.88	1524.22	2176.78	2652.45	1.198775	1.198775	1.195491	1.195491		248.08	1486.90	2176.78	2631.19	1.195333	1.195333	1.201693	1.201693
	44.72	1534.84	2186.93	2666.86	1.203769	1.197263	1.199832	1.193984		248.40	1478.83	2186.93	2635.03	1.196964	1.195219	1.207463	1.201578
	44.57	1545.47	2197.05	2681.27	1.207414	1.194439	1.202836	1.191167		248.71	1470.80	2197.05	2638.93	1.196909	1.193396	1.211499	1.199746
	44.43	1555.76	2207.12	2695.43	1.212903	1.193565	1.207659	1.190296		249.01	1463.00	2207.12	2642.97	1.197380	1.192040	1.215864	1.198383
	44.28	1566.45	2217.13	2709.78	1.217497	1.191742	1.211609	1.188477		249.33	1455.00	2217.13	2646.91	1.198415	1.191296	1.220945	1.197635
4	67.86	1489.92	2146.20	2607.74	1.181961	1.199595	1.181579	1.198933	11	269.66	1507.96	2146.20	2618.09	1.189698	1.197626	1.184611	1.202009
	67.57	1497.87	2156.41	2620.67	1.186488	1.198251	1.185989	1.197589		270.04	1503.44	2156.41	2623.85	1.191255	1.196562	1.189309	1.200942
	67.28	1505.87	2166.60	2633.60	1.190787	1.196888	1.190172	1.196027		270.42	1498.98	2166.60	2629.66	1.193167	1.195833	1.194335	1.200210
	66.98	1514.09	2176.78	2646.65	1.195362	1.195362	1.194702	1.194702		270.82	1494.59	2176.78	2635.54	1.194854	1.194854	1.199227	1.199227
	66.69	1522.36	2186.93	2659.70	1.199723	1.193834	1.199018	1.193174		271.23	1490.28	2186.93	2641.47	1.196741	1.194053	1.204293	1.198423
	66.39	1530.67	2197.05	2672.76	1.202706	1.190955	1.201958	1.190297		271.64	1486.05	2197.05	2647.46	1.197197	1.191807	1.207888	1.196169
	66.12	1538.82	2207.12	2685.68	1.207619	1.190067	1.206759	1.189409		272.03	1481.87	2207.12	2653.46	1.199276	1.191175	1.212974	1.195534
	65.83	1547.26	2217.13	2698.72	1.211687	1.188306	1.210765	1.187649		272.44	1477.72	2217.13	2659.47	1.200869	1.190066	1.217669	1.194421
5	90.59	1496.14	2146.20	2611.30	1.181047	1.195881	1.179055	1.196372	12	291.95	1499.68	2146.20	2613.33	1.186885	1.198089	1.183963	1.201352
	90.21	1500.57	2156.41	2622.21	1.184600	1.194489	1.183405	1.194980		292.37	1499.28	2156.41	2621.47	1.189364	1.196863	1.188498	1.200123
	89.83	1505.07	2166.60	2633.14	1.188293	1.193239	1.187885	1.193729		292.78	1498.97	2166.60	2629.66	1.191873	1.195654	1.193042	1.198911
	89.43	1509.64	2176.78	2644.10	1.192145	1.192145	1.192634	1.192634		293.22	1498.93	2176.78	2638.00	1.194174	1.194174	1.197426	1.197426
	89.04	1514.28	2186.93	2655.08	1.195878	1.190931	1.197255	1.191420		293.66	1498.98	2186.93	2646.39	1.196862	1.193069	1.202178	1.196318
	88.64	1518.99	2197.05	2666.09	1.198432	1.188548	1.200684	1.189036		294.09	1499.11	2197.05	2654.82	1.198182	1.190594	1.205532	1.193836
	88.27	1523.76	2207.12	2677.08	1.202638	1.187821	1.205642	1.188309		294.51	1499.13	2207.12	2663.14	1.201070	1.189732	1.210374	1.192972
	87.88	1528.67	2217.13	2688.11	1.205965	1.186221	1.209805	1.186708		294.95	1499.38	2217.13	2671.56	1.203406	1.188290	1.214717	1.191526
6	112.89	1502.42	2146.20	2614.91	1.186092	1.197712	1.182460	1.199827	13	314.46	1496.26	2146.20	2611.37	1.186359	1.200885	1.184328	1.201722
	112.48	1502.72	2156.41	2623.44	1.188914	1.196657	1.187159	1.198770		314.85	1500.09	2156.41	2621.93	1.190034	1.199752	1.188959	1.200588
	112.06	1503.09	2166.60	2632.01	1.191880	1.195734	1.191982	1.197846		315.24	1503.99	2166.60	2632.52	1.193866	1.198774	1.193737	1.199609
	111.62	1503.36	2176.78	2640.52	1.195018	1.195018	1.197128	1.197128		315.65	1508.31	2176.78	2643.34	1.197490	1.197490	1.198325	1.198325
	111.19	1503.72	2186.93	2649.08	1.198035	1.194166	1.202134	1.196275		316.05	1512.71	2186.93	2654.19	1.201128	1.196219	1.202916	1.197053
	110.75	1504.16	2197.05	2657.67	1.199630	1.191890	1.205692	1.193995		316.44	1517.18	2197.05	2665.06	1.203274	1.193469	1.206001	1.194301
	110.34	1504.87	2207.12	2666.38	1.202864	1.191201	1.210711	1.193304		316.83	1521.36	2207.12	2675.72	1.207288	1.192679	1.210920	1.193511
	109.90	1505.54	2217.13	2675.02	1.205548	1.190000	1.215303	1.192101		317.22	1525.93	2217.13	2686.55	1.210394	1.190926	1.214951	1.191756
7	135.40	1508.34	2146.20	2618.31	1.190086	1.198389	1.184899	1.202302	14	337.24	1488.44	2146.20	2606.90	1.181058	1.198404	1.181058	1.198404
	135.01	1504.41	2156.41	2624.41	1.192038	1.197565	1.189837	1.201475		337.54	1495.94	2156.41	2619.56	1.185591	1.197718	1.185591	1.197718
	134.62	1505.66	2166.60	2630.57	1.194156	1.196926	1.194955	1.200883		337.83	1503.49	2166.60	2632.24	1.190270	1.196125	1.190270	1.196125
	134.21	1496.42	2176.78	2636.58	1.196383	1.196383	1.200289	1.200289		338.16	1511.54	2176.78	2645.19	1.194668	1.194668	1.194668	1.194668
	133.80	1492.36	2186.93	2642.65	1.198493	1.195740	1.205519	1.196446		338.46	1519.63	2186.93	2658.14	1.199249	1.193404	1.199249	1.193404
	133.39	1488.38	2197.05	2648.77	1.199071	1.193551	1.209179	1.197448		338.76	1527.77	2197.05	2671.10	1.202408	1.190743	1.202408	1.190743
	132.99	1484.82	2207.12	2655.11	1.201366	1.192979	1.214333	1.196874		339.05	1539.48	2207.12	2683.77	1.207210	1.189854	1.207210	1.189854
	132.57	1481.04	2217.13	2661.31	1.203122	1.191942	1.219107	1.195833		339.35	1543.67	2217.13	2696.67	1.211217	1.188093	1.211217	1.188093

## **APPENDIX C**

### **Walkaway VSP: Traveltimes**

**Table C.1: Traveltimes for Receiver 1.**

Receiver Depth = 1973.923 m											
Source N.o.	Source Offset (m)	Travelttime (ms)	Source N.o.	Source Offset (m)	Travelttime (ms)	Source N.o.	Source Offset (m)	Travelttime (ms)	Source N.o.	Source Offset (m)	Travelttime (ms)
1	1014.078	1036.432	51	244.406	941.458	101	1485.368	1136.798	151	2737.504	1478.316
2	989.797	1031.409	52	270.447	942.481	102	1513.211	1143.508	152	2763.498	1486.156
3	966.288	1027.439	53	293.032	944.033	103	1539.303	1149.417	153	2790.900	1492.776
4	941.466	1023.055	54	317.805	945.562	104	1565.130	1154.933	154	2818.515	1501.544
5	915.969	1018.204	55	343.415	947.720	105	1588.644	1160.874	155	2840.130	1509.010
6	889.718	1014.435	56	369.719	949.464	106	1612.475	1167.062	156	2867.558	1516.612
7	864.303	1010.473	57	393.092	952.038	107	1638.883	1173.549	157	2891.097	1522.475
8	841.107	1005.947	58	417.457	953.379	108	1663.079	1178.955	158	2913.083	1527.969
9	816.118	1002.145	59	443.392	956.346	109	1689.771	1185.425	159	2936.480	1537.739
10	788.795	998.318	60	465.151	958.015	110	1711.871	1191.324	160	2963.685	1544.497
11	765.793	994.844	61	493.184	960.078	111	1739.048	1197.521	161	2985.984	1551.710
12	740.308	991.292	62	515.711	963.346	112	1763.081	1203.817	162	3013.154	1560.112
13	716.162	987.772	63	541.511	965.572	113	1789.370	1210.837	163	3037.280	1566.471
14	694.514	985.218	64	566.218	968.150	114	1814.387	1217.784	164	3062.143	1575.806
15	663.944	980.535	65	594.084	971.846	115	1836.461	1223.474	165	3087.867	1582.710
16	642.565	977.875	66	616.525	974.437	116	1863.985	1231.080	166	3113.355	1587.800
17	617.231	975.246	67	640.390	977.709	117	1888.688	1235.614	167	3137.870	1597.852
18	591.674	971.165	68	666.096	980.848	118	1912.386	1242.405	168	3163.910	1605.218
19	568.580	968.847	69	686.674	983.892	119	1936.696	1250.340	169	3187.722	1614.170
20	538.050	966.045	70	714.131	987.625	120	1962.993	1255.989	170	3214.578	1620.041
21	515.799	963.125	71	734.065	990.735	121	1986.236	1262.363	171	3236.351	1627.195
22	489.340	960.062	72	763.765	994.462	122	2011.513	1269.025	172	3259.675	1634.435
23	469.040	958.225	73	790.341	998.943	123	2038.012	1276.389	173	3288.287	1645.422
24	444.262	955.686	74	818.537	1002.359	124	2058.654	1281.452	174	3312.831	1651.273
25	418.215	953.700	75	838.613	1006.107	125	2089.406	1291.095	175	3338.804	1660.710
26	394.946	951.439	76	864.183	1009.904	126	2113.127	1297.340	176	3361.215	1665.429
27	373.059	949.506	77	889.644	1015.459	127	2137.010	1304.095	177	3387.640	1674.863
28	344.072	948.215	78	916.870	1018.333	128	2162.001	1308.005	178	3405.836	1681.033
29	324.116	946.461	79	938.114	1022.636	129	2190.353	1318.307	179	3438.279	1690.683
30	297.101	944.746	80	967.871	1028.093	130	2208.538	1324.103	180	3462.882	1698.660
31	275.418	943.693	81	984.094	1032.088	131	2240.131	1332.692	181	3488.647	1706.745
32	246.708	941.976	82	1014.404	1035.925	132	2262.848	1340.505	182	3512.857	1712.753
33	225.285	940.090	83	1043.220	1041.995	133	2285.069	1346.629	183	3539.715	1720.417
34	201.211	938.334	84	1065.184	1046.384	134	2313.522	1354.231	184	3562.825	1742.573
35	182.634	937.775	85	1088.895	1050.471	135	2338.818	1361.689	185	3586.331	1738.627
36	151.037	937.281	86	1115.015	1055.210	136	2364.031	1368.898	186	3614.704	1743.987
37	136.395	936.890	87	1140.098	1060.235	137	2387.757	1376.166	187	3639.544	1750.378
38	119.615	936.139	88	1165.295	1065.256	138	2414.140	1384.134	188	3664.411	1773.884
39	94.406	935.931	89	1187.085	1070.389	139	2438.493	1389.482	189	3686.858	1767.780
40	82.931	935.126	90	1214.352	1075.694	140	2462.794	1396.500	190	3715.162	1773.923
41	76.916	935.534	91	1238.248	1080.502	141	2487.398	1404.673	191	3738.511	1782.683
42	74.741	935.336	92	1262.578	1085.769	142	2515.010	1412.021	192	3763.146	1802.645
43	84.530	935.707	93	1288.093	1092.119	143	2538.668	1420.411	193	3787.190	1796.954
44	93.234	935.612	94	1312.260	1097.591	144	2561.908	1425.506	194	3813.895	1807.817
45	112.705	936.244	95	1337.566	1102.887	145	2586.946	1432.678	195	3837.164	1825.078
46	130.648	936.110	96	1366.579	1110.075	146	2611.466	1439.409	196	3863.906	1823.494
47	152.613	937.377	97	1386.806	1113.877	147	2634.472	1447.930	197	3889.009	1820.780
48	176.332	938.209	98	1413.235	1120.171	148	2664.740	1457.009	198	3914.736	1833.245
49	200.664	939.183	99	1434.249	1125.078	149	2693.145	1465.913	199	3937.224	1860.562
50	222.033	940.566	100	1457.820	1129.865	150	2713.475	1471.688	200	3964.125	1870.558



**Table C.2: Traveltimes for Receiver 2.**

Receiver Depth = 1983.809 m											
Source N.o.	Source Offset (m)	Travelttime (ms)	Source N.o.	Source Offset (m)	Travelttime (ms)	Source N.o.	Source Offset (m)	Travelttime (ms)	Source N.o.	Source Offset (m)	Travelttime (ms)
201	1008.351	1038.840	251	247.111	945.205	301	1490.113	1140.644	351	2742.351	1481.698
202	984.043	1033.122	252	273.339	946.367	302	1517.949	1147.233	352	2768.347	1489.435
203	960.508	1029.148	253	296.045	947.988	303	1544.086	1153.155	353	2795.751	1496.836
204	935.676	1025.027	254	321.033	949.649	304	1569.900	1158.895	354	2823.373	1504.003
205	910.130	1021.168	255	346.827	952.137	305	1593.404	1164.270	355	2845.001	1510.775
206	883.891	1017.319	256	373.160	953.549	306	1617.242	1170.602	356	2872.444	1517.430
207	858.483	1013.209	257	396.718	955.886	307	1643.658	1177.444	357	2895.995	1527.097
208	835.240	1008.312	258	421.107	957.665	308	1667.848	1182.653	358	2917.992	1531.993
209	810.244	1004.878	259	447.157	960.745	309	1694.537	1189.136	359	2941.398	1540.569
210	782.892	1001.203	260	469.001	962.260	310	1716.647	1194.793	360	2968.622	1546.735
211	759.852	997.567	261	497.013	964.153	311	1743.842	1201.199	361	2990.918	1553.385
212	734.346	994.381	262	519.641	967.471	312	1767.872	1207.696	362	3018.090	1561.528
213	710.170	990.638	263	545.499	969.745	313	1794.159	1214.073	363	3042.218	1568.398
214	688.527	988.177	264	570.228	972.201	314	1819.208	1220.868	364	3067.084	1576.207
215	657.899	983.886	265	598.156	975.986	315	1841.269	1226.550	365	3092.811	1585.550
216	636.545	981.287	266	620.641	978.617	316	1868.805	1233.862	366	3118.302	1590.731
217	611.188	977.982	267	644.580	981.874	317	1893.512	1240.130	367	3142.820	1600.101
218	585.598	974.139	268	670.325	985.060	318	1917.232	1246.604	368	3168.861	1608.303
219	562.487	971.586	269	691.031	988.157	319	1941.535	1253.548	369	3192.675	1615.857
220	531.796	968.724	270	718.482	991.753	320	1967.839	1259.847	370	3219.534	1622.663
221	509.525	966.093	271	738.482	994.879	321	1991.090	1265.565	371	3241.315	1631.572
222	483.059	963.084	272	768.171	998.693	322	2016.374	1273.312	372	3264.630	1638.071
223	462.703	961.095	273	794.790	1002.989	323	2042.866	1280.025	373	3293.246	1647.669
224	437.891	958.631	274	822.941	1006.748	324	2063.524	1285.407	374	3317.799	1653.441
225	411.844	956.849	275	843.036	1010.184	325	2094.281	1294.071	375	3343.766	1662.421
226	388.454	954.877	276	868.614	1013.894	326	2117.996	1299.952	376	3366.177	1667.257
227	366.440	953.134	277	894.119	1019.595	327	2141.883	1307.700	377	3392.607	1675.520
228	337.400	951.426	278	921.307	1022.321	328	2166.886	1310.301	378	3410.802	1681.964
229	317.048	949.415	279	942.569	1027.050	329	2195.224	1323.274	379	3443.246	1691.929
230	289.835	947.845	280	972.347	1032.722	330	2213.413	1327.841	380	3467.846	1710.587
231	267.858	946.987	281	988.598	1036.735	331	2245.016	1336.037	381	3493.613	1709.635
232	239.050	945.197	282	1018.913	1040.235	332	2267.713	1343.859	382	3517.821	1713.031
233	217.478	943.625	283	1047.728	1045.885	333	2289.923	1348.996	383	3544.681	1722.879
234	193.088	942.345	284	1069.727	1050.348	334	2318.389	1357.301	384	3567.794	1741.318
235	174.105	941.309	285	1093.448	1054.671	335	2343.698	1365.345	385	3591.299	1736.081
236	142.494	940.727	286	1119.573	1059.151	336	2368.914	1372.069	386	3619.680	1747.966
237	126.875	940.937	287	1144.664	1064.439	337	2392.644	1379.635	387	3644.514	1752.301
238	109.503	939.762	288	1169.907	1069.724	338	2419.031	1386.817	388	3669.383	1778.166
239	83.743	939.623	289	1191.722	1074.964	339	2443.401	1392.626	389	3691.832	1770.612
240	71.966	938.903	290	1219.006	1080.203	340	2467.697	1400.358	390	3720.138	1775.954
241	66.459	939.149	291	1242.914	1084.769	341	2492.313	1408.040	391	3743.487	1783.222
242	66.310	939.227	292	1267.262	1090.486	342	2519.922	1415.364	392	3768.123	1791.143
243	78.328	939.528	293	1292.784	1096.443	343	2543.581	1422.726	393	3792.172	1802.154
244	89.803	939.563	294	1316.929	1101.800	344	2566.833	1429.279	394	3818.878	1808.063
245	111.608	940.394	295	1342.261	1107.092	345	2591.883	1436.051	395	3842.148	1812.050
246	130.642	940.091	296	1371.339	1113.786	346	2616.403	1443.447	396	3868.893	1834.522
247	153.154	941.688	297	1391.577	1118.027	347	2639.425	1451.370	397	3893.998	1832.293
248	177.687	942.350	298	1418.030	1124.079	348	2669.654	1459.092	398	3919.728	1841.510
249	202.354	943.109	299	1439.032	1129.362	349	2698.020	1468.384	399	3942.218	1849.791
250	224.320	944.924	300	1462.608	1134.666	350	2718.334	1472.716	400	3969.119	1856.989



**Table C.3: Traveltimes for Receiver 3.**

Receiver Depth = 1993.699 m											
Source N.o.	Source Offset (m)	Travelttime (ms)	Source N.o.	Source Offset (m)	Travelttime (ms)	Source N.o.	Source Offset (m)	Travelttime (ms)	Source N.o.	Source Offset (m)	Travelttime (ms)
401	1002.711	1040.296	451	250.268	949.125	501	1494.924	1144.481	551	2747.233	1483.652
402	978.378	1034.723	452	276.636	950.369	502	1522.751	1151.295	552	2773.232	1491.746
403	954.820	1031.448	453	299.430	952.101	503	1548.932	1156.979	553	2800.637	1498.916
404	929.979	1027.611	454	324.600	953.662	504	1574.732	1162.905	554	2828.265	1506.587
405	904.386	1023.126	455	350.549	955.781	505	1598.225	1168.160	555	2849.906	1514.083
406	878.162	1019.032	456	376.889	957.374	506	1622.070	1174.337	556	2877.363	1521.606
407	852.764	1015.012	457	400.611	960.273	507	1648.491	1180.674	557	2900.926	1528.903
408	829.477	1010.589	458	425.009	961.745	508	1672.676	1186.362	558	2922.933	1535.242
409	804.476	1007.059	459	451.156	964.632	509	1699.359	1192.925	559	2946.349	1542.711
410	777.100	1003.557	460	473.074	966.243	510	1721.478	1198.836	560	2973.590	1550.466
411	754.023	999.276	461	501.052	968.510	511	1748.692	1204.910	561	2995.885	1557.133
412	728.501	996.141	462	523.771	971.570	512	1772.717	1211.548	562	3023.058	1565.767
413	704.297	992.892	463	549.677	973.782	513	1799.002	1217.934	563	3047.187	1573.079
414	682.665	990.319	464	574.419	976.722	514	1824.082	1224.612	564	3072.056	1580.030
415	651.983	986.067	465	602.401	980.039	515	1846.130	1230.545	565	3097.786	1588.145
416	630.660	982.786	466	624.922	982.692	516	1873.676	1237.567	566	3123.280	1595.589
417	605.282	980.150	467	648.928	985.882	517	1898.386	1244.110	567	3147.799	1603.017
418	579.666	976.420	468	674.706	988.900	518	1922.128	1250.350	568	3173.841	1610.568
419	556.544	974.146	469	695.534	992.308	519	1946.425	1256.844	569	3197.658	1618.286
420	525.697	971.431	470	722.973	995.547	520	1972.733	1263.463	570	3224.520	1625.947
421	503.412	968.550	471	743.035	998.774	521	1995.992	1269.489	571	3246.308	1633.840
422	476.947	965.518	472	772.708	1002.640	522	2021.284	1276.605	572	3269.615	1641.181
423	456.543	963.432	473	799.365	1007.501	523	2047.768	1283.477	573	3298.234	1648.665
424	431.704	961.216	474	827.466	1010.404	524	2068.441	1289.092	574	3322.795	1656.675
425	405.669	959.313	475	847.578	1014.153	525	2099.202	1297.742	575	3348.757	1664.216
426	382.167	957.363	476	873.161	1017.853	526	2122.910	1304.563	576	3371.168	1670.785
427	360.032	955.795	477	898.705	1023.541	527	2146.801	1310.749	577	3397.601	1678.696
428	330.958	953.984	478	925.852	1026.076	528	2171.815	1314.782	578	3415.795	1685.196
429	310.206	952.081	479	947.130	1030.365	529	2200.140	1325.703	579	3448.241	1694.415
430	282.808	950.759	480	976.925	1036.107	530	2218.331	1331.626	580	3472.837	1701.577
431	260.541	949.642	481	993.203	1040.563	531	2249.944	1339.540	581	3498.606	1710.192
432	231.657	948.256	482	1023.519	1044.037	532	2272.620	1346.336	582	3522.813	1717.371
433	209.954	946.459	483	1052.331	1049.905	533	2294.818	1352.489	583	3549.675	1725.993
434	185.259	945.197	484	1074.363	1054.403	534	2323.298	1360.202	584	3572.790	1733.222
435	165.862	944.430	485	1098.092	1058.814	535	2348.619	1368.284	585	3596.293	1739.830
436	134.304	943.874	486	1124.219	1063.483	536	2373.838	1375.471	586	3624.682	1748.377
437	117.607	943.475	487	1149.317	1068.660	537	2397.572	1382.493	587	3649.510	1756.174
438	99.571	942.953	488	1174.603	1073.632	538	2423.962	1389.803	588	3674.382	1763.768
439	73.169	942.483	489	1196.443	1078.861	539	2448.348	1396.371	589	3696.833	1770.490
440	61.000	941.891	490	1223.741	1084.101	540	2472.638	1403.782	590	3725.141	1779.702
441	56.197	942.147	491	1247.658	1088.584	541	2497.266	1411.481	591	3748.488	1786.963
442	58.722	942.353	492	1272.022	1094.326	542	2524.872	1418.757	592	3773.125	1794.582
443	73.252	942.618	493	1297.550	1100.294	543	2548.532	1425.434	593	3797.180	1802.597
444	87.620	942.868	494	1321.672	1105.547	544	2571.795	1432.337	594	3823.886	1810.145
445	111.582	943.735	495	1347.028	1110.953	545	2596.858	1439.589	595	3847.157	1817.675
446	131.554	943.171	496	1376.170	1117.626	546	2621.377	1446.632	596	3873.904	1825.487
447	154.473	945.169	497	1396.418	1121.891	547	2644.413	1453.807	597	3899.011	1833.940
448	179.703	945.881	498	1422.895	1128.178	548	2674.605	1462.258	598	3924.745	1841.541
449	204.619	946.732	499	1443.884	1132.653	549	2702.929	1470.753	599	3947.236	1849.245
450	227.115	948.627	500	1467.463	1138.044	550	2723.228	1476.894	600	3974.137	1857.089



**Table C.4: Traveltimes for Receiver 4.**

Receiver Depth = 2003.758 m											
Source N.o.	Source Offset (m)	Traveltime (ms)	Source N.o.	Source Offset (m)	Traveltime (ms)	Source N.o.	Source Offset (m)	Traveltime (ms)	Source N.o.	Source Offset (m)	Traveltime (ms)
601	997.086	1042.833	651	253.949	953.203	701	1499.879	1148.672	751	2752.229	1487.699
602	972.731	1037.513	652	280.412	954.468	702	1527.695	1155.408	752	2778.230	1494.594
603	949.152	1033.673	653	303.261	956.100	703	1553.918	1161.119	753	2805.637	1502.098
604	924.305	1029.444	654	328.581	957.547	704	1579.704	1167.420	754	2833.270	1508.771
605	898.668	1025.462	655	354.657	959.877	705	1603.186	1172.206	755	2854.923	1516.733
606	872.462	1021.558	656	380.983	961.524	706	1627.036	1178.204	756	2882.394	1525.492
607	847.076	1017.731	657	404.849	964.467	707	1653.462	1184.507	757	2905.969	1531.940
608	823.748	1012.982	658	429.240	965.664	708	1677.641	1190.805	758	2927.986	1539.600
609	798.746	1009.341	659	455.469	968.875	709	1704.318	1197.292	759	2951.411	1546.765
610	771.348	1005.985	660	477.448	970.314	710	1726.445	1203.018	760	2978.669	1554.718
611	748.238	1002.028	661	505.381	972.350	711	1753.676	1209.147	761	3000.961	1561.351
612	722.703	999.005	662	528.180	975.954	712	1777.695	1215.748	762	3028.136	1568.134
613	698.475	995.761	663	554.124	977.649	713	1803.977	1221.607	763	3052.265	1577.714
614	676.858	993.036	664	578.871	980.507	714	1829.087	1228.617	764	3077.138	1582.686
615	646.129	988.844	665	606.897	984.222	715	1851.122	1234.195	765	3102.869	1590.615
616	624.840	985.924	666	629.448	987.011	716	1878.678	1241.198	766	3128.367	1599.738
617	599.449	983.380	667	653.514	990.246	717	1903.390	1247.676	767	3152.887	1606.000
618	573.811	979.481	668	679.317	993.458	718	1927.153	1254.113	768	3178.930	1613.464
619	550.684	977.140	669	700.261	996.693	719	1951.442	1260.869	769	3202.748	1619.519
620	519.689	974.557	670	727.683	1000.173	720	1977.755	1267.338	770	3229.613	1630.294
621	497.397	971.818	671	747.801	1003.167	721	2001.021	1273.069	771	3251.407	1636.149
622	470.942	969.121	672	777.454	1006.854	722	2026.319	1280.433	772	3274.706	1643.357
623	450.496	966.698	673	804.143	1011.369	723	2052.794	1287.490	773	3303.329	1649.475
624	425.642	964.633	674	832.193	1015.020	724	2073.482	1293.358	774	3327.898	1657.560
625	399.631	962.887	675	852.318	1018.689	725	2104.247	1301.024	775	3353.854	1664.552
626	376.026	960.981	676	877.902	1022.437	726	2127.948	1308.343	776	3376.264	1675.352
627	353.782	959.268	677	903.481	1027.936	727	2151.842	1314.503	777	3402.702	1680.203
628	324.691	957.854	678	930.585	1030.703	728	2176.867	1318.469	778	3420.895	1687.718
629	303.545	955.870	679	951.877	1035.000	729	2205.177	1329.099	779	3453.340	1698.745
630	275.979	954.239	680	981.685	1040.677	730	2223.370	1334.982	780	3477.933	1705.403
631	253.431	953.240	681	997.988	1045.077	731	2254.993	1342.631	781	3503.704	1711.605
632	224.502	952.059	682	1028.302	1048.441	732	2277.647	1350.118	782	3527.909	1720.754
633	202.690	950.595	683	1057.108	1054.518	733	2299.834	1357.171	783	3554.773	1729.231
634	177.711	949.141	684	1079.172	1058.712	734	2328.326	1364.622	784	3577.890	1735.458
635	157.906	948.403	685	1102.905	1063.161	735	2353.659	1371.613	785	3601.391	1744.448
636	126.487	948.019	686	1129.033	1067.551	736	2378.880	1379.627	786	3629.788	1751.149
637	108.628	947.600	687	1154.135	1072.604	737	2402.618	1386.764	787	3654.610	1760.526
638	89.868	947.095	688	1179.462	1077.918	738	2429.010	1393.956	788	3679.484	1768.197
639	62.742	946.545	689	1201.324	1083.181	739	2453.412	1400.834	789	3701.937	1775.120
640	50.086	945.980	690	1228.635	1088.640	740	2477.697	1407.589	790	3730.246	1782.591
641	46.358	946.538	691	1252.559	1092.830	741	2502.335	1415.158	791	3753.592	1790.948
642	52.469	946.447	692	1276.939	1098.534	742	2529.938	1422.226	792	3778.230	1798.312
643	69.671	946.954	693	1302.470	1104.879	743	2553.598	1429.520	793	3802.290	1804.984
644	86.893	947.101	694	1326.568	1109.972	744	2576.873	1436.827	794	3828.996	1813.300
645	112.734	947.711	695	1351.947	1115.153	745	2601.946	1443.173	795	3852.268	1823.626
646	133.464	947.722	696	1381.150	1121.642	746	2626.465	1450.736	796	3879.018	1828.743
647	156.651	949.129	697	1401.407	1126.247	747	2649.516	1458.285	797	3904.126	1835.432
648	182.453	949.660	698	1427.905	1132.330	748	2679.669	1465.704	798	3929.863	1845.600
649	207.535	950.746	699	1448.880	1136.977	749	2707.953	1474.176	799	3952.356	1852.445
650	230.490	952.851	700	1472.461	1142.246	750	2728.236	1480.744	800	3979.256	1857.067



**Table C.5: Traveltimes for Receiver 5.**

Receiver Depth = 2013.927 m											
Source N.o.	Source Offset (m)	Traveltime (ms)	Source N.o.	Source Offset (m)	Traveltime (ms)	Source N.o.	Source Offset (m)	Traveltime (ms)	Source N.o.	Source Offset (m)	Traveltime (ms)
801	991.550	1044.546	851	258.040	957.373	901	1504.896	1152.406	951	2757.260	1489.196
802	967.175	1039.433	852	284.557	958.386	902	1532.702	1159.518	952	2783.262	1497.292
803	943.576	1035.737	853	307.433	960.111	903	1558.966	1164.752	953	2810.670	1504.319
804	918.726	1031.620	854	332.872	961.630	904	1584.736	1170.728	954	2838.309	1512.353
805	893.046	1027.395	855	359.049	963.944	905	1608.206	1176.191	955	2859.972	1519.220
806	866.861	1023.883	856	385.343	965.418	906	1632.059	1182.031	956	2887.458	1526.834
807	841.491	1019.800	857	409.334	968.447	907	1658.491	1188.399	957	2911.043	1534.916
808	818.125	1015.300	858	433.705	969.921	908	1682.662	1193.896	958	2933.070	1540.726
809	793.125	1011.754	859	460.001	972.838	909	1709.332	1200.831	959	2956.504	1548.725
810	765.709	1008.324	860	482.029	974.457	910	1731.466	1206.627	960	2983.778	1555.046
811	742.569	1004.757	861	509.907	976.609	911	1758.713	1212.206	961	3006.069	1562.470
812	717.025	1001.513	862	532.777	979.967	912	1782.727	1218.930	962	3033.245	1570.417
813	692.777	998.272	863	558.748	981.933	913	1809.004	1224.991	963	3057.374	1578.054
814	671.179	995.647	864	583.493	985.107	914	1834.144	1232.119	964	3082.250	1585.655
815	640.407	991.688	865	611.554	988.531	915	1856.165	1237.956	965	3107.982	1593.522
816	619.158	988.858	866	634.129	991.086	916	1883.729	1244.659	966	3133.483	1600.080
817	593.758	986.490	867	658.248	994.422	917	1908.443	1250.987	967	3158.005	1608.654
818	568.106	982.274	868	684.072	997.434	918	1932.226	1257.720	968	3184.048	1615.445
819	544.979	980.074	869	705.124	1000.876	919	1956.508	1264.184	969	3207.868	1623.756
820	513.842	977.187	870	732.526	1004.018	920	1982.824	1270.513	970	3234.734	1630.595
821	491.551	974.652	871	752.696	1007.432	921	2006.097	1276.609	971	3256.536	1639.147
822	465.116	971.956	872	782.323	1011.254	922	2031.400	1283.866	972	3279.827	1646.444
823	444.635	970.103	873	809.041	1015.565	923	2057.867	1290.939	973	3308.451	1654.579
824	419.775	967.793	874	837.034	1019.073	924	2078.568	1296.333	974	3333.029	1662.212
825	393.803	966.024	875	857.170	1022.852	925	2109.336	1305.118	975	3358.978	1669.892
826	370.105	963.975	876	882.753	1026.294	926	2133.030	1311.261	976	3381.389	1674.585
827	347.762	962.375	877	908.363	1031.885	927	2156.926	1317.697	977	3407.830	1683.330
828	318.675	960.815	878	935.422	1034.363	928	2181.962	1322.426	978	3426.021	1689.103
829	297.136	959.260	879	956.725	1038.713	929	2210.257	1332.953	979	3458.467	1699.251
830	269.418	957.826	880	986.543	1044.700	930	2228.452	1338.401	980	3483.057	1707.174
831	246.599	956.764	881	1002.868	1049.014	931	2260.084	1346.712	981	3508.829	1714.270
832	217.658	955.323	882	1033.179	1052.495	932	2282.716	1353.271	982	3533.031	1721.476
833	195.765	953.803	883	1061.975	1058.421	933	2304.890	1359.676	983	3559.898	1730.402
834	170.528	952.296	884	1084.068	1062.677	934	2333.394	1367.060	984	3583.016	1738.836
835	150.322	951.830	885	1107.805	1066.960	935	2358.739	1375.573	985	3606.516	1744.451
836	119.158	951.246	886	1133.931	1071.377	936	2383.962	1382.318	986	3634.919	1752.517
837	100.035	951.140	887	1159.036	1076.518	937	2407.702	1389.120	987	3659.735	1760.693
838	80.477	950.595	888	1184.402	1081.816	938	2434.097	1396.500	988	3684.612	1767.779
839	52.512	950.060	889	1206.284	1087.232	939	2458.515	1403.233	989	3707.066	1774.926
840	39.174	949.748	890	1233.606	1092.486	940	2482.793	1410.509	990	3735.376	1785.556
841	37.125	949.931	891	1257.536	1096.881	941	2507.442	1418.106	991	3758.721	1792.247
842	47.917	949.852	892	1281.929	1102.535	942	2535.041	1425.056	992	3783.360	1799.150
843	67.679	950.437	893	1307.463	1108.661	943	2558.701	1432.211	993	3807.424	1805.479
844	87.531	950.647	894	1331.536	1113.833	944	2581.986	1439.055	994	3834.131	1814.840
845	114.917	951.544	895	1356.935	1119.047	945	2607.071	1445.480	995	3857.404	1823.009
846	136.226	951.374	896	1386.199	1125.490	946	2631.588	1452.599	996	3884.155	1829.612
847	159.548	953.025	897	1406.463	1130.003	947	2654.653	1459.835	997	3909.264	1837.849
848	185.804	953.865	898	1432.981	1136.112	948	2684.768	1469.199	998	3935.005	1845.303
849	210.975	954.950	899	1453.941	1141.041	949	2713.012	1477.709	999	3957.499	1852.544
850	234.325	956.605	900	1477.524	1145.902	950	2733.279	1482.503	1000	3984.399	1860.716

## **APPENDIX D**

### **Synthetic Data**



### Computations for ray parameter, $p$ , and traveltimes

The following equations were used for computations.

Original expression (1.2):

$$t = \frac{1}{b} \ln \left[ \frac{a+bz}{a} \frac{1+\sqrt{1-p^2 a^2 (1+2\chi)}}{1+\sqrt{1-p^2 (a+bz)^2 (1+2\chi)}} \right].$$

Reformulated expression (1.3):

$$t = \frac{1}{2b} \left[ \ln \frac{1-\sqrt{1-p^2 a^2 (1+2\chi)} + pbX}{1+\sqrt{1-p^2 a^2 (1+2\chi)} - pbX} - \ln \frac{1-\sqrt{1-p^2 a^2 (1+2\chi)}}{1+\sqrt{1-p^2 a^2 (1+2\chi)}} \right].$$

Expression (1.36) to obtain the ray parameter,  $p$ :

$$p = \frac{2X}{\sqrt{[X^2 + (1+2\chi)Z^2] [(2a+bZ)^2 (1+2\chi) + b^2 X^2]}}.$$

**Table D.1:** Ray parameter  $p$  and traveltimes for synthetic zero-offset data.  
 $a = 1350.1624$  m/s and  $b = 0.884$  /s.  $\chi = 0$ .

Depth $z$ (m)	Offset $x$ (m)	Ray parameter $p$	Traveltime using original expression (1.2) (ms)	Traveltime using reformulated expression (1.3) (ms)
1.000	1.000	0.000523548	1.047097	1.047097
100.000	1.000	0.000007171	71.744968	71.744968
200.000	1.000	0.000003476	139.204741	139.204741
300.000	1.000	0.000002248	202.867987	202.867987
400.000	1.000	0.000001637	263.138681	263.138681
500.000	1.000	0.000001273	320.360047	320.360047
600.000	1.000	0.000001032	374.825796	374.825796
700.000	1.000	0.000000861	426.789168	426.789168
800.000	1.000	0.000000734	476.470029	476.470029
900.000	1.000	0.000000636	524.060488	524.060488
1000.000	1.000	0.000000558	569.729374	569.729374
1100.000	1.000	0.000000495	613.625860	613.625860
1200.000	1.000	0.000000443	655.882392	655.882393
1300.000	1.000	0.000000400	696.617107	696.617107
1400.000	1.000	0.000000363	735.935816	735.935816
1500.000	1.000	0.000000331	773.933666	773.933667
1600.000	1.000	0.000000304	810.696526	810.696526
1700.000	1.000	0.000000280	846.302153	846.302153
1800.000	1.000	0.000000259	880.821184	880.821184
1900.000	1.000	0.000000240	914.317980	914.317981
2000.000	1.000	0.000000224	946.851349	946.851349
$a = 1350.1624$		$b = 0.8840$		

**Table D.2:** Ray parameter  $p$  and traveltime calculations for synthetic offset data.  
 $a = 1350.1624$  m/s and  $b = 0.884$  /s.  $\chi = 0$ .

Depth $z$ (m)	Offset $x$ (m)	Ray parameter $p$	Traveltime using original expression (1.2) (ms)	Traveltime using reformulated expression (1.3) (ms)	Depth $z$ (m)	Offset $x$ (m)	Ray parameter $p$	Traveltime using original expression (1.2) (ms)	Traveltime using reformulated expression (1.3) (ms)
1960.000	900.000	0.00018531	1022.030112	1022.030112	1990.000	900.000	0.00018194	1030.001859	1030.001859
1960.000	1000.000	0.00020108	1041.359390	1041.359390	1990.000	1000.000	0.00019753	1048.984602	1048.984602
1960.000	1100.000	0.00021568	1062.207268	1062.207268	1990.000	1100.000	0.00021198	1069.469698	1069.469698
1960.000	1200.000	0.00022911	1084.456357	1084.456357	1990.000	1200.000	0.00022531	1091.343548	1091.343548
1960.000	1300.000	0.00024140	1107.990997	1107.990997	1990.000	1300.000	0.00023752	1114.493960	1114.49396
1960.000	1400.000	0.00025258	1132.698629	1132.698629	1990.000	1400.000	0.00024866	1138.811491	1138.811491
1960.000	1500.000	0.00026270	1158.470841	1158.470841	1990.000	1500.000	0.00025876	1164.190474	1164.190474
1960.000	1600.000	0.00027181	1185.204118	1185.204118	1990.000	1600.000	0.00026787	1190.529791	1190.529791
1960.000	1700.000	0.00027996	1212.800355	1212.800355	1990.000	1700.000	0.00027605	1217.733385	1217.733385
1960.000	1800.000	0.00028723	1241.167151	1241.167151	1990.000	1800.000	0.00028335	1245.710592	1245.710592
1960.000	1900.000	0.00029365	1270.217937	1270.217937	1990.000	1900.000	0.00028983	1274.376288	1274.376288
1960.000	2000.000	0.00029930	1299.871972	1299.871972	1990.000	2000.000	0.00029554	1303.650921	1303.650921
1960.000	2100.000	0.00030423	1330.054235	1330.054235	1990.000	2100.000	0.00030054	1333.460430	1333.46043
1960.000	2200.000	0.00030849	1360.695243	1360.695243	1990.000	2200.000	0.00030487	1363.736096	1363.736096
1960.000	2300.000	0.00031213	1391.730826	1391.730826	1990.000	2300.000	0.00030860	1394.414338	1394.414338
1960.000	2400.000	0.00031520	1423.101855	1423.101855	1990.000	2400.000	0.00031176	1425.436472	1425.436472
1960.000	2500.000	0.00031776	1454.753962	1454.753962	1990.000	2500.000	0.00031440	1456.748447	1456.748447
1960.000	2600.000	0.00031983	1486.637246	1486.637246	1990.000	2600.000	0.00031657	1488.300577	1488.300577
1960.000	2700.000	0.00032147	1518.705980	1518.70598	1990.000	2700.000	0.00031830	1520.047259	1520.047259
1970.000	900.000	0.00018417	1024.690802	1024.690802	2000.000	900.000	0.00018083	1032.652174	1032.652174
1970.000	1000.000	0.00019989	1043.903554	1043.903554	2000.000	1000.000	0.00019636	1051.521414	1051.521414
1970.000	1100.000	0.00021444	1064.629493	1064.629493	2000.000	1100.000	0.00021077	1071.887587	1071.887587
1970.000	1200.000	0.00022783	1086.752508	1086.752508	2000.000	1200.000	0.00022406	1093.638326	1093.638326
1970.000	1300.000	0.00024009	1110.158108	1110.158108	2000.000	1300.000	0.00023625	1116.662574	1116.662574
1970.000	1400.000	0.00025126	1134.734782	1134.734782	2000.000	1400.000	0.00024737	1140.851907	1140.851907
1970.000	1500.000	0.00026137	1160.375038	1160.375038	2000.000	1500.000	0.00025746	1166.101562	1166.101562
1970.000	1600.000	0.00027049	1186.976165	1186.976165	2000.000	1600.000	0.00026657	1192.311208	1192.311208
1970.000	1700.000	0.00027865	1214.440743	1214.440743	2000.000	1700.000	0.00027476	1219.385471	1219.385471
1970.000	1800.000	0.00028593	1242.676950	1242.67695	2000.000	1800.000	0.00028207	1247.234260	1247.23426
1970.000	1900.000	0.00029237	1271.598699	1271.598699	2000.000	1900.000	0.00028857	1275.772936	1275.772936
1970.000	2000.000	0.00029804	1301.125644	1301.125644	2000.000	2000.000	0.00029430	1304.922344	1304.922344
1970.000	2100.000	0.00030299	1331.183081	1331.183081	2000.000	2100.000	0.00029932	1334.608748	1334.608748
1970.000	2200.000	0.00030728	1361.701782	1361.701782	2000.000	2200.000	0.00030368	1364.763686	1364.763686
1970.000	2300.000	0.00031095	1392.617768	1392.617768	2000.000	2300.000	0.00030743	1395.323781	1395.323781
1970.000	2400.000	0.00031405	1423.872057	1423.872057	2000.000	2400.000	0.00031062	1426.230499	1426.230499
1970.000	2500.000	0.00031663	1455.410384	1455.410384	2000.000	2500.000	0.00031329	1457.429904	1457.429904
1970.000	2600.000	0.00031874	1487.182916	1487.182916	2000.000	2600.000	0.00031549	1488.872383	1488.872383
1970.000	2700.000	0.00032041	1519.143966	1519.143966	2000.000	2700.000	0.00031725	1520.512383	1520.512383
1980.000	900.000	0.00018305	1027.348060	1027.34806	$a \quad 1350.1624 \quad b \quad 0.8840$				
1980.000	1000.000	0.00019870	1046.445303	1046.445303					
1980.000	1100.000	0.00021321	1067.050318	1067.050318					
1980.000	1200.000	0.00022656	1089.048257	1089.048257					
1980.000	1300.000	0.00023880	1112.325784	1112.325784					
1980.000	1400.000	0.00024995	1136.772426	1136.772426					
1980.000	1500.000	0.00026006	1162.281608	1162.281608					
1980.000	1600.000	0.00026917	1188.751416	1188.751416					
1980.000	1700.000	0.00027735	1216.085115	1216.085115					
1980.000	1800.000	0.00028464	1244.191459	1244.191459					
1980.000	1900.000	0.00029110	1272.984846	1272.984846					
1980.000	2000.000	0.00029679	1302.385324	1302.385324					
1980.000	2100.000	0.00030176	1332.318510	1332.31851					
1980.000	2200.000	0.00030607	1362.715430	1362.71543					
1980.000	2300.000	0.00030977	1393.512303	1393.512303					
1980.000	2400.000	0.00031290	1424.650294	1424.650294					
1980.000	2500.000	0.00031551	1456.075243	1456.075243					
1980.000	2600.000	0.00031765	1487.737391	1487.737391					
1980.000	2700.000	0.00031935	1519.591090	1519.59109					



**Table D.3:** Ray parameter  $p$  and traveltimes calculations for synthetic offset data.  
 $a = 2000 \text{ m/s}$ ,  $b = 0.88/\text{s}$ .  $\chi = 0$ .

Depth $z$ (m)	Offset $x$ (m)	Ray parameter $p$	Traveltimes using original expression (1.2) (ms)	Traveltimes using reformulated expression (1.3) (ms)	Depth $z$ (m)	Offset $x$ (m)	Ray parameter $p$	Traveltimes using original expression (1.2) (ms)	Traveltimes using reformulated expression (1.3) (ms)
1960.000	900.000	0.00014441	775.083667	775.083667	1990.000	900.000	0.00014196	781.863152	781.863152
1960.000	1000.000	0.00015693	790.157754	790.157754	1990.000	1000.000	0.00015435	796.685562	796.685562
1960.000	1100.000	0.00016859	806.440785	806.440785	1990.000	1100.000	0.00016590	812.704950	812.704950
1960.000	1200.000	0.00017939	823.846835	823.846835	1990.000	1200.000	0.00017662	829.838092	829.838092
1960.000	1300.000	0.00018936	842.291228	842.291228	1990.000	1300.000	0.00018654	848.002778	848.002778
1960.000	1400.000	0.00019851	861.691526	861.691526	1990.000	1400.000	0.00019566	867.118777	867.118777
1960.000	1500.000	0.00020689	881.968278	881.968278	1990.000	1500.000	0.00020402	887.108581	887.108581
1960.000	1600.000	0.00021453	903.045562	903.045562	1990.000	1600.000	0.00021165	907.897953	907.897953
1960.000	1700.000	0.00022147	924.851336	924.851336	1990.000	1700.000	0.00021860	929.416291	929.416291
1960.000	1800.000	0.00022775	947.317647	947.317647	1990.000	1800.000	0.00022490	951.596856	951.596856
1960.000	1900.000	0.00023341	970.380708	970.380708	1990.000	1900.000	0.00023060	974.376870	974.376870
1960.000	2000.000	0.00023850	993.980889	993.980889	1990.000	2000.000	0.00023572	997.697528	997.697528
1960.000	2100.000	0.00024305	1018.062624	1018.062624	1990.000	2100.000	0.00024032	1021.503931	1021.503931
1960.000	2200.000	0.00024710	1042.574277	1042.574277	1990.000	2200.000	0.00024442	1045.744972	1045.744972
1960.000	2300.000	0.00025070	1067.467971	1067.467971	1990.000	2300.000	0.00024807	1070.373181	1070.373181
1960.000	2400.000	0.00025386	1092.699386	1092.699386	1990.000	2400.000	0.00025129	1095.344549	1095.344549
1960.000	2500.000	0.00025664	1118.227556	1118.227556	1990.000	2500.000	0.00025412	1120.618331	1120.618331
1960.000	2600.000	0.00025905	1144.014656	1144.014656	1990.000	2600.000	0.00025659	1146.156854	1146.156854
1960.000	2700.000	0.00026112	1170.025787	1170.025787	1990.000	2700.000	0.00025873	1171.925314	1171.925314
1970.000	900.000	0.00014359	777.345779	777.345779	2000.000	900.000	0.00014116	784.118369	784.118369
1970.000	1000.000	0.00015606	792.335274	792.335274	2000.000	1000.000	0.00015350	798.858270	798.858270
1970.000	1100.000	0.00016769	808.529729	808.529729	2000.000	1100.000	0.00016502	814.791154	814.791154
1970.000	1200.000	0.00017846	825.844129	825.844129	2000.000	1200.000	0.00017572	831.834675	831.834675
1970.000	1300.000	0.00018841	844.194629	844.194629	2000.000	1300.000	0.00018561	849.907431	849.907431
1970.000	1400.000	0.00019756	863.499531	863.499531	2000.000	1400.000	0.00019471	868.929913	868.929913
1970.000	1500.000	0.00020593	883.680038	883.680038	2000.000	1500.000	0.00020307	888.825255	888.825255
1970.000	1600.000	0.00021357	904.660790	904.660790	2000.000	1600.000	0.00021070	909.519773	909.519773
1970.000	1700.000	0.00022051	926.370228	926.370228	2000.000	1700.000	0.00021766	930.943344	930.943344
1970.000	1800.000	0.00022680	948.740802	948.740802	2000.000	1800.000	0.00022397	953.029633	953.029633
1970.000	1900.000	0.00023247	971.709063	971.709063	2000.000	1900.000	0.00022967	975.716199	975.716199
1970.000	2000.000	0.00023757	995.215653	995.215653	2000.000	2000.000	0.00023481	998.944513	998.944513
1970.000	2100.000	0.00024214	1019.205227	1019.205227	2000.000	2100.000	0.00023942	1022.659905	1022.659905
1970.000	2200.000	0.00024621	1043.626326	1043.626326	2000.000	2200.000	0.00024354	1046.811444	1046.811444
1970.000	2300.000	0.00024982	1068.431203	1068.431203	2000.000	2300.000	0.00024720	1071.351802	1071.351802
1970.000	2400.000	0.00025300	1093.575642	1093.575642	2000.000	2400.000	0.00025044	1096.237075	1096.237075
1970.000	2500.000	0.00025580	1119.018748	1119.018748	2000.000	2500.000	0.00025329	1121.426599	1121.426599
1970.000	2600.000	0.00025823	1144.722744	1144.722744	2000.000	2600.000	0.00025578	1146.882753	1146.882753
1970.000	2700.000	0.00026032	1170.652763	1170.652763	2000.000	2700.000	0.00025793	1172.570769	1172.570769
1980.000	900.000	0.00014277	779.605615	779.605615	$a = 2000.0000 \quad b = 0.8800$				
1980.000	1000.000	0.00015520	794.511220	794.511220					
1980.000	1100.000	0.00016679	810.617796	810.617796					
1980.000	1200.000	0.00017754	827.841229	827.841229					
1980.000	1300.000	0.00018747	846.098495	846.098495					
1980.000	1400.000	0.00019660	865.308632	865.308632					
1980.000	1500.000	0.00020497	885.393491	885.393491					
1980.000	1600.000	0.00021261	906.278273	906.278273					
1980.000	1700.000	0.00021955	927.891900	927.891900					
1980.000	1800.000	0.00022585	950.167226	950.167226					
1980.000	1900.000	0.00023153	973.041138	973.041138					
1980.000	2000.000	0.00023664	996.454553	996.454553					
1980.000	2100.000	0.00024123	1020.352351	1020.352351					
1980.000	2200.000	0.00024531	1044.683245	1044.683245					
1980.000	2300.000	0.00024894	1069.399628	1069.399628					
1980.000	2400.000	0.00025215	1094.457384	1094.457384					
1980.000	2500.000	0.00025496	1119.815694	1119.815694					
1980.000	2600.000	0.00025741	1145.436831	1145.436831					
1980.000	2700.000	0.00025952	1171.285959	1171.285959					



**Table D.4:** Ray parameter  $p$  and traveltimes calculations for synthetic offset data. Introduction of insignificant  $\chi$ ,  $a = 2000$  m/s,  $b = 0.880$  /s and  $\chi = 0.0001$ .

Depth $z$ (m)	Offset $x$ (m)	Ray parameter $p$	Traveltime using original expression (1.2) (ms)	Traveltime using reformulated expression (1.3) (ms)	Depth $z$ (m)	Offset $x$ (m)	Ray parameter $p$	Traveltime using original expression (1.2) (ms)	Traveltime using reformulated expression (1.3) (ms)
1960.000	900.000	0.000144	775.070673	775.070673	1990.000	900.000	0.00014194	781.850378	781.850378
1960.000	1000.000	0.00015690	790.142064	790.142064	1990.000	1000.000	0.00015432	796.670130	796.670130
1960.000	1100.000	0.00016856	806.422244	806.422244	1990.000	1100.000	0.00016587	812.686704	812.686704
1960.000	1200.000	0.00017936	823.825312	823.825312	1990.000	1200.000	0.00017659	829.816901	829.816901
1960.000	1300.000	0.00018933	842.266616	842.266616	1990.000	1300.000	0.00018650	847.978533	847.978533
1960.000	1400.000	0.00019848	861.663739	861.663739	1990.000	1400.000	0.00019562	867.091390	867.091390
1960.000	1500.000	0.00020686	881.937250	881.937250	1990.000	1500.000	0.00020398	887.077984	887.077984
1960.000	1600.000	0.00021450	903.011243	903.011243	1990.000	1600.000	0.00021162	907.864095	907.864095
1960.000	1700.000	0.00022144	924.813692	924.813692	1990.000	1700.000	0.00021857	929.379136	929.379136
1960.000	1800.000	0.00022772	947.276659	947.276659	1990.000	1800.000	0.00022487	951.556381	951.556381
1960.000	1900.000	0.00023338	970.336368	970.336368	1990.000	1900.000	0.00023056	974.333064	974.333064
1960.000	2000.000	0.00023847	993.933197	993.933197	1990.000	2000.000	0.00023569	997.650391	997.650391
1960.000	2100.000	0.00024302	1018.011592	1018.011592	1990.000	2100.000	0.00024029	1021.453472	1021.453472
1960.000	2200.000	0.00024707	1042.519923	1042.519923	1990.000	2200.000	0.00024439	1045.691208	1045.691208
1960.000	2300.000	0.00025066	1067.410320	1067.410320	1990.000	2300.000	0.00024804	1070.316135	1070.316135
1960.000	2400.000	0.00025383	1092.638469	1092.638469	1990.000	2400.000	0.00025126	1095.284249	1095.284249
1960.000	2500.000	0.00025660	1118.163407	1118.163407	1990.000	2500.000	0.00025409	1120.554811	1120.554811
1960.000	2600.000	0.00025902	1143.947314	1143.947314	1990.000	2600.000	0.00025656	1146.090151	1146.090151
1960.000	2700.000	0.00026109	1169.955296	1169.955296	1990.000	2700.000	0.00025869	1171.855469	1171.855469
1970.000	900.000	0.00014356	777.332859	777.332859	2000.000	900.000	0.00014113	784.105667	784.105667
1970.000	1000.000	0.00015603	792.319671	792.319671	2000.000	1000.000	0.00015347	798.842923	798.842923
1970.000	1100.000	0.00016766	808.511287	808.511287	2000.000	1100.000	0.00016499	814.773005	814.773005
1970.000	1200.000	0.00017843	825.822718	825.822718	2000.000	1200.000	0.00017569	831.813593	831.813593
1970.000	1300.000	0.00018838	844.170140	844.170140	2000.000	1300.000	0.00018558	849.883307	849.883307
1970.000	1400.000	0.00019752	863.471879	863.471879	2000.000	1400.000	0.00019468	868.902658	868.902658
1970.000	1500.000	0.00020590	883.649154	883.649154	2000.000	1500.000	0.00020304	888.794800	888.794800
1970.000	1600.000	0.00021353	904.626625	904.626625	2000.000	1600.000	0.00021067	909.486066	909.486066
1970.000	1700.000	0.00022048	926.332748	926.332748	2000.000	1700.000	0.00021762	930.906349	930.906349
1970.000	1800.000	0.00022676	948.699986	948.699986	2000.000	1800.000	0.00022393	952.989326	952.989326
1970.000	1900.000	0.00023244	971.664901	971.664901	2000.000	1900.000	0.00022964	975.672569	975.672569
1970.000	2000.000	0.00023754	995.168147	995.168147	2000.000	2000.000	0.00023477	998.897560	998.897560
1970.000	2100.000	0.00024210	1019.154387	1019.154387	2000.000	2100.000	0.00023938	1022.609636	1022.609636
1970.000	2200.000	0.00024617	1043.572169	1043.572169	2000.000	2200.000	0.00024350	1046.757875	1046.757875
1970.000	2300.000	0.00024978	1068.373755	1068.373755	2000.000	2300.000	0.00024717	1071.294956	1071.294956
1970.000	2400.000	0.00025297	1093.514931	1093.514931	2000.000	2400.000	0.00025041	1096.176980	1096.176980
1970.000	2500.000	0.00025576	1118.954809	1118.954809	2000.000	2500.000	0.00025326	1121.363287	1121.363287
1970.000	2600.000	0.00025819	1144.655617	1144.655617	2000.000	2600.000	0.00025574	1146.816262	1146.816262
1970.000	2700.000	0.00026029	1170.582488	1170.582488	2000.000	2700.000	0.00025790	1172.501139	1172.501139
1980.000	900.000	0.00014274	779.592768	779.592768	$a = 2000.0000 \quad b = 0.8800 \quad \chi = 0.0001000$				
1980.000	1000.000	0.00015517	794.495703	794.495703					
1980.000	1100.000	0.00016676	810.599453	810.599453					
1980.000	1200.000	0.00017751	827.819928	827.819928					
1980.000	1300.000	0.00018744	846.074128	846.074128					
1980.000	1400.000	0.00019657	865.281113	865.281113					
1980.000	1500.000	0.00020494	885.362751	885.362751					
1980.000	1600.000	0.00021257	906.244262	906.244262					
1980.000	1700.000	0.00021952	927.854582	927.854582					
1980.000	1800.000	0.00022581	950.126580	950.126580					
1980.000	1900.000	0.00023150	972.997154	972.997154					
1980.000	2000.000	0.00023661	996.407233	996.407233					
1980.000	2100.000	0.00024119	1020.301702	1020.301702					
1980.000	2200.000	0.00024528	1044.629285	1044.629285					
1980.000	2300.000	0.00024891	1069.342381	1069.342381					
1980.000	2400.000	0.00025211	1094.396879	1094.396879					
1980.000	2500.000	0.00025493	1119.751965	1119.751965					
1980.000	2600.000	0.00025738	1145.369916	1145.369916					
1980.000	2700.000	0.00025949	1171.215899	1171.215899					



**Table D.5:** Ray parameter  $p$  and traveltime calculations for synthetic offset data. Introduction of significant  $\chi$ ,  $a = 2000$  m/s,  $b = 0.880$  /s and  $\chi = 0.2$ .

Depth $z$ (m)	Offset $x$ (m)	Ray parameter $p$	Traveltime using original expression (1.2) (ms)	Traveltime using reformulated expression (1.3) (ms)	Depth $z$ (m)	Offset $x$ (m)	Ray parameter $p$	Traveltime using original expression (1.2) (ms)	Traveltime using reformulated expression (1.3) (ms)
1960.000	900.000	0.00010610	756.254532	756.254532	1990.000	900.000	0.00010423	763.359293	763.359293
1960.000	1000.000	0.00011594	767.360570	767.360570	1990.000	1000.000	0.00011394	774.271966	774.271966
1960.000	1100.000	0.00012526	779.424862	779.424862	1990.000	1100.000	0.00012316	786.131092	786.131092
1960.000	1200.000	0.00013407	792.395934	792.395934	1990.000	1200.000	0.00013188	798.887008	798.887008
1960.000	1300.000	0.00014236	806.221805	806.221805	1990.000	1300.000	0.00014009	812.489461	812.489461
1960.000	1400.000	0.00015013	820.850604	820.850604	1990.000	1400.000	0.00014780	826.888205	826.888205
1960.000	1500.000	0.00015740	836.231098	836.231098	1990.000	1500.000	0.00015502	842.033509	842.033509
1960.000	1600.000	0.00016416	852.313124	852.313124	1990.000	1600.000	0.00016176	857.876581	857.876581
1960.000	1700.000	0.00017045	869.047939	869.047939	1990.000	1700.000	0.00016803	874.369915	874.369915
1960.000	1800.000	0.00017628	886.388485	886.388485	1990.000	1800.000	0.00017385	891.467555	891.467555
1960.000	1900.000	0.00018167	904.289583	904.289583	1990.000	1900.000	0.00017924	909.125297	909.125297
1960.000	2000.000	0.00018663	922.708070	922.708070	1990.000	2000.000	0.00018421	927.300826	927.300826
1960.000	2100.000	0.00019120	941.602871	941.602871	1990.000	2100.000	0.00018879	945.953803	945.953803
1960.000	2200.000	0.00019538	960.935042	960.935042	1990.000	2200.000	0.00019299	965.045911	965.045911
1960.000	2300.000	0.00019921	980.667764	980.667764	1990.000	2300.000	0.00019685	984.540865	984.540865
1960.000	2400.000	0.00020270	1000.766315	1000.766315	1990.000	2400.000	0.00020037	1004.404391	1004.404391
1960.000	2500.000	0.00020588	1021.198024	1021.198024	1990.000	2500.000	0.00020358	1024.604186	1024.604186
1960.000	2600.000	0.00020876	1041.932200	1041.932200	1990.000	2600.000	0.00020649	1045.109864	1045.109864
1960.000	2700.000	0.00021136	1062.940056	1062.940056	1990.000	2700.000	0.00020913	1065.892881	1065.892881
1970.000	900.000	0.00010547	758.626027	758.626027	2000.000	900.000	0.00010362	765.721041	765.721041
1970.000	1000.000	0.00011527	769.667033	769.667033	2000.000	1000.000	0.00011329	776.570400	776.570400
1970.000	1100.000	0.00012456	781.662348	781.662348	2000.000	1100.000	0.00012247	788.362300	788.362300
1970.000	1200.000	0.00013333	794.561110	794.561110	2000.000	1200.000	0.00013116	801.047667	801.047667
1970.000	1300.000	0.00014160	808.311922	808.311922	2000.000	1300.000	0.00013934	814.576810	814.576810
1970.000	1400.000	0.00014935	822.863460	822.863460	2000.000	1400.000	0.00014704	828.900013	828.900013
1970.000	1500.000	0.00015660	838.164995	838.164995	2000.000	1500.000	0.00015424	843.968033	843.968033
1970.000	1600.000	0.00016336	854.166828	854.166828	2000.000	1600.000	0.00016097	859.732530	859.732530
1970.000	1700.000	0.00016964	870.820630	870.820630	2000.000	1700.000	0.00016723	876.146404	876.146404
1970.000	1800.000	0.00017547	888.079711	888.079711	2000.000	1800.000	0.00017305	893.164061	893.164061
1970.000	1900.000	0.00018085	905.899221	905.899221	2000.000	1900.000	0.00017843	910.741621	910.741621
1970.000	2000.000	0.00018582	924.236278	924.236278	2000.000	2000.000	0.00018341	928.837048	928.837048
1970.000	2100.000	0.00019039	943.050053	943.050053	2000.000	2100.000	0.00018799	947.410249	947.410249
1970.000	2200.000	0.00019458	962.301812	962.301812	2000.000	2200.000	0.00019221	966.423117	966.423117
1970.000	2300.000	0.00019842	981.954911	981.954911	2000.000	2300.000	0.00019607	985.839546	985.839546
1970.000	2400.000	0.00020192	1001.974779	1001.974779	2000.000	2400.000	0.00019960	1005.625412	1005.625412
1970.000	2500.000	0.00020511	1022.328866	1022.328866	2000.000	2500.000	0.00020282	1025.748539	1025.748539
1970.000	2600.000	0.00020800	1042.986580	1042.986580	2000.000	2600.000	0.00020574	1046.178642	1046.178642
1970.000	2700.000	0.00021061	1063.919216	1063.919216	2000.000	2700.000	0.00020839	1066.887261	1066.887261
1980.000	900.000	0.00010485	760.994284	760.994284	$a = 2000.0000 \quad b = 0.8800 \quad \chi = 0.2000$				
1980.000	1000.000	0.00011460	771.970838	771.970838					
1980.000	1100.000	0.00012385	783.897766	783.897766					
1980.000	1200.000	0.00013260	796.724812	796.724812					
1980.000	1300.000	0.00014084	810.401153	810.401153					
1980.000	1400.000	0.00014857	824.876007	824.876007					
1980.000	1500.000	0.00015581	840.099148	840.099148					
1980.000	1600.000	0.00016256	856.021330	856.021330					
1980.000	1700.000	0.00016883	872.594639	872.594639					
1980.000	1800.000	0.00017466	889.772753	889.772753					
1980.000	1900.000	0.00018004	907.511145	907.511145					
1980.000	2000.000	0.00018501	925.767216	925.767216					
1980.000	2100.000	0.00018959	944.500384	944.500384					
1980.000	2200.000	0.00019379	963.672122	963.672122					
1980.000	2300.000	0.00019763	983.245966	983.245966					
1980.000	2400.000	0.00020114	1003.187492	1003.187492					
1980.000	2500.000	0.00020434	1023.464274	1023.464274					
1980.000	2600.000	0.00020724	1044.045823	1044.045823					
1980.000	2700.000	0.00020987	1064.903512	1064.903512					

## APPENDIX E

### Real Data: Offset

Isotropic Cases: Inverse results for  $a$ ,  $b$ , with  $\chi = 0$

Anisotropic Cases: Inverse results for  $a$ ,  $b$ , and  $\chi$



**Table E.1:**  $a$ ,  $b$ , and  $\chi = 0$ , with maximum offsets increasing from 47.9 m to 3984.4 m, for all receivers, includes the longside and shortside, (A+B+C). Best values (minimum standard error) are highlighted.

Max Offset (m)	# observations	$a$	Standard Error	$b$	Standard Error	Max Offset (m)	# observations	$a$	Standard Error	$b$	Standard Error
47.92	19	1665.84	28.778	0.4893	0.03398	2047.77	613	1077.89	2.268	1.2999	0.00349
99.57	33	1654.28	17.564	0.5028	0.02088	2073.48	619	1078.62	2.205	1.2988	0.00339
119.62	44	1661.06	14.674	0.4947	0.01739	2099.20	623	1078.92	2.160	1.2983	0.00331
142.49	54	1660.06	16.201	0.4960	0.01922	2122.91	628	1079.57	2.110	1.2973	0.00323
174.10	65	1652.94	16.406	0.5046	0.01952	2146.80	633	1080.44	2.063	1.2959	0.00315
195.77	75	1657.14	15.691	0.4996	0.01863	2171.82	638	1080.15	2.031	1.2964	0.00310
224.50	88	1664.87	14.822	0.4905	0.01754	2195.22	642	1080.41	1.988	1.2960	0.00303
247.11	98	1673.08	14.056	0.4808	0.01658	2223.37	649	1082.33	1.940	1.2930	0.00294
273.34	107	1674.49	13.396	0.4791	0.01579	2249.94	653	1083.07	1.912	1.2918	0.00290
299.43	119	1668.35	12.970	0.4865	0.01533	2272.62	658	1084.47	1.880	1.2896	0.00284
324.69	130	1666.61	12.936	0.4887	0.01530	2299.83	664	1086.39	1.854	1.2866	0.00279
347.76	138	1659.12	12.830	0.4976	0.01522	2323.30	668	1087.31	1.831	1.2832	0.00275
373.16	148	1656.23	13.542	0.5012	0.01608	2348.62	673	1088.85	1.808	1.2828	0.00271
399.63	159	1644.04	14.341	0.5159	0.01712	2373.84	678	1090.46	1.792	1.2803	0.00268
421.11	168	1643.13	14.971	0.5171	0.01787	2397.57	683	1092.23	1.780	1.2775	0.00265
447.16	178	1630.54	16.272	0.5323	0.01953	2423.96	688	1093.99	1.769	1.2748	0.00263
473.07	190	1615.42	17.577	0.5507	0.02124	2448.35	693	1095.44	1.753	1.2726	0.00260
497.40	199	1603.17	19.059	0.5658	0.02315	2472.64	698	1096.96	1.739	1.2702	0.00257
523.77	210	1579.93	19.828	0.5944	0.02433	2497.27	703	1098.65	1.730	1.2676	0.00255
549.68	219	1564.36	20.370	0.6137	0.02517	2524.87	708	1100.26	1.721	1.2652	0.00253
574.42	230	1520.57	21.733	0.6687	0.02740	2548.53	713	1101.87	1.708	1.2627	0.00250
599.45	239	1492.65	22.186	0.7043	0.02834	2571.80	718	1103.39	1.697	1.2604	0.00248
624.92	250	1450.70	21.976	0.7587	0.02865	2596.86	723	1104.92	1.688	1.2581	0.00246
648.93	260	1412.84	21.473	0.8087	0.02853	2621.38	728	1106.30	1.674	1.2559	0.00243
674.71	269	1381.41	20.977	0.8510	0.02832	2649.52	734	1108.45	1.672	1.2527	0.00242
698.48	280	1343.86	19.646	0.9024	0.02705	2674.60	738	1109.58	1.661	1.2510	0.00239
722.97	290	1312.83	18.671	0.9457	0.02615	2698.02	742	1110.99	1.660	1.2488	0.00239
748.24	301	1281.28	17.346	0.9905	0.02472	2723.23	748	1112.93	1.653	1.2459	0.00237
772.71	310	1255.69	16.593	1.0274	0.02399	2747.23	753	1118.02	1.285	1.2385	0.00182
799.36	320	1231.35	15.503	1.0630	0.02273	2773.23	758	1127.74	1.244	1.2245	0.00175
823.75	329	1209.00	14.746	1.0962	0.02191	2795.75	762	1135.23	1.247	1.2138	0.00174
847.58	340	1186.16	13.764	1.1305	0.02072	2823.37	767	1147.06	1.234	1.1971	0.00169
873.16	350	1172.17	12.920	1.1518	0.01961	2849.91	773	1160.98	1.226	1.1776	0.00165
898.70	360	1160.80	12.022	1.1692	0.01837	2872.44	777	1170.34	1.296	1.1646	0.00173
924.31	369	1149.69	11.491	1.1864	0.01767	2895.99	782	1182.57	1.399	1.1478	0.00184
949.15	380	1134.32	10.699	1.2103	0.01661	2922.93	788	1196.67	1.460	1.1286	0.00189
972.73	389	1124.84	10.120	1.2252	0.01580	2946.35	793	1207.64	1.509	1.1138	0.00193
997.99	401	1120.93	9.456	1.2314	0.01478	2973.59	798	1219.31	1.599	1.0982	0.00202
1023.52	408	1114.82	9.192	1.2410	0.01442	2995.88	803	1231.00	1.682	1.0827	0.00210
1047.73	412	1112.53	8.966	1.2446	0.01408	3023.06	808	1243.55	1.804	1.0663	0.00223
1074.36	418	1110.38	8.607	1.2480	0.01353	3047.19	813	1254.84	1.837	1.0516	0.00223
1098.09	423	1108.38	8.332	1.2512	0.01311	3072.06	818	1265.98	1.875	1.0372	0.00225
1124.22	428	1105.23	8.065	1.2562	0.01271	3097.79	823	1278.39	1.978	1.0214	0.00235
1149.32	433	1101.63	7.776	1.2620	0.01227	3123.28	828	1290.09	2.034	1.0066	0.00238
1174.60	438	1098.42	7.492	1.2671	0.01184	3147.80	833	1300.92	2.061	0.9930	0.00238
1196.44	443	1096.90	7.203	1.2695	0.01139	3173.84	838	1312.21	2.117	0.9790	0.00241
1223.74	448	1095.81	6.951	1.2713	0.01099	3197.66	843	1324.33	2.197	0.9641	0.00248
1247.66	453	1093.81	6.704	1.2744	0.01061	3224.52	848	1335.40	2.242	0.9506	0.00250
1272.02	458	1091.80	6.444	1.2777	0.01021	3246.31	853	1346.37	2.284	0.9373	0.00252
1297.55	463	1091.26	6.191	1.2785	0.00980	3274.71	859	1359.20	2.328	0.9219	0.00253
1321.67	468	1091.58	5.962	1.2780	0.00943	3298.23	863	1367.77	2.358	0.9117	0.00254
1347.03	473	1091.38	5.743	1.2783	0.00908	3322.80	868	1378.21	2.393	0.8993	0.00254
1371.34	477	1091.33	5.566	1.2784	0.00879	3348.76	873	1388.65	2.427	0.8870	0.00255
1396.42	483	1090.53	5.305	1.2797	0.00837	3371.17	878	1398.72	2.454	0.8753	0.00254
1422.89	488	1090.08	5.104	1.2804	0.00805	3397.60	883	1408.58	2.484	0.8639	0.00254
1448.88	494	1090.23	4.870	1.2802	0.00767	3420.89	889	1421.13	2.532	0.8496	0.00256
1472.46	499	1089.58	4.698	1.2812	0.00740	3448.24	893	1428.94	2.549	0.8407	0.00255
1499.88	504	1088.81	4.524	1.2825	0.00712	3472.84	898	1438.93	2.579	0.8294	0.00255
1522.75	508	1087.92	4.393	1.2839	0.00691	3498.61	903	1448.51	2.604	0.8187	0.00254
1548.93	513	1087.36	4.242	1.2848	0.00667	3522.81	908	1457.85	2.624	0.8083	0.00253
1574.73	518	1086.00	4.096	1.2870	0.00644	3549.68	913	1467.98	2.666	0.7971	0.00255
1598.23	523	1084.67	3.957	1.2891	0.00622	3572.79	918	1478.51	2.713	0.7857	0.00257
1622.07	528	1083.56	3.815	1.2908	0.00600	3596.29	923	1487.64	2.724	0.7757	0.00254
1648.49	533	1082.73	3.680	1.2922	0.00578	3624.68	928	1497.71	2.751	0.7649	0.00255
1672.68	538	1081.57	3.558	1.2940	0.00558	3649.51	933	1505.66	2.741	0.7563	0.00249
1699.36	543	1080.46	3.442	1.2958	0.00540	3674.38	938	1515.63	2.781	0.7457	0.00251
1721.48	548	1079.76	3.329	1.2969	0.00522	3696.83	943	1524.02	2.789	0.7368	0.00248
1748.69	553	1078.89	3.231	1.2983	0.00506	3720.14	947	1531.36	2.810	0.7291	0.00248
1772.72	558	1077.99	3.127	1.2997	0.00490	3748.49	953	1541.60	2.821	0.7184	0.00246
1799.00	563	1077.41	3.030	1.3007	0.00474	3773.13	958	1550.72	2.849	0.7091	0.00246
1824.08	568	1076.90	2.930	1.3015	0.00458	3797.18	963	1558.69	2.855	0.7008	0.00243
1846.13	573	1076.79	2.840	1.3017	0.00443	3823.89	968	1566.57	2.860	0.6927	0.00241
1873.68	578	1076.85	2.752	1.3016	0.00429	3847.16	973	1574.54	2.869	0.6846	0.00238
1898.39	583	1076.56	2.676	1.3020	0.00416	3873.90	978	1582.46	2.880	0.6766	0.00236
1922.13	588	1076.51	2.599	1.3021	0.00404	3899.01	983	1590.91	2.898	0.6682	0.00235
1946.43	593	1076.97	2.524	1.3014	0.00392	3924.74	988	1598.90	2.919	0.6603	0.00235
1972.73	598	1077.19	2.458	1.3010	0.00381	3947.24	993	1606.60	2.929	0.6526	0.00233
1995.99	603	1077.25	2.392	1.3009	0.00370	3974.14	998	1614.19	2.940	0.6451	0.00230
2021.28	608	1077.49	2.327	1.3006	0.00359	3984.40	1000	1617.24	2.941	0.6422	0.00230



**Table E.2:**  $a$ ,  $b$ , and  $\chi = 0$ , with maximum offsets increasing from 74.7 m to 3984.4 m, for all receivers, includes the longside only, (A+C). Best values (minimum standard error) are highlighted.

Max Offset (m)	# observations	$a$	Standard Error	$b$	Standard Error	Max Offset (m)	# observations	$a$	Standard Error	$b$	Standard Error
74.74	11	1669.12	34.30	0.4852	0.04044	2047.77	411	1075.73	2.80	1.3031	0.00425
93.23	18	1656.88	21.47	0.4996	0.02549	2073.48	417	1076.66	2.73	1.3016	0.00412
114.92	23	1657.78	18.51	0.4984	0.02197	2099.20	421	1077.07	2.67	1.3010	0.00403
136.23	28	1661.64	24.71	0.4941	0.02928	2122.91	426	1077.88	2.62	1.2997	0.00394
159.55	33	1665.29	22.33	0.4897	0.02642	2146.80	431	1078.95	2.56	1.2981	0.00384
185.80	38	1665.45	19.53	0.4895	0.02311	2171.82	436	1078.68	2.53	1.2985	0.00379
224.32	45	1663.34	17.56	0.4920	0.02080	2195.22	440	1079.02	2.47	1.2980	0.00370
247.11	50	1677.33	17.49	0.4754	0.02059	2223.37	447	1081.29	2.42	1.2944	0.00361
273.34	55	1683.35	17.58	0.4685	0.02064	2249.94	451	1082.19	2.39	1.2931	0.00356
299.43	61	1678.60	18.26	0.4742	0.02148	2272.62	456	1083.84	2.36	1.2905	0.00349
324.60	66	1678.72	18.45	0.4742	0.02170	2299.83	462	1086.09	2.33	1.2870	0.00344
346.83	70	1672.04	18.37	0.4821	0.02166	2323.30	466	1087.17	2.31	1.2854	0.00340
373.16	75	1673.06	18.57	0.4810	0.02189	2348.62	471	1088.96	2.28	1.2826	0.00335
396.72	80	1660.90	19.33	0.4956	0.02291	2373.84	476	1090.84	2.27	1.2798	0.00332
421.11	85	1667.03	19.50	0.4884	0.02304	2397.57	481	1092.89	2.26	1.2766	0.00330
447.16	90	1656.71	20.01	0.5007	0.02374	2423.96	486	1094.93	2.25	1.2735	0.00327
473.07	96	1652.81	20.83	0.5055	0.02476	2448.35	491	1096.60	2.24	1.2710	0.00324
497.01	100	1646.48	23.89	0.5132	0.02846	2472.64	496	1098.34	2.22	1.2684	0.00321
523.77	106	1615.77	26.62	0.5504	0.03215	2497.27	501	1100.29	2.22	1.2654	0.00319
549.68	111	1600.55	28.41	0.5690	0.03453	2524.87	506	1102.14	2.21	1.2627	0.00316
574.42	116	1565.41	31.08	0.6123	0.03838	2548.53	511	1103.97	2.19	1.2599	0.00313
598.16	120	1536.58	31.98	0.6484	0.04000	2571.80	516	1105.71	2.18	1.2573	0.00311
624.92	126	1485.85	32.61	0.7129	0.04178	2596.86	521	1107.44	2.17	1.2547	0.00308
648.93	131	1441.98	32.08	0.7699	0.04199	2621.38	526	1109.01	2.15	1.2524	0.00305
674.71	136	1399.09	31.27	0.8269	0.04183	2649.52	532	1111.45	2.15	1.2487	0.00303
695.53	141	1360.12	29.71	0.8798	0.04055	2674.60	536	1112.73	2.14	1.2468	0.00301
722.97	146	1327.84	28.23	0.9244	0.03920	2698.02	540	1114.33	2.14	1.2445	0.00300
747.80	152	1293.56	25.85	0.9727	0.03657	2723.23	546	1116.53	2.13	1.2412	0.00297
772.71	156	1269.15	25.01	1.0076	0.03587	2747.23	551	1120.28	1.78	1.2359	0.00246
799.36	161	1244.28	23.30	1.0437	0.03390	2773.23	556	1131.62	1.46	1.2200	0.00200
822.94	165	1225.74	22.36	1.0710	0.03288	2795.75	560	1139.47	1.58	1.2090	0.00214
847.58	171	1195.41	20.56	1.1162	0.03079	2823.37	565	1151.74	1.49	1.1921	0.00198
873.16	176	1177.33	19.37	1.1436	0.02931	2849.91	571	1166.78	1.49	1.1716	0.00195
898.70	181	1167.06	17.95	1.1593	0.02732	2872.44	575	1176.24	1.48	1.1588	0.00191
921.31	185	1159.14	17.38	1.1715	0.02656	2895.99	580	1189.43	1.65	1.1412	0.00211
947.13	191	1139.34	16.03	1.2021	0.02480	2922.93	586	1203.85	1.68	1.1221	0.00211
972.35	195	1132.73	15.22	1.2124	0.02364	2946.35	591	1215.97	1.77	1.1062	0.00220
997.99	202	1132.68	13.91	1.2125	0.02158	2973.59	596	1227.63	1.80	1.0911	0.00221
1023.52	206	1126.05	13.52	1.2229	0.02105	2995.88	601	1239.83	1.88	1.0754	0.00227
1047.73	210	1119.83	12.90	1.2327	0.02015	3023.06	606	1252.96	2.01	1.0587	0.00241
1074.36	216	1114.06	12.00	1.2418	0.01880	3047.19	611	1264.67	2.03	1.0438	0.00239
1098.09	221	1109.63	11.39	1.2488	0.01787	3072.06	616	1277.53	2.15	1.0278	0.00251
1124.22	226	1104.01	10.85	1.2578	0.01707	3097.79	621	1289.93	2.21	1.0124	0.00254
1149.32	231	1098.30	10.29	1.2669	0.01624	3123.28	626	1300.92	2.22	0.9989	0.00251
1174.60	236	1093.65	9.78	1.2743	0.01547	3147.80	631	1313.43	2.32	0.9837	0.00260
1196.44	241	1091.66	9.28	1.2775	0.01468	3173.84	636	1325.32	2.36	0.9693	0.00262
1223.74	246	1090.39	8.88	1.2795	0.01404	3197.66	641	1336.96	2.41	0.9554	0.00263
1247.66	251	1088.03	8.50	1.2833	0.01345	3224.52	646	1349.01	2.49	0.9411	0.00270
1272.02	256	1085.76	8.11	1.2870	0.01283	3246.31	651	1359.47	2.49	0.9287	0.00265
1297.55	261	1085.42	7.73	1.2875	0.01223	3274.71	657	1372.56	2.52	0.9135	0.00265
1321.67	266	1086.14	7.41	1.2864	0.01170	3298.23	661	1381.30	2.55	0.9033	0.00265
1347.03	271	1086.20	7.12	1.2863	0.01121	3322.80	666	1392.80	2.61	0.8902	0.00269
1371.34	275	1086.36	6.88	1.2860	0.01082	3348.76	671	1403.42	2.64	0.8781	0.00268
1396.42	281	1085.73	6.53	1.2871	0.01026	3371.17	676	1414.40	2.69	0.8657	0.00272
1422.89	286	1085.46	6.26	1.2875	0.00983	3397.60	681	1425.44	2.75	0.8534	0.00274
1448.88	292	1085.93	5.96	1.2867	0.00934	3420.89	687	1436.58	2.73	0.8409	0.00267
1474.46	297	1085.42	5.74	1.2876	0.00899	3448.24	691	1444.45	2.74	0.8322	0.00266
1499.88	302	1084.74	5.52	1.2886	0.00864	3472.84	696	1454.49	2.77	0.8211	0.00265
1522.75	306	1083.89	5.36	1.2900	0.00838	3498.61	701	1465.13	2.82	0.8096	0.00267
1548.93	311	1083.45	5.18	1.2907	0.00809	3522.81	706	1475.38	2.86	0.7985	0.00269
1574.73	316	1082.11	5.00	1.2929	0.00781	3549.68	711	1484.98	2.87	0.7882	0.00266
1598.23	321	1080.79	4.84	1.2950	0.00754	3572.79	716	1496.68	2.94	0.7758	0.00272
1622.07	326	1079.72	4.66	1.2967	0.00726	3596.29	721	1506.06	2.94	0.7659	0.00268
1648.49	331	1078.96	4.49	1.2979	0.00699	3624.68	726	1514.26	2.92	0.7571	0.00261
1672.68	336	1077.84	4.35	1.2997	0.00676	3649.51	731	1523.12	2.92	0.7479	0.00258
1699.36	341	1076.75	4.21	1.3014	0.00654	3674.38	736	1533.05	2.96	0.7376	0.00260
1721.48	346	1076.14	4.07	1.3024	0.00632	3696.83	741	1542.49	2.99	0.7279	0.00259
1748.69	351	1075.32	3.96	1.3037	0.00613	3720.14	745	1549.94	3.00	0.7203	0.00259
1772.72	356	1074.47	3.83	1.3050	0.00593	3748.49	751	1560.21	3.01	0.7099	0.00256
1799.00	361	1073.97	3.71	1.3058	0.00574	3773.13	756	1569.07	3.03	0.7010	0.00256
1824.08	366	1073.54	3.59	1.3065	0.00554	3797.18	761	1577.30	3.03	0.6927	0.00252
1846.13	371	1073.56	3.48	1.3065	0.00536	3823.89	766	1584.51	3.01	0.6854	0.00246
1873.68	376	1073.77	3.38	1.3062	0.00519	3847.16	771	1592.52	3.02	0.6774	0.00243
1898.39	381	1073.58	3.29	1.3065	0.00504	3873.90	776	1601.40	3.04	0.6687	0.00243
1922.13	386	1073.63	3.19	1.3064	0.00489	3899.01	781	1609.44	3.06	0.6609	0.00242
1946.43	391	1074.28	3.10	1.3053	0.00474	3924.74	786	1617.03	3.06	0.6534	0.00239
1972.73	396	1074.65	3.03	1.3048	0.00462	3947.24	791	1625.59	3.08	0.6452	0.00239
1995.99	401	1074.81	2.95	1.3045	0.00449	3974.14	796	1634.08	3.10	0.6371	0.00239
2021.28	406	1075.18	2.87	1.3039	0.00436	3984.40	798	1636.32	3.09	0.6349	0.00235



**Table E.3:**  $a$ ,  $b$ , and  $\chi = 0$ , with maximum offsets increasing from 2850.0 m to 3984.4 m, for all receivers, for the longside, longoffsets only, (D+C). Best values (minimum standard error) are highlighted.

Max Offset (m)	# observations	$a$	Standard Error	$b$	Standard Error	Max Offset (m)	# observations	$a$	Standard Error	$b$	Standard Error
2849.91	11	1790.44	89.51	0.5086	0.09086	3448.24	131	1536.78	1.69	0.7788	0.00159
2872.44	15	1777.71	101.54	0.5222	0.10307	3472.84	136	1550.00	1.78	0.7659	0.00167
2895.99	20	1687.96	94.53	0.6142	0.09660	3498.61	141	1559.14	1.81	0.7570	0.00169
2922.93	26	1553.33	89.97	0.7536	0.09336	3522.81	146	1566.85	1.65	0.7496	0.00152
2946.35	31	1513.93	70.44	0.7948	0.07346	3549.68	151	1577.74	1.74	0.7391	0.00159
2973.59	36	1459.79	62.29	0.8518	0.06550	3572.79	156	1594.29	2.09	0.7233	0.00194
2995.88	41	1406.24	52.53	0.9087	0.05576	3596.29	161	1599.48	1.84	0.7183	0.00167
3023.06	46	1313.09	1.57	1.0085	0.00159	3624.68	166	1606.46	1.75	0.7117	0.00155
3047.19	51	1327.52	1.49	0.9930	0.00151	3649.51	171	1614.91	1.67	0.7037	0.00145
3072.06	56	1343.78	1.51	0.9756	0.00152	3674.38	176	1634.06	2.37	0.6857	0.00217
3097.79	61	1359.43	1.42	0.9589	0.00143	3696.83	181	1638.14	2.09	0.6820	0.00188
3123.28	66	1371.35	1.16	0.9463	0.00113	3720.14	185	1641.02	1.83	0.6792	0.00158
3147.80	71	1388.00	1.45	0.9290	0.00145	3748.49	191	1651.06	1.76	0.6699	0.00149
3173.84	76	1402.36	1.43	0.9140	0.00142	3773.13	196	1659.66	1.77	0.6619	0.00147
3197.66	81	1416.23	1.44	0.8997	0.00143	3797.18	201	1669.88	1.88	0.6527	0.00158
3224.52	86	1428.04	1.21	0.8875	0.00117	3823.89	206	1677.67	1.83	0.6455	0.00151
3246.31	91	1441.49	1.49	0.8738	0.00147	3847.16	211	1687.06	1.98	0.6370	0.00165
3274.71	97	1452.49	1.26	0.8626	0.00121	3873.90	216	1697.45	2.14	0.6276	0.00182
3298.23	101	1467.25	1.32	0.8476	0.00126	3899.01	221	1702.45	1.86	0.6231	0.00149
3322.80	106	1478.55	1.34	0.8363	0.00128	3924.74	226	1709.20	1.82	0.6170	0.00144
3348.76	111	1049.65	94.57	1.0755	0.04128	3947.24	231	1717.60	1.91	0.6094	0.00150
3371.17	116	1501.08	1.46	0.8138	0.00138	3974.14	236	1731.45	2.34	0.5972	0.00197
3397.60	121	1513.67	1.54	0.8014	0.00146	3984.40	238	1728.73	1.95	0.5996	0.00153
3420.89	127	1520.91	1.31	0.7944	0.00119						

**Table E.4:**  $a$ ,  $b$ , and  $\chi = 0$ , with maximum offsets increasing from 73.2 m to 1014.1 m, for all receivers, for the shortside only, (B). Best values (minimum standard error) are highlighted.

Max Offset (m)	# observations	$a$	Standard Error	$b$	Standard Error	Max Offset (m)	# observations	$a$	Standard Error	$b$	Standard Error
73.17	8	1658.04	50.06	0.4988	0.0593	573.81	114	1479.34	29.54	0.7216	0.0380
99.57	15	1648.20	28.86	0.5102	0.0344	599.45	119	1453.93	30.04	0.7546	0.0391
119.62	21	1663.77	21.90	0.4917	0.0259	624.84	124	1420.28	29.17	0.7990	0.0386
142.49	26	1657.95	21.68	0.4986	0.0257	646.13	129	1387.88	28.40	0.8425	0.0382
174.10	32	1639.47	23.28	0.5208	0.0279	671.18	133	1364.94	27.87	0.8737	0.0380
195.77	37	1647.54	23.06	0.5114	0.0275	698.48	139	1330.05	25.75	0.9219	0.0357
224.50	43	1668.16	22.51	0.4869	0.0266	722.70	144	1299.97	24.47	0.9641	0.0345
246.71	48	1668.35	20.45	0.4867	0.0242	748.24	149	1269.59	23.07	1.0076	0.0331
269.42	52	1665.95	19.24	0.4895	0.0228	771.35	154	1243.91	21.83	1.0449	0.0318
297.14	58	1657.90	17.81	0.4991	0.0211	798.75	159	1219.84	20.45	1.0803	0.0302
324.69	64	1654.99	17.59	0.5027	0.0209	823.75	164	1194.71	19.26	1.1179	0.0289
347.76	68	1646.31	17.44	0.5130	0.0208	847.08	169	1177.73	18.27	1.1437	0.0277
373.06	73	1639.49	19.12	0.5214	0.0229	872.46	174	1167.54	17.08	1.1592	0.0260
399.63	79	1627.97	20.52	0.5354	0.0247	898.67	179	1155.05	15.96	1.1785	0.0245
419.78	83	1619.08	21.86	0.5462	0.0264	924.31	184	1141.38	15.04	1.1997	0.0233
444.64	88	1603.83	24.68	0.5649	0.0300	949.15	189	1129.69	14.15	1.2179	0.0220
470.94	94	1577.65	26.90	0.5972	0.0331	972.73	194	1117.82	13.32	1.2366	0.0209
497.40	99	1560.18	28.18	0.6189	0.0349	997.09	199	1109.12	12.66	1.2504	0.0200
519.69	104	1545.04	28.38	0.6379	0.0354	1014.08	202	1102.85	12.28	1.2604	0.0194
544.98	108	1528.55	28.40	0.6587	0.0357						

**Table E.5:**  $a$ ,  $b$ , and  $\chi = 0$ , with maximum offsets increasing from 74.7 m to 1014.4 m, for all receivers, for the longside, shortoffsets only (B'). This is the same as Table E.2 up to the offset of 998.0 m, and is included here for comparison with results for the shortside only (B), Table E.4. Best values (minimum standard error) are highlighted.

Max Offset (m)	# observations	$a$	Standard Error	$b$	Standard Error	Max Offset (m)	# observations	$a$	Standard Error	$b$	Standard Error
74.74	11	1669.12	34.30	0.4852	0.04044	574.42	116	1565.41	31.08	0.6123	0.03838
93.23	18	1656.88	21.47	0.4996	0.02549	598.16	120	1536.58	31.98	0.6484	0.04000
114.92	23	1657.78	18.51	0.4984	0.02197	624.92	126	1485.85	32.61	0.7129	0.04178
136.23	28	1661.64	24.71	0.4941	0.02928	648.93	131	1441.98	32.08	0.7699	0.04199
159.55	33	1665.29	22.33	0.4897	0.02642	674.71	136	1399.09	31.27	0.8269	0.04183
185.80	38	1665.45	19.53	0.4895	0.02311	695.53	141	1360.12	29.71	0.8798	0.04055
224.32	45	1663.34	17.56	0.4920	0.02080	722.97	146	1327.84	28.23	0.9244	0.03920
247.11	50	1677.33	17.49	0.4754	0.02059	747.80	152	1293.56	25.85	0.9727	0.03657
273.34	55	1683.35	17.58	0.4685	0.02064	772.71	156	1269.15	25.01	1.0076	0.03587
299.43	61	1678.60	18.26	0.4742	0.02148	799.36	161	1244.28	23.30	1.0437	0.03390
324.60	66	1678.72	18.45	0.4742	0.02170	822.94	165	1225.74	22.36	1.0710	0.03288
346.83	70	1672.04	18.37	0.4821	0.02166	847.58	171	1195.41	20.56	1.1162	0.03079
373.16	75	1673.06	18.57	0.4810	0.02189	873.16	176	1177.33	19.37	1.1436	0.02931
396.72	80	1660.90	19.33	0.4956	0.02291	898.70	181	1167.06	17.95	1.1593	0.02732
421.11	85	1667.03	19.50	0.4884	0.02304	921.31	185	1159.14	17.38	1.1715	0.02656
447.16	90	1656.71	20.01	0.5007	0.02374	947.13	191	1139.34	16.03	1.2021	0.02480
473.07	96	1652.81	20.83	0.5055	0.02476	972.35	195	1132.73	15.22	1.2124	0.02364
497.01	100	1646.48	23.89	0.5132	0.02846	997.99	202	1132.68	13.91	1.2125	0.02158
523.77	106	1615.77	26.62	0.5504	0.03215	1014.40	203	1127.83	13.92	1.2201	0.02165
549.68	111	1600.55	28.41	0.5690	0.03453						



**Table E.6:**  $a$ ,  $b$ , and  $\chi$ , with maximum offsets increasing from 47.9 m to 3984.4 m, for all receivers, includes longside and shortside, (A+B+C). Best values (minimum standard error) are highlighted. Ambiguous values are obtained when rays are close to vertical resulting in large standard errors.

Max Offset (m)	# observations	$a$	Standard Error	$b$	Standard Error	$\chi$	Standard Error	Max Offset (m)	# observations	$a$	Standard Error	$b$	Standard Error	$\chi$	Standard Error
47.92	19	2000.11	70904.71	0.9503	90.02314	0.0002	378.202456	2047.77	613	1283.48	13.05	0.9816	0.01886	0.0427	0.002341
99.57	33	2000.34	35984.99	0.9507	45.88702	0.0002	130.112478	2073.48	619	1272.68	12.54	0.9972	0.01824	0.0411	0.002312
119.62	44	2000.60	26729.16	0.9512	34.22440	0.0002	59.835778	2099.20	623	1265.29	12.22	1.0079	0.01787	0.0400	0.002295
142.49	54	1654.92	16.52	0.5019	0.01960	0.0542	0.043993	2122.91	628	1257.97	11.81	1.0186	0.01735	0.0388	0.002263
174.10	65	1649.98	15.96	0.5077	0.01899	0.0611	0.030271	2146.80	633	1253.04	11.40	1.0258	0.01680	0.0381	0.002222
195.77	75	1655.24	14.86	0.5014	0.01765	0.0584	0.021008	2171.82	638	1239.81	11.18	1.0453	0.01662	0.0359	0.002241
224.50	88	1663.64	14.54	0.4917	0.01721	0.0269	0.013325	2195.22	642	1232.45	10.84	1.0562	0.01619	0.0346	0.002211
247.11	98	1672.45	14.11	0.4814	0.01664	0.0074	0.009835	2223.37	649	1233.20	10.33	1.0551	0.01543	0.0348	0.002135
273.34	107	1674.41	13.28	0.4790	0.01565	0.0131	0.007920	2249.94	653	1231.66	10.08	1.0574	0.01508	0.0345	0.002105
299.43	119	1668.50	12.36	0.4859	0.01460	0.0211	0.006144	2272.62	658	1232.47	9.74	1.0562	0.01456	0.0347	0.002051
324.69	130	1669.43	11.63	0.4848	0.01374	0.0264	0.004963	2299.83	664	1235.55	9.38	1.0516	0.01401	0.0353	0.001992
347.76	138	1663.08	11.21	0.4923	0.01328	0.0267	0.004278	2323.30	668	1235.13	9.15	1.0522	0.01367	0.0353	0.001959
373.16	148	1664.17	10.85	0.4909	0.01284	0.0314	0.003664	2348.62	673	1237.04	8.86	1.0493	0.01323	0.0356	0.001912
399.63	159	1659.58	10.45	0.4963	0.01239	0.0347	0.003113	2373.84	678	1239.60	8.60	1.0455	0.01283	0.0361	0.001869
421.11	168	1662.39	10.56	0.4929	0.01251	0.0348	0.002840	2397.57	683	1243.16	8.36	1.0402	0.01245	0.0368	0.001826
447.16	178	1659.40	10.63	0.4964	0.01261	0.0377	0.002590	2423.96	688	1246.48	8.13	1.0353	0.01208	0.0375	0.001785
473.07	190	1659.63	10.77	0.4961	0.01278	0.0396	0.002343	2448.35	693	1247.45	7.90	1.0339	0.01173	0.0377	0.001749
497.40	199	1662.55	10.70	0.4926	0.01268	0.0430	0.002176	2472.64	698	1248.87	7.67	1.0318	0.01139	0.0380	0.001713
523.77	210	1659.68	10.33	0.4959	0.01225	0.0439	0.001911	2497.27	703	1251.45	7.45	1.0280	0.01105	0.0385	0.001675
549.68	219	1660.25	10.12	0.4953	0.01201	0.0441	0.001741	2524.87	708	1253.42	7.25	1.0250	0.01075	0.0389	0.001642
574.42	230	1657.13	10.15	0.4989	0.01206	0.0474	0.001623	2548.53	713	1254.98	7.02	1.0228	0.01041	0.0392	0.001603
599.45	239	1659.65	9.93	0.4958	0.01178	0.0487	0.001495	2571.80	718	1256.19	6.82	1.0210	0.01010	0.0395	0.001571
624.92	250	1658.37	9.60	0.4973	0.01140	0.0491	0.001342	2596.86	723	1257.42	6.64	1.0191	0.00983	0.0397	0.001541
648.93	260	1657.74	9.33	0.4980	0.01108	0.0497	0.001238	2621.38	728	1257.59	6.44	1.0189	0.00954	0.0398	0.001510
674.71	269	1659.15	9.08	0.4963	0.01077	0.0502	0.001134	2649.52	734	1260.98	6.23	1.0139	0.00921	0.0405	0.001471
698.48	280	1656.91	8.78	0.4990	0.01043	0.0504	0.001036	2674.60	738	1261.32	6.08	1.0134	0.00899	0.0406	0.001447
722.97	290	1657.65	8.62	0.4981	0.01023	0.0511	0.000969	2698.02	742	1263.31	5.95	1.0105	0.00879	0.0410	0.001422
748.24	301	1654.65	8.54	0.5016	0.01016	0.0518	0.000919	2723.23	748	1265.03	5.74	1.0079	0.00848	0.0413	0.001387
772.71	310	1655.71	8.58	0.5003	0.01019	0.0530	0.000889	2747.23	753	1266.67	5.58	1.0055	0.00823	0.0417	0.001358
799.36	320	1652.54	8.62	0.5040	0.01026	0.0538	0.000862	2773.23	758	1268.30	5.42	1.0031	0.00799	0.0420	0.001329
823.75	329	1652.54	8.96	0.5039	0.01066	0.0553	0.000871	2795.75	762	1268.82	5.30	1.0024	0.00782	0.0421	0.001309
847.58	340	1652.33	9.12	0.5040	0.01086	0.0569	0.000857	2821.37	767	1268.49	5.13	1.0029	0.00758	0.0421	0.001281
873.16	350	1652.52	9.05	0.5038	0.01077	0.0577	0.000827	2849.91	773	1268.21	4.93	1.0033	0.00729	0.0420	0.001246
898.70	360	1647.50	9.07	0.5097	0.01082	0.0580	0.000811	2872.44	777	1268.22	4.82	1.0032	0.00712	0.0420	0.001227
924.31	369	1650.00	9.39	0.5066	0.01119	0.0592	0.000821	2895.99	782	1268.88	4.68	1.0023	0.00692	0.0422	0.001203
949.15	380	1645.42	9.75	0.5120	0.01164	0.0604	0.000837	2922.93	788	1269.19	4.53	1.0018	0.00670	0.0423	0.001178
972.73	389	1641.78	9.94	0.5162	0.01189	0.0612	0.000844	2946.35	793	1270.92	4.41	0.9993	0.00652	0.0426	0.001156
997.99	401	1641.48	10.20	0.5166	0.01220	0.0615	0.000850	2973.59	798	1272.00	4.31	0.9977	0.00637	0.0429	0.001138
1023.52	408	1645.83	10.25	0.5113	0.01224	0.0622	0.000834	2995.88	803	1272.66	4.19	0.9967	0.00620	0.0430	0.001117
1047.73	412	1644.92	10.21	0.5124	0.01219	0.0624	0.000827	3023.06	808	1273.83	4.09	0.9950	0.00604	0.0433	0.001098
1074.36	418	1644.74	10.10	0.5126	0.01207	0.0627	0.000811	3047.19	813	1274.36	3.98	0.9942	0.00588	0.0434	0.001079
1098.09	423	1645.29	10.05	0.5119	0.01200	0.0631	0.000801	3072.06	818	1276.09	3.89	0.9917	0.00575	0.0438	0.001063
1124.22	428	1645.66	10.15	0.5114	0.01212	0.0637	0.000804	3097.79	823	1277.51	3.79	0.9896	0.00560	0.0441	0.001045
1149.32	433	1644.04	10.30	0.5133	0.01231	0.0643	0.000814	3123.28	828	1269.78	0.77	1.0011	0.00106	0.0420	0.000285
1174.60	438	1642.56	10.45	0.5149	0.01249	0.0648	0.000823	3147.80	833	1280.27	1.00	0.9856	0.00142	0.0448	0.000334
1196.44	443	1640.81	10.43	0.5170	0.01248	0.0651	0.000820	3173.84	838	1288.56	0.99	0.9733	0.00139	0.0470	0.000331
1223.74	448	1641.49	10.44	0.5161	0.01249	0.0656	0.000817	3197.66	843	1297.17	0.98	0.9607	0.00137	0.0494	0.000330
1247.66	453	1641.17	10.59	0.5164	0.01266	0.0662	0.000827	3224.52	848	1304.49	0.74	0.9500	0.00099	0.0513	0.000280
1272.02	458	1638.87	10.73	0.5191	0.01285	0.0667	0.000840	3246.31	853	1312.26	0.74	0.9386	0.00099	0.0535	0.000282
1297.55	463	1637.06	10.72	0.5212	0.01284	0.0670	0.000840	3274.71	859	1319.62	0.74	0.9280	0.00099	0.0554	0.000285
1321.67	468	1636.69	10.66	0.5216	0.01277	0.0672	0.000835	3298.23	863	1329.36	0.76	0.9139	0.00100	0.0581	0.000291
1347.03	473	1635.93	10.68	0.5225	0.01280	0.0676	0.000838	3322.80	868	1336.06	0.76	0.9042	0.00100	0.0599	0.000292
1371.34	477	1633.93	10.67	0.5248	0.01281	0.0678	0.000841	3348.76	873	1344.52	0.78	0.8921	0.00102	0.0622	0.000303
1396.42	483	1630.53	10.84	0.5288	0.01303	0.0683	0.000861	3371.17	878	1350.16	0.68	0.8840	0.00085	0.0638	0.000288
1422.89	488	1627.44	10.96	0.5325	0.01320	0.0686	0.000878	3397.60	883	1358.17	0.70	0.8726	0.00087	0.0661	0.000297
1448.88	494	1622.23	11.09	0.5387	0.01339	0.0689	0.000902	3420.89	889	1363.78	0.71	0.8646	0.00088	0.0677	0.000303
1472.46	499	1618.51	11.32	0.5431	0.01369	0.0692	0.000931	3448.24	893	1372.95	0.73	0.8516	0.00090	0.0703	0.000315
1499.88	504	1612.97	11.60	0.5497	0.01405	0.0695	0.000968	3472.84	898	1382.46	0.87	0.8382	0.00111	0.0729	0.000349
1522.75	508	1609.42	11.83	0.5539	0.01436	0.0697	0.000997	3498.61	903	1387.62	0.77	0.8309	0.00093	0.0743	0.000336
1548.93	513	1603.99	12.15	0.5604	0.01479	0.0700	0.001041	3522.81	908	1393.35	0.78	0.8229	0.00095	0.0760	0.000343
1574.73	518	1595.32	12.71	0.5708	0.01554	0.0702	0.001116	3549.68	913	1400.72	0.80	0.8125	0.00097	0.0781	0.000355
1598.23	523	1585.25	13.28	0.5830	0.01630	0.0702	0.001197	3572.79	918	1411.21	0.97	0.7979	0.00121	0.0811	0.000398
1622.07	528	1573.20	13.73	0.5977	0.01696	0.0700	0.001277	3596.29	923	1413.46	0.85	0.7949	0.00101	0.0816	0.000379
1648.49	533	1560.64	14.11	0.6132	0.01752	0.0696	0.001355	3624.68	928	1420.67	0.87	0.7848	0.00103	0.0837	0.000391
1672.68	538	1546.21	14.59	0.6310	0.01825	0.0691	0.001453	3649.51	933	1425.82	0.81	0.7777	0.00091	0.0853	0.000389
1699.36	543	1530.09	15.04	0.6511	0.01896	0.0684	0.001559	3674.38	938	1437.95	1.40	0.7609	0.00179	0.0888	0.000510
1721.48	548	1514.02	15.32	0.6713	0.01947	0.0675	0.001651	3696.83	943	1439					



**Table E.7:  $a$ ,  $b$ , and  $\chi$ , with maximum offsets increasing from 69.7 m to 3984.4 m, for all receivers, for the longside only, (A+C). Best values (minimum standard error) are highlighted. Ambiguous values are obtained when rays are close to vertical resulting in large standard errors.**

Max Offset (m)	# observations	$a$	Standard Error	$b$	Standard Error	$\chi$	Standard Error	Max Offset (m)	# observations	$a$	Standard Error	$b$	Standard Error	$\chi$	Standard Error
69.67	9	2000.09	139925.2081	0.9502	178.0073	0.0002	622.9144	2021.28	406	1278.75	16.4267	0.9875	0.02382	0.0432	0.003007
73.25	10	2000.11	103505.2859	0.9503	131.8120	0.0002	485.3994	2047.77	411	1268.88	15.8284	1.0017	0.02310	0.0416	0.002970
74.74	11	2000.11	87487.3008	0.9503	111.17851	0.0002	472.093590	2073.48	417	1260.06	15.1239	1.0146	0.02220	0.0403	0.002911
93.23	18	2000.55	51761.2955	0.9511	65.99247	0.0002	189.622034	2099.20	421	1253.60	14.6884	1.0240	0.02166	0.0392	0.002876
114.92	23	2000.29	39486.3098	0.9506	50.53036	0.0002	89.395875	2122.91	426	1247.76	14.1385	1.0326	0.02093	0.0383	0.002821
136.23	28	1651.81	22.9928	0.5051	0.02731	0.1660	0.089408	2146.80	431	1244.40	13.6009	1.0375	0.02019	0.0378	0.002756
159.55	33	1664.78	22.8133	0.4902	0.02697	0.0079	0.037432	2171.82	436	1231.41	13.3290	1.0567	0.01996	0.0356	0.002778
185.80	38	1665.18	19.8259	0.4898	0.02345	0.0057	0.023885	2195.22	440	1224.53	12.8643	1.0670	0.01936	0.0343	0.002729
224.32	45	1663.12	17.8894	0.4923	0.02117	0.0015	0.014741	2223.37	447	1227.85	12.2328	1.0620	0.01838	0.0350	0.002624
247.11	50	2004.84	24997.2688	0.9612	32.12677	0.0002	11.997892	2249.94	451	1227.30	11.9260	1.0628	0.01793	0.0349	0.002581
273.34	55	1682.10	17.4960	0.4697	0.02054	0.0130	0.010229	2272.62	456	1229.54	11.4945	1.0595	0.01727	0.0354	0.002507
299.43	61	1677.64	16.6957	0.4748	0.01964	0.0280	0.008344	2299.83	462	1234.41	11.0614	1.0522	0.01658	0.0363	0.002429
324.60	66	1679.46	15.5544	0.4726	0.01829	0.0331	0.006792	2323.30	466	1234.72	10.7744	1.0517	0.01613	0.0364	0.002384
346.83	70	1674.73	14.8605	0.4782	0.01751	0.0330	0.005807	2348.62	471	1237.73	10.4166	1.0472	0.01559	0.0370	0.002321
373.16	75	1678.88	13.9731	0.4733	0.01643	0.0337	0.004765	2373.84	476	1241.37	10.1069	1.0418	0.01510	0.0378	0.002265
396.72	80	1671.75	13.5079	0.4817	0.01594	0.0346	0.004060	2397.57	481	1245.98	9.8168	1.0349	0.01463	0.0387	0.002211
421.11	85	1681.38	13.5908	0.4704	0.01597	0.0321	0.003606	2423.96	486	1250.22	9.5344	1.0286	0.01418	0.0395	0.002158
447.16	90	1677.47	13.0519	0.4750	0.01536	0.0322	0.003103	2448.35	491	1251.75	9.2518	1.0264	0.01376	0.0399	0.002113
473.07	96	1682.65	12.5900	0.4689	0.01479	0.0324	0.002645	2472.64	496	1253.70	8.9741	1.0235	0.01334	0.0403	0.002066
497.01	100	1687.87	13.3294	0.4626	0.01562	0.0372	0.002656	2497.27	501	1256.86	8.7085	1.0188	0.01292	0.0409	0.002018
523.77	106	1680.75	13.5361	0.4709	0.01591	0.0406	0.002442	2524.87	506	1259.28	8.4662	1.0152	0.01255	0.0414	0.001977
549.68	111	1686.14	13.3716	0.4645	0.01568	0.0425	0.002238	2548.53	511	1261.16	8.1839	1.0125	0.01213	0.0418	0.001927
574.42	116	1685.51	13.7029	0.4651	0.01607	0.0463	0.002150	2571.80	516	1262.62	7.9377	1.0103	0.01176	0.0421	0.001886
598.16	120	1684.52	13.4008	0.4663	0.01573	0.0478	0.001999	2596.86	521	1264.07	7.7145	1.0082	0.01143	0.0425	0.001849
624.92	126	1685.58	12.9885	0.4650	0.01524	0.0495	0.001786	2621.38	526	1264.31	7.4735	1.0078	0.01107	0.0425	0.001810
648.93	131	1684.55	12.5514	0.4661	0.01473	0.0503	0.001625	2649.52	532	1268.05	7.2160	1.0023	0.01068	0.0433	0.001762
674.71	136	1686.16	12.2482	0.4642	0.01436	0.0514	0.001500	2674.60	536	1268.40	7.0326	1.0018	0.01041	0.0434	0.001731
695.53	141	1684.52	11.8676	0.4661	0.01393	0.0518	0.001379	2698.02	540	1270.57	6.8674	0.9986	0.01016	0.0439	0.001701
722.97	146	1686.66	11.5861	0.4635	0.01358	0.0524	0.001281	2723.23	546	1272.36	6.6187	0.9960	0.00979	0.0443	0.001657
747.80	152	1684.10	11.2298	0.4665	0.01318	0.0529	0.001182	2747.23	551	1274.07	6.4189	0.9935	0.00949	0.0446	0.001620
772.71	156	1686.85	11.2520	0.4632	0.01319	0.0540	0.001141	2773.23	556	1275.74	6.2224	0.9910	0.00919	0.0450	0.001584
799.36	161	1684.63	11.1155	0.4658	0.01304	0.0547	0.001084	2795.75	560	1276.22	6.0773	0.9903	0.00898	0.0451	0.001561
822.94	165	1687.93	11.3327	0.4619	0.01328	0.0560	0.001074	2823.37	565	1275.73	5.8740	0.9910	0.00869	0.0450	0.001525
847.58	171	1684.44	11.9221	0.4658	0.01399	0.0578	0.001087	2849.91	571	1275.25	5.6299	0.9917	0.00834	0.0449	0.001483
873.16	176	1685.82	12.1741	0.4641	0.01428	0.0592	0.001077	2872.44	575	1275.15	5.4943	0.9919	0.00815	0.0449	0.001459
898.70	181	1679.42	12.1719	0.4716	0.01432	0.0591	0.001050	2895.99	580	1275.73	5.3284	0.9910	0.00790	0.0450	0.001430
921.31	185	1686.21	12.5276	0.4636	0.01469	0.0602	0.001056	2922.93	586	1275.90	5.1505	0.9907	0.00765	0.0451	0.001400
947.13	191	1679.45	13.5566	0.4714	0.01594	0.0618	0.001118	2946.35	591	1277.63	5.0075	0.9882	0.00743	0.0455	0.001372
972.35	195	1676.27	13.4691	0.4751	0.01586	0.0622	0.001097	2973.59	596	1278.67	4.8840	0.9867	0.00725	0.0457	0.001351
997.99	202	1674.08	13.4288	0.4777	0.01583	0.0617	0.001067	2995.88	601	1279.23	4.7472	0.9859	0.00705	0.0459	0.001326
1023.52	206	1680.39	13.7764	0.4702	0.01620	0.0627	0.001070	3023.06	606	1280.34	4.6224	0.9842	0.00687	0.0461	0.001304
1047.73	210	1677.38	13.9074	0.4737	0.01637	0.0634	0.001073	3047.19	611	1280.76	4.4959	0.9836	0.00668	0.0462	0.001281
1074.36	216	1675.78	13.8001	0.4755	0.01626	0.0641	0.001048	3072.06	616	1282.47	4.3919	0.9817	0.00653	0.0467	0.001262
1098.09	221	1675.92	13.7892	0.4752	0.01624	0.0649	0.001036	3097.79	621	1283.83	4.2740	0.9791	0.00635	0.0470	0.001239
1124.22	226	1676.13	14.1482	0.4749	0.01667	0.0659	0.001053	3123.28	626	1289.94	4.1001	1.0000	0.00155	0.0429	0.000396
1149.32	231	1673.02	14.5836	0.4784	0.01720	0.0668	0.001083	3147.80	631	1279.45	4.0759	0.9857	0.00150	0.0456	0.000390
1174.60	236	1670.43	14.9054	0.4814	0.01760	0.0676	0.001104	3173.84	636	1287.66	4.0590	0.9735	0.00147	0.0479	0.000385
1196.44	241	1667.23	14.8349	0.4851	0.01754	0.0680	0.001099	3197.66	641	1296.18	4.0448	0.9608	0.00144	0.0504	0.000382
1223.74	246	1668.59	14.7636	0.4834	0.01745	0.0686	0.001087	3224.52	646	1303.13	4.0306	0.9503	0.00104	0.0523	0.000329
1247.66	251	1668.64	14.9667	0.4833	0.01769	0.0694	0.001099	3246.31	651	1310.78	4.0209	0.9382	0.00103	0.0545	0.000331
1272.02	256	1665.41	15.1616	0.4870	0.01795	0.0700	0.001118	3274.71	657	1318.05	4.0057	0.9286	0.00103	0.0566	0.000333
1297.55	261	1662.81	15.0249	0.4900	0.01780	0.0703	0.001111	3298.23	661	1327.60	4.0152	0.9146	0.00104	0.0593	0.000340
1321.67	266	1662.62	14.8035	0.4902	0.01754	0.0706	0.001095	3322.80	666	1334.22	4.0213	0.9049	0.00104	0.0613	0.000344
1347.03	271	1662.15	14.7264	0.4907	0.01746	0.0710	0.001091	3348.76	671	1342.54	4.0341	0.8928	0.00105	0.0637	0.000352
1371.34	275	1659.37	14.6298	0.4939	0.01736	0.0712	0.001092	3371.17	676	1347.93	4.0416	0.8850	0.00088	0.0653	0.000337
1396.42	281	1655.46	14.8065	0.4984	0.01761	0.0717	0.001116	3397.60	681	1355.78	4.0798	0.8736	0.00089	0.0677	0.000348
1422.89	286	1651.86	14.9117	0.5026	0.01776	0.0720	0.001136	3420.89	687	1361.29	4.0700	0.8656	0.00090	0.0694	0.000354
1448.88	292	1645.41	15.0156	0.5102	0.01794	0.0723	0.001167	3448.24	691	1370.27	4.0798	0.8527	0.00092	0.0721	0.000368
1472.46	297	1641.40	15.3046	0.5149	0.01831	0.0727	0.001205	3472.84	696	1379.71	4.0925	0.8392	0.00112	0.0749	0.000404
1499.88	302	1634.82	15.6630	0.5227	0.01880	0.0729	0.001256	3498.61	701	1384.67	4.0879	0.8321	0.00096	0.0763	0.000394
1522.75	306	1630.98	15.9538	0.5272	0.01918	0.0732	0.001293	3522.81	706	1390.28	4.0528	0.8241	0.00097	0.0780	0.000402
1548.93	311	1625.16	16.3875	0.5341	0.01976	0.0735	0.001353	3549.68	711	1397.49	4.0772	0.8138	0.00099	0.0803	0.000417
1574.73	316	1615.07	17.2203	0.5461	0.02086	0.0736	0.001463	3572.79	716	1407.66	4.1284	0.7994	0.00169	0.0834	0.000522
1598.23	321	1603.15	18.0358	0.5604	0.02196	0.0736	0.001582	3596.29	721	1409.99	4.0938	0.7962	0.00104	0.0840	0.000447
1622.07	326	1588.30	18.6514	0.5784	0.02287	0.0732	0.001701	3624.68	726	1417.04	4.0513	0.7862	0.00105	0.0862	0.000460
1648.39	331														



**Table E.8:**  $a$ ,  $b$ , and  $\chi$ , with maximum offsets increasing from 2849.9 m to 3984.4 m, for all receivers, for the longside, longoffsets only, (D+C). Best values (minimum standard error) are highlighted.

Max Offset (m)	# observations	$a$	Standard Error	$b$	Standard Error	$\chi$	Standard Error	Max Offset (m)	# observations	$a$	Standard Error	$b$	Standard Error	$\chi$	Standard Error
2849.91	11	1470.53	90.18	0.6504	0.0686	0.1631	0.04575	3448.24	131	1506.57	10.92	0.5654	0.0175	0.2142	0.00765
2872.44	15	1460.49	69.43	0.6338	0.0584	0.1933	0.03704	3472.84	136	1508.08	14.51	0.5691	0.0237	0.2082	0.01042
2895.99	20	1506.75	50.44	0.5976	0.0467	0.1779	0.02653	3498.61	141	1506.63	13.83	0.5719	0.0228	0.2067	0.01015
2922.93	26	1515.68	38.93	0.5652	0.0398	0.2035	0.02118	3522.81	146	1500.56	13.54	0.5783	0.0226	0.2068	0.01024
2946.35	31	1541.42	32.98	0.5569	0.0358	0.1819	0.01744	3549.68	151	1498.00	13.05	0.5805	0.0220	0.2073	0.01008
2973.59	36	1549.17	29.21	0.5368	0.0331	0.1950	0.01540	3572.79	156	1495.94	17.73	0.5950	0.0309	0.1937	0.01443
2995.88	41	1534.85	26.39	0.5456	0.0316	0.2023	0.01423	3596.29	161	1492.85	17.12	0.5989	0.0303	0.1930	0.01429
3023.06	46	1535.25	23.58	0.5429	0.0293	0.2050	0.01275	3624.68	166	1490.67	16.46	0.6010	0.0294	0.1932	0.01403
3047.19	51	1527.11	21.44	0.5448	0.0275	0.2128	0.01178	3649.51	171	1484.55	16.03	0.6077	0.0291	0.1930	0.01411
3072.06	56	1533.55	20.89	0.5395	0.0274	0.2109	0.01146	3674.38	176	1485.91	19.46	0.6158	0.0362	0.1828	0.01783
3097.79	61	1530.88	18.57	0.5432	0.0250	0.2100	0.01033	3696.83	181	1481.32	18.56	0.6225	0.0352	0.1808	0.01758
3123.28	66	1530.10	18.78	0.5336	0.0255	0.2222	0.01044	3720.14	185	1477.81	18.09	0.6259	0.0346	0.1811	0.01750
3147.80	71	1529.38	17.53	0.5357	0.0242	0.2206	0.00987	3748.49	191	1473.87	17.27	0.6303	0.0336	0.1809	0.01724
3173.84	76	1530.25	16.06	0.5340	0.0225	0.2216	0.00912	3773.13	196	1472.15	17.29	0.6360	0.0343	0.1767	0.01784
3197.66	81	1524.53	15.07	0.5437	0.0216	0.2173	0.00881	3797.18	201	1470.29	16.56	0.6392	0.0333	0.1765	0.01749
3224.52	86	1521.55	14.41	0.5437	0.0209	0.2210	0.00853	3823.89	206	1465.41	15.73	0.6461	0.0323	0.1736	0.01726
3246.31	91	1523.07	13.96	0.5436	0.0205	0.2192	0.00836	3847.16	211	1462.33	15.60	0.6534	0.0328	0.1693	0.01780
3274.71	97	1529.62	13.07	0.5360	0.0193	0.2199	0.00790	3873.90	216	1466.86	15.55	0.6467	0.0327	0.1714	0.01775
3298.23	101	1530.62	12.81	0.5374	0.0191	0.2171	0.00777	3899.01	221	1461.65	15.42	0.6528	0.0330	0.1707	0.01820
3322.80	106	1526.40	12.46	0.5413	0.0188	0.2177	0.00772	3924.74	226	1457.66	14.82	0.6583	0.0323	0.1691	0.01808
3348.76	111	1523.01	12.02	0.5466	0.0184	0.2157	0.00764	3947.24	231	1459.47	14.96	0.6589	0.0331	0.1668	0.01867
3371.17	116	1518.38	12.02	0.5498	0.0186	0.2178	0.00780	3974.14	236	1460.58	15.12	0.6604	0.0340	0.1641	0.01935
3397.60	121	1514.90	11.83	0.5538	0.0185	0.2173	0.00786	3984.40	238	1456.83	14.49	0.6678	0.0333	0.1606	0.01918
3420.89	127	1509.37	11.29	0.5617	0.0180	0.2151	0.00780								

**Table E.9:**  $a$ ,  $b$ , and  $\chi$ , with maximum offsets increasing from 99.6 m to 1014.1 m, for all receivers, for the shortside only, (B). Best values (minimum standard error) are highlighted.

Max Offset (m)	# observations	$a$	Standard Error	$b$	Standard Error	$\chi$	Standard Error	Max Offset (m)	# observations	$a$	Standard Error	$b$	Standard Error	$\chi$	Standard Error
99.57	15	2000.21	55862.29	0.9504	71.2550	0.0002	199.53349	573.81	114	1629.25	13.07	0.5324	0.0157	0.0482	0.00213
119.62	21	2001.32	39254.67	0.9527	50.2985	0.0002	87.70875	599.45	119	1635.28	12.95	0.5251	0.0155	0.0491	0.00197
142.49	26	2000.86	36636.46	0.9517	46.9292	0.0002	56.80207	624.84	124	1631.34	12.59	0.5299	0.0151	0.0485	0.00179
174.10	32	1636.08	21.10	0.5243	0.0253	0.1022	0.04431	646.13	129	1631.04	12.32	0.5302	0.0148	0.0487	0.00165
195.77	37	1645.61	19.20	0.5129	0.0229	0.1039	0.03086	671.18	133	1631.73	12.00	0.5294	0.0144	0.0489	0.00153
224.50	43	1670.40	20.86	0.4837	0.0246	0.0536	0.02132	698.48	139	1629.20	11.99	0.5324	0.0139	0.0486	0.00139
246.71	48	1667.38	20.20	0.4875	0.0239	0.0214	0.01502	722.70	144	1628.59	11.33	0.5331	0.0136	0.0495	0.00130
269.42	52	1666.99	19.23	0.4881	0.0227	0.0121	0.01168	748.24	149	1624.80	11.40	0.5376	0.0137	0.0505	0.00126
297.14	58	1658.56	17.59	0.4980	0.0209	0.0132	0.00868	771.35	154	1624.61	11.43	0.5378	0.0138	0.0517	0.00121
324.69	64	1658.61	16.71	0.4979	0.0198	0.0189	0.00695	798.75	159	1620.55	11.63	0.5426	0.0140	0.0527	0.00120
347.76	68	1650.58	16.24	0.5074	0.0193	0.0197	0.00604	823.75	164	1617.36	12.20	0.5464	0.0147	0.0543	0.00122
373.06	73	1648.99	16.05	0.5092	0.0191	0.0285	0.00536	847.08	169	1620.34	12.38	0.5427	0.0149	0.0557	0.00120
399.63	79	1647.60	15.35	0.5108	0.0183	0.0340	0.00453	872.46	174	1619.21	12.07	0.5440	0.0146	0.0560	0.00114
419.78	83	1643.42	15.04	0.5157	0.0180	0.0370	0.00409	898.67	179	1615.67	12.10	0.5482	0.0146	0.0566	0.00112
444.64	88	1641.72	15.00	0.5176	0.0179	0.0429	0.00374	924.31	184	1613.97	12.45	0.5502	0.0151	0.0578	0.00113
470.94	94	1638.25	14.62	0.5217	0.0175	0.0465	0.00329	949.15	189	1611.46	12.71	0.5531	0.0154	0.0589	0.00114
497.40	99	1638.73	14.05	0.5211	0.0168	0.0481	0.00291	972.73	194	1607.52	13.21	0.5578	0.0160	0.0600	0.00117
519.69	104	1639.54	13.52	0.5201	0.0162	0.0470	0.00257	997.09	199	1608.49	13.58	0.5565	0.0165	0.0612	0.00119
544.98	108	1634.21	13.27	0.5265	0.0159	0.0457	0.00235	1014.08	202	1609.29	13.47	0.5555	0.0163	0.0615	0.00115

**Table E.10:**  $a$ ,  $b$ , and  $\chi$ , with maximum offsets increasing from 69.7 m to 1014.4 m, for all receivers, for the longside, shortoffsets only, (B'). This is the same as Table E.7 up to the offset of 998.0 m, and is included here for comparison with results for the shortside only (B), Table E.9. Best values (minimum standard error) are highlighted.

Max Offset (m)	# observations	$a$	Standard Error	$b$	Standard Error	$\chi$	Standard Error	Max Offset (m)	# observations	$a$	Standard Error	$b$	Standard Error	$\chi$	Standard Error
69.67	9	2000.06	106137.68	0.9501	135.18087	0.0002	559.65448	549.68	111	1686.14	13.37	0.4645	0.01568	0.0425	0.00224
73.25	10	2000.11	103505.29	0.9503	131.81201	0.0002	485.39942	574.42	116	1685.51	13.70	0.4651	0.01607	0.0463	0.00215
74.74	11	2000.11	87487.30	0.9503	111.17851	0.0002	472.09359	598.16	120	1684.52	13.40	0.4663	0.01573	0.0478	0.00200
93.23	18	2000.55	51761.30	0.9511	65.99247	0.0002	189.62203	624.92	126	1685.58	12.99	0.4650	0.01524	0.0495	0.00179
114.92	23	2000.29	39486.31	0.9506	50.53036	0.0002	89.39587	648.93	131	1684.55	12.55	0.4661	0.01473	0.0503	0.00163
136.23	28	1651.81	22.99	0.5051	0.02731	0.1660	0.08941	674.71	136	1686.16	12.25	0.4642	0.01436	0.0514	0.00150
159.55	33	1664.78	22.81	0.4902	0.02697	0.0079	0.03743	695.53	141	1684.52	11.87	0.4661	0.01393	0.0518	0.00138
185.80	38	1665.18	19.83	0.4898	0.02345	0.0057	0.02389	722.97	146	1686.66	11.59	0.4635	0.01358	0.0524	0.00128
224.32	45	1663.12	17.89	0.4923	0.02117	0.0015	0.01474	747.80	152	1684.10	11.23	0.4665	0.01318	0.0529	0.00118
247.11	50	2004.84	24997.27	0.9612	32.12677	0.0002	11.99789	772.71	156	1686.85	11.25	0.4632	0.01319	0.0540	0.00114
273.34	55	1682.10	17.50	0.4697	0.02054	0.0130	0.01023	799.36	161	1684.63	11.12	0.4658	0.01304	0.0547	0.00108
299.43	61	1677.64	16.70	0.4748	0.01964	0.0280	0.00834	822.94	165	1687.93	11.33	0.4619	0.01328	0.0560	0.00107
324.60	66	1679.46	15.55	0.4726	0.01829	0.0331	0.00679	847.58	171	1684.44	11.92	0.4658	0.01399	0.0578	0.00109
346.83	70	1674.73	14.86	0.4782	0.01751	0.0330	0.00581	873.16	176	1685.82	12.17	0.4641	0.01428	0.0592	0.00108
373.16	75	1678.88	13.97	0.4733	0.01643	0.0337	0.00476	898.70	181	1679.42	12.17	0.4716	0.01432	0.0591	0.00105
396.72	80	1671.75	13.51	0.4817	0.01594	0.0346	0.00406	921.31	185	1686.21	12.53	0.4636	0.01469	0.0602	0.00106
421.11	85	1681.38	13.59	0.4704	0.01597	0.0321	0.00361	947.13	191	1679.45	13.56	0.4714	0.01594	0.0618	0.00112
447.16	90	1677.47	13.05	0.4750	0.01536	0.0322	0.00310	972.35	195	1676.27	13.47	0.4751	0.01586	0.0622	0.00110
473.07	96	1682.65	12.59	0.4689	0.01479	0.0324	0.00264	997.99	202	1674.08	13.43	0.4777	0.01583	0.0617	0.00107
497.01	100	1687.87	13.33	0.4626	0.01562	0.0372	0.00266	1014.40	203	1677.39	13.56	0.4738	0.01597	0.0622	0.00106
523.77	106	1680.75	13.54	0.4709	0.01591	0.0406	0.00244								

## **APPENDIX F**

### **Forward Modelling**

Isotropic and Anisotropic Cases



**Table F.1a: Isotropic Case:  $a$ , and  $b$  from zero-offset VSP times, receiver at 1974 m.**

$a = 1592.258651185210$					$b = 0.575514064006845$					$\chi = 0$					$z = 1973.923$				
offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)
1014.078	0.000209626510788	1048.740	1036.432	-12.307	1485.368	0.000273040472415	1163.395	1136.798	-26.597	1485.368	0.000273040472415	1163.395	1136.798	-26.597	1485.368	0.000273040472415	1163.395	1136.798	-26.597
989.797	0.000205712753012	1043.697	1031.409	-12.288	1513.211	0.000276078525991	1171.040	1143.508	-27.532	1513.211	0.000276078525991	1171.040	1143.508	-27.532	1513.211	0.000276078525991	1171.040	1143.508	-27.532
966.288	0.000201861434798	1038.906	1027.439	-11.467	1539.303	0.000278858977004	1178.280	1149.417	-28.863	1539.303	0.000278858977004	1178.280	1149.417	-28.863	1539.303	0.000278858977004	1178.280	1149.417	-28.863
941.466	0.000197728989511	1033.947	1023.055	-10.891	1565.130	0.000281548776419	1185.517	1154.933	-30.584	1565.130	0.000281548776419	1185.517	1154.933	-30.584	1565.130	0.000281548776419	1185.517	1154.933	-30.584
915.969	0.000193413716236	1028.960	1018.204	-10.756	1588.644	0.000283944368610	1192.165	1160.874	-31.291	1588.644	0.000283944368610	1192.165	1160.874	-31.291	1588.644	0.000283944368610	1192.165	1160.874	-31.291
889.718	0.00018896311053	1023.942	1014.435	-9.507	1612.475	0.000286321211223	1198.960	1167.062	-31.897	1612.475	0.000286321211223	1198.960	1167.062	-31.897	1612.475	0.000286321211223	1198.960	1167.062	-31.897
864.303	0.00018445109466	1019.197	1010.473	-8.724	1638.883	0.000288895887271	1206.556	1173.549	-33.007	1638.883	0.000288895887271	1206.556	1173.549	-33.007	1638.883	0.000288895887271	1206.556	1173.549	-33.007
841.107	0.000180332827748	1014.966	1005.947	-9.019	1663.079	0.000291209993883	1213.574	1178.955	-34.619	1663.079	0.000291209993883	1213.574	1178.955	-34.619	1663.079	0.000291209993883	1213.574	1178.955	-34.619
816.118	0.000175831304874	1010.516	1002.145	-8.371	1689.771	0.000293685063573	1221.340	1185.425	-35.915	1689.771	0.000293685063573	1221.340	1185.425	-35.915	1689.771	0.000293685063573	1221.340	1185.425	-35.915
788.795	0.000170832978479	1005.780	998.318	-7.462	1711.871	0.000295969786599	1227.893	1191.524	-36.369	1711.871	0.000295969786599	1227.893	1191.524	-36.369	1711.871	0.000295969786599	1227.893	1191.524	-36.369
765.793	0.000166561833394	1001.900	994.844	-7.055	1739.048	0.000298112092385	1235.962	1197.521	-38.441	1739.048	0.000298112092385	1235.962	1197.521	-38.441	1739.048	0.000298112092385	1235.962	1197.521	-38.441
740.308	0.000162305993933	997.716	991.292	-6.424	1763.081	0.000300198038172	1243.152	1203.817	-39.335	1763.081	0.000300198038172	1243.152	1203.817	-39.335	1763.081	0.000300198038172	1243.152	1203.817	-39.335
716.162	0.000157164252031	993.865	987.772	-6.093	1789.170	0.000302425907052	1251.073	1210.837	-40.235	1789.170	0.000302425907052	1251.073	1210.837	-40.235	1789.170	0.000302425907052	1251.073	1210.837	-40.235
694.514	0.000152985000465	990.508	985.218	-5.290	1814.387	0.000304494673641	1258.665	1217.784	-40.881	1814.387	0.000304494673641	1258.665	1217.784	-40.881	1814.387	0.000304494673641	1258.665	1217.784	-40.881
663.944	0.000147003342623	985.922	980.535	-5.387	1836.461	0.000306279094921	1265.406	1223.474	-41.932	1836.461	0.000306279094921	1265.406	1223.474	-41.932	1836.461	0.000306279094921	1265.406	1223.474	-41.932
642.565	0.000142765274082	982.825	977.875	-4.950	1863.985	0.000308451379149	1273.866	1231.080	-42.786	1863.985	0.000308451379149	1273.866	1231.080	-42.786	1863.985	0.000308451379149	1273.866	1231.080	-42.786
617.231	0.000137680663139	979.272	975.246	-4.027	1888.688	0.000310351817400	1281.509	1235.614	-45.895	1888.688	0.000310351817400	1281.509	1235.614	-45.895	1888.688	0.000310351817400	1281.509	1235.614	-45.895
591.674	0.000132500320033	975.819	971.165	-4.654	1912.386	0.000312132086319	1288.885	1242.405	-46.480	1912.386	0.000312132086319	1288.885	1242.405	-46.480	1912.386	0.000312132086319	1288.885	1242.405	-46.480
568.580	0.000127265271806	972.814	968.847	-3.968	1936.696	0.000313915332891	1296.495	1250.340	-46.155	1936.696	0.000313915332891	1296.495	1250.340	-46.155	1936.696	0.000313915332891	1296.495	1250.340	-46.155
538.050	0.000121425391083	969.010	966.045	-2.965	1962.993	0.000315796344855	1304.775	1255.989	-48.786	1962.993	0.000315796344855	1304.775	1255.989	-48.786	1962.993	0.000315796344855	1304.775	1255.989	-48.786
515.799	0.00011655354013	966.360	963.125	-3.235	1986.236	0.000317417970578	1312.134	1262.363	-49.771	1986.236	0.000317417970578	1312.134	1262.363	-49.771	1986.236	0.000317417970578	1312.134	1262.363	-49.771
489.340	0.00011147870939	963.345	960.062	-3.283	2011.513	0.000319138702301	1320.179	1269.025	-51.154	2011.513	0.000319138702301	1320.179	1269.025	-51.154	2011.513	0.000319138702301	1320.179	1269.025	-51.154
469.040	0.00010606740167	961.133	958.225	-2.908	2038.012	0.000320895641195	1328.659	1276.389	-52.270	2038.012	0.000320895641195	1328.659	1276.389	-52.270	2038.012	0.000320895641195	1328.659	1276.389	-52.270
444.362	0.000101463996162	958.552	955.584	-2.968	2058.654	0.000322315182344	1335.397	1281.452	-53.845	2058.654	0.000322315182344	1335.397	1281.452	-53.845	2058.654	0.000322315182344	1335.397	1281.452	-53.845
418.215	0.000095797380544	955.983	953.700	-2.283	2089.406	0.000324169383499	1345.236	1291.095	-54.141	2089.406	0.000324169383499	1345.236	1291.095	-54.141	2089.406	0.000324169383499	1345.236	1291.095	-54.141
394.946	0.000090969352314	953.813	951.439	-2.375	2113.127	0.000325623237771	1352.943	1297.340	-55.603	2113.127	0.000325623237771	1352.943	1297.340	-55.603	2113.127	0.000325623237771	1352.943	1297.340	-55.603
373.059	0.000085858578081	951.881	949.506	-2.375	2137.010	0.000327049070906	1360.737	1304.095	-56.642	2137.010	0.000327049070906	1360.737	1304.095	-56.642	2137.010	0.000327049070906	1360.737	1304.095	-56.642
344.072	0.000079406553017	949.486	948.215	-1.271	2162.001	0.000328503809092	1368.928	1308.005	-60.921	2162.001	0.000328503809092	1368.928	1308.005	-60.921	2162.001	0.000328503809092	1368.928	1308.005	-60.921
324.116	0.000074934387020	947.946	946.461	-1.485	2190.353	0.000330107893497	1378.265	1318.307	-59.958	2190.353	0.000330107893497	1378.265	1318.307	-59.958	2190.353	0.000330107893497	1378.265	1318.307	-59.958
297.101	0.000068843303390	946.003	944.746	-1.258	2208.538	0.000331112994044	1384.277	1324.103	-60.174	2208.538	0.000331112994044	1384.277	1324.103	-60.174	2208.538	0.000331112994044	1384.277	1324.103	-60.174
275.418	0.000063925608551	944.564	943.693	-0.871	2240.131	0.000332808083626	1394.765	1332.692	-62.073	2240.131	0.000332808083626	1394.765	1332.692	-62.073	2240.131	0.000332808083626	1394.765	1332.692	-62.073
246.708	0.000057377986764	942.823	941.976	-0.847	2262.848	0.000333992490758	1402.339	1340.505	-61.834	2262.848	0.000333992490758	1402.339	1340.505	-61.834	2262.848	0.000333992490758	1402.339	1340.505	-61.834
225.285	0.000052467204414	941.646	940.090	-1.556	2285.069	0.000335122655714	1409.773	1346.629	-63.144	2285.069	0.000335122655714	1409.773	1346.629	-63.144	2285.069	0.000335122655714	1409.773	1346.629	-63.144
201.211	0.000046925935798	940.450	938.334	-2.116	2313.522	0.000336529579747	1419.328	1354.231	-65.098	2313.522	0.000336529579747	1419.328	1354.231	-65.098	2313.522	0.000336529579747	1419.328	1354.231	-65.098
182.634	0.000042634846020	939.618	937.775	-1.843	2338.818	0.000337743237750	1427.857	1361.689	-66.168	2338.818	0.000337743237750	1427.857	1361.689	-66.168	2338.818	0.000337743237750	1427.857	1361.689	-66.168
151.037	0.000035109403062	938.386	937.281	-1.105	2364.031	0.000338918806965	1436.387	1368.898	-67.489	2364.031	0.000338918806965	1436.387	1368.898	-67.489	2364.031	0.000338918806965	1436.387	1368.898	-67.489
136.395	0.000031904729124	937.894	936.890	-1.004	2387.757	0.000339994557160	1444.441	1376.166	-68.275	2387.757	0.000339994557160	1444.441	1376.166	-68.275	2387.757	0.000339994557160	1444.441	1376.166	-68.275
119.615	0.000027996108001	937.392	936.139	-1.252	2414.140	0.000341156703928	1453.427	1384.134	-69.293	2414.140	0.000341156703928	1453.427	1384.134	-69.293	2414.140	0.000341156703928	1453.427	1384.134	-69.293
94.486	0.000022112186426	936.760	935.331	-0.829	2438.403	0.000342441081677	1461.748	1389.482	-72.265	2438.403	0.000342441081677	1461.748	1389.482	-72.265	2438.403	0.000342441081677	1461.748	1389.482	-72.265
82.931	0.000019429200259	936.522	935.126	-1.396	2462.794	0.000343708213368	1470.076	1396.500	-73.576	2462.794	0.000343708213368	1470.076	1396.500	-73.576	2462.794	0.000343708213368	1470.076	1396.500	-73.576
76.916	0.000018022874721	936.409	935.534	-0.875	2487.308	0.000344201529301	1478.532	1404.673	-73.860	2487.308	0.000344201529301	1478.532	1404.673	-73.860					



**Table F.1b: Isotropic Case:  $a$ , and  $b$  from zero-offset VSP times, receiver at 2014 m.**

$a = 1592.258651185210$					$b = 0.575514064006845$					$z = 0$					$z = 2013.927$				
offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)
991.550	0.000201654230831	1056.171	1044.546	-11.625	1504.896	0.000270299158992	1178.452	1152.406	-26.046	1504.896	0.000270299158992	1178.452	1152.406	-26.046	1504.896	0.000270299158992	1178.452	1152.406	-26.046
967.175	0.000197716966781	1051.303	1039.433	-11.870	1532.702	0.000273277453099	1186.009	1159.518	-26.491	1532.702	0.000273277453099	1186.009	1159.518	-26.491	1532.702	0.000273277453099	1186.009	1159.518	-26.491
943.576	0.000193845400315	1046.683	1035.737	-10.946	1558.966	0.000276026059265	1193.223	1164.752	-28.471	1558.966	0.000276026059265	1193.223	1164.752	-28.471	1558.966	0.000276026059265	1193.223	1164.752	-28.471
918.728	0.000189705387838	1041.917	1031.620	-10.297	1584.736	0.000278662849997	1200.370	1170.728	-29.642	1584.736	0.000278662849997	1200.370	1170.728	-29.642	1584.736	0.000278662849997	1200.370	1170.728	-29.642
893.046	0.000185359168315	1037.101	1027.395	-9.706	1608.206	0.000281013068388	1206.938	1176.191	-30.747	1608.206	0.000281013068388	1206.938	1176.191	-30.747	1608.206	0.000281013068388	1206.938	1176.191	-30.747
866.861	0.000180836782854	1032.306	1023.883	-8.424	1632.059	0.000283352466466	1213.669	1182.031	-31.639	1632.059	0.000283352466466	1213.669	1182.031	-31.639	1632.059	0.000283352466466	1213.669	1182.031	-31.639
841.491	0.000176426853083	1027.774	1019.800	-7.974	1658.491	0.000285887348787	1221.192	1188.199	-32.794	1658.491	0.000285887348787	1221.192	1188.199	-32.794	1658.491	0.000285887348787	1221.192	1188.199	-32.794
818.125	0.000172288121928	1023.700	1015.300	-8.400	1682.662	0.000288153537308	1228.130	1193.896	-34.233	1682.662	0.000288153537308	1228.130	1193.896	-34.233	1682.662	0.000288153537308	1228.130	1193.896	-34.233
793.125	0.000167798605938	1019.449	1011.754	-7.694	1709.332	0.000290597333961	1235.848	1200.831	-35.017	1709.332	0.000290597333961	1235.848	1200.831	-35.017	1709.332	0.000290597333961	1235.848	1200.831	-35.017
765.709	0.000162802777077	1014.917	1008.324	-6.593	1731.466	0.000292580881624	1242.302	1206.627	-35.675	1731.466	0.000292580881624	1242.302	1206.627	-35.675	1731.466	0.000292580881624	1242.302	1206.627	-35.675
742.569	0.000158527571133	1011.199	1004.757	-6.442	1758.713	0.000294967979608	1250.306	1212.206	-38.100	1758.713	0.000294967979608	1250.306	1212.206	-38.100	1758.713	0.000294967979608	1250.306	1212.206	-38.100
717.025	0.000153747415346	1007.210	1001.513	-5.697	1782.727	0.000297022573371	1257.414	1218.930	-38.484	1782.727	0.000297022573371	1257.414	1218.930	-38.484	1782.727	0.000297022573371	1257.414	1218.930	-38.484
692.777	0.000149151206006	1003.538	998.272	-5.266	1809.004	0.000299218891144	1265.249	1224.991	-40.257	1809.004	0.000299218891144	1265.249	1224.991	-40.257	1809.004	0.000299218891144	1265.249	1224.991	-40.257
671.179	0.00014500977834	1000.361	995.647	-4.714	1834.144	0.000301270004102	1272.797	1232.119	-40.678	1834.144	0.000301270004102	1272.797	1232.119	-40.678	1834.144	0.000301270004102	1272.797	1232.119	-40.678
640.407	0.000139034242110	995.990	991.688	-4.302	1856.165	0.000303027049826	1279.450	1237.956	-41.494	1856.165	0.000303027049826	1279.450	1237.956	-41.494	1856.165	0.000303027049826	1279.450	1237.956	-41.494
619.150	0.00013487644448	993.080	988.858	-4.222	1883.229	0.000305051742529	1287.833	1244.659	-43.175	1883.229	0.000305051742529	1287.833	1244.659	-43.175	1883.229	0.000305051742529	1287.833	1244.659	-43.175
593.758	0.000129810849718	989.719	986.490	-3.229	1908.444	0.000307051492485	1295.398	1250.987	-44.411	1908.444	0.000307051492485	1295.398	1250.987	-44.411	1908.444	0.000307051492485	1295.398	1250.987	-44.411
568.106	0.000124657305285	986.455	982.274	-4.181	1932.226	0.000308819142825	1302.722	1257.720	-45.002	1932.226	0.000308819142825	1302.722	1257.720	-45.002	1932.226	0.000308819142825	1302.722	1257.720	-45.002
544.979	0.000119662388498	983.626	980.074	-3.553	1956.508	0.000310580263369	1310.242	1264.184	-46.058	1956.508	0.000310580263369	1310.242	1264.184	-46.058	1956.508	0.000310580263369	1310.242	1264.184	-46.058
513.842	0.000113571816005	979.990	977.187	-2.803	1982.824	0.000312442202163	1318.440	1270.513	-47.927	1982.824	0.000312442202163	1318.440	1270.513	-47.927	1982.824	0.000312442202163	1318.440	1270.513	-47.927
491.551	0.00010894927262	977.510	974.652	-2.858	2006.097	0.000314048979787	1325.730	1276.609	-49.121	2006.097	0.000314048979787	1325.730	1276.609	-49.121	2006.097	0.000314048979787	1325.730	1276.609	-49.121
465.116	0.00010341755348	974.703	971.956	-2.747	2031.400	0.00031574292660	1333.698	1283.866	-49.832	2031.400	0.00031574292660	1333.698	1283.866	-49.832	2031.400	0.00031574292660	1333.698	1283.866	-49.832
444.635	0.00009906192246	972.629	970.103	-2.527	2057.867	0.000317492382963	1342.078	1290.939	-51.140	2057.867	0.000317492382963	1342.078	1290.939	-51.140	2057.867	0.000317492382963	1342.078	1290.939	-51.140
419.775	0.000093810548193	970.231	967.793	-2.438	2078.568	0.000318819860907	1348.664	1296.333	-52.332	2078.568	0.000318819860907	1348.664	1296.333	-52.332	2078.568	0.000318819860907	1348.664	1296.333	-52.332
393.803	0.000088243082683	967.867	966.024	-1.843	2109.336	0.000320742056822	1358.504	1305.118	-53.386	2109.336	0.000320742056822	1358.504	1305.118	-53.386	2109.336	0.000320742056822	1358.504	1305.118	-53.386
370.105	0.000083125024313	965.836	963.975	-1.862	2133.030	0.000322181538855	1366.121	1311.261	-54.860	2133.030	0.000322181538855	1366.121	1311.261	-54.860	2133.030	0.000322181538855	1366.121	1311.261	-54.860
347.762	0.000078267666663	964.033	962.375	-1.658	2156.626	0.000323598085087	1373.837	1317.697	-56.140	2156.626	0.000323598085087	1373.837	1317.697	-56.140	2156.626	0.000323598085087	1373.837	1317.697	-56.140
318.675	0.00007368013275	961.849	960.815	-1.035	2181.960	0.000325044877507	1381.956	1322.426	-59.531	2181.960	0.000325044877507	1381.956	1322.426	-59.531	2181.960	0.000325044877507	1381.956	1322.426	-59.531
297.136	0.000067155731989	960.350	959.240	-1.092	2210.257	0.000326644989862	1391.176	1332.953	-58.223	2210.257	0.000326644989862	1391.176	1332.953	-58.223	2210.257	0.000326644989862	1391.176	1332.953	-58.223
269.418	0.000061013371498	958.575	957.826	-0.749	2238.452	0.0003283673212373	1397.128	1338.401	-58.727	2238.452	0.0003283673212373	1397.128	1338.401	-58.727	2238.452	0.0003283673212373	1397.128	1338.401	-58.727
246.999	0.000055913096068	957.241	956.764	-0.477	2260.084	0.000329321835536	1407.519	1346.712	-60.806	2260.084	0.000329321835536	1407.519	1346.712	-60.806	2260.084	0.000329321835536	1407.519	1346.712	-60.806
217.658	0.000049453536324	955.716	955.323	-0.393	2282.716	0.000330495669237	1414.985	1353.271	-61.714	2282.716	0.000330495669237	1414.985	1353.271	-61.714	2282.716	0.000330495669237	1414.985	1353.271	-61.714
195.765	0.000044531612892	954.687	953.803	-0.884	2304.890	0.000331618204253	1422.326	1359.676	-62.650	2304.890	0.000331618204253	1422.326	1359.676	-62.650	2304.890	0.000331618204253	1422.326	1359.676	-62.650
170.528	0.00003883956756	953.635	952.296	-1.339	2333.394	0.000333021810186	1431.799	1367.060	-64.739	2333.394	0.000333021810186	1431.799	1367.060	-64.739	2333.394	0.000333021810186	1431.799	1367.060	-64.739
150.322	0.000034266629687	952.896	951.830	-1.066	2358.739	0.00033423378210	1440.254	1375.573	-64.681	2358.739	0.00033423378210	1440.254	1375.573	-64.681	2358.739	0.00033423378210	1440.254	1375.573	-64.681
119.158	0.000027192651614	951.938	951.246	-0.692	2383.962	0.000335405752374	1448.700	1382.318	-66.381	2383.962	0.000335405752374	1448.700	1382.318	-66.381	2383.962	0.000335405752374	1448.700	1382.318	-66.381
100.035	0.000022841226068	951.460	951.140	-0.320	2407.702	0.000336749328248	1456.675	1389.120	-67.556	2407.702	0.000336749328248	1456.675	1389.120	-67.556	2407.702	0.000336749328248	1456.675	1389.120	-67.556
80.477	0.00001833974152	951.057	950.595	-0.462	2434.097	0.000337639588051	1465.572	1396.500	-69.072	2434.097	0.000337639588051	1465.572	1396.500	-69.072	2434.097	0.000337639588051	1465.572	1396.500	-69.072
52.512	0.000012001658523	950.632	950.600	-0.032	2458.515	0.00033862213284	1473.829	1403.233	-70.596	2458.515	0.00033862213284	1473.829	1403.233	-70.596	2458.515	0.00033862213284	1473.829	1403.233	-70.596
39.174	0.00000894579994	950.492	949.748	-0.744	2482.793	0.000339890192838	1481.956	1410.599	-71.355	2482.793	0.000339890192838	1481.956	1410.599	-71.355	2482.793	0.000339890192838	1481.956	1410.599	-71.355
37.125	0.000008486544180	950.474	949.931	-0.543	2507.442	0.00034068489684	1490.449	1418.106	-72.343	2507.442	0.00034068489684	1490.449	1418.106	-72.343	2507.442</				



**Table F.2a:** Inhomogeneous Isotropic Case: Forward modelling using  $a$ , and  $b$  estimates obtained from offset VSP times for segment 1 with receiver at 1974 m.

$a = 1677\ 328397137130$					$b = 0.475453558665$					$z = 0$					1973.923				
offset	$p$	computed time	observed time	residual	offset	$p$	computed time	observed time	residual	offset	$p$	computed time	observed time	residual	offset	$p$	computed time	observed time	residual
(m)		(ms)	(ms)		(m)		(ms)	(ms)		(m)		(ms)	(ms)		(m)		(ms)	(ms)	
84.530	0.000019930563972	935.498	935.707	0.209	2011.513	0.000324550345872	1323.510	1269.025	-54.485	3132.513	0.000324550345872	1323.510	1269.025	-54.485	3132.513	0.000324550345872	1323.510	1269.025	-54.485
93.234	0.000021978170725	935.680	935.612	-0.068	2038.012	0.000326422240018	1332.135	1276.389	-55.747	3162.001	0.000326422240018	1332.135	1276.389	-55.747	3162.001	0.000326422240018	1332.135	1276.389	-55.747
112.705	0.00005553994418	936.153	936.244	0.091	2058.654	0.000327848350200	1338.888	1281.452	-57.437	3189.888	0.000327848350200	1338.888	1281.452	-57.437	3189.888	0.000327848350200	1338.888	1281.452	-57.437
130.648	0.000030763440395	936.667	936.110	-0.557	2089.406	0.000329921729814	1349.002	1291.095	-57.907	3217.010	0.000329921729814	1349.002	1291.095	-57.907	3217.010	0.000329921729814	1349.002	1291.095	-57.907
152.613	0.000053905420261	937.399	937.377	-0.022	2113.127	0.000331480087016	1356.847	1297.340	-59.507	3245.010	0.000331480087016	1356.847	1297.340	-59.507	3245.010	0.000331480087016	1356.847	1297.340	-59.507
176.332	0.000041442663785	938.316	938.209	-0.108	2137.010	0.000330313727286	1364.782	1304.095	-60.687	3273.010	0.000330313727286	1364.782	1304.095	-60.687	3273.010	0.000330313727286	1364.782	1304.095	-60.687
200.664	0.000047103736030	939.394	939.183	-0.211	2162.001	0.000334581121556	1373.124	1308.005	-65.119	3301.010	0.000334581121556	1373.124	1308.005	-65.119	3301.010	0.000334581121556	1373.124	1308.005	-65.119
222.033	0.000052057261935	940.453	940.566	0.113	2190.353	0.000336313993129	1382.635	1318.307	-64.328	3329.010	0.000336313993129	1382.635	1318.307	-64.328	3329.010	0.000336313993129	1382.635	1318.307	-64.328
244.406	0.000057223543694	941.676	941.458	-0.218	2208.538	0.000337400514689	1388.760	1324.103	-64.658	3357.010	0.000337400514689	1388.760	1324.103	-64.658	3357.010	0.000337400514689	1388.760	1324.103	-64.658
270.447	0.00003208380075	943.244	942.481	-0.763	2231.104	0.000339242746572	1399.449	1332.692	-66.757	3385.010	0.000339242746572	1399.449	1332.692	-66.757	3385.010	0.000339242746572	1399.449	1332.692	-66.757
293.032	0.000068372014663	944.730	944.033	-0.697	2262.848	0.000340532479505	1407.170	1340.505	-66.665	3413.010	0.000340532479505	1407.170	1340.505	-66.665	3413.010	0.000340532479505	1407.170	1340.505	-66.665
317.805	0.000074004929848	946.493	945.562	-0.931	2285.069	0.000341766281931	1414.751	1346.629	-68.122	3441.010	0.000341766281931	1414.751	1346.629	-68.122	3441.010	0.000341766281931	1414.751	1346.629	-68.122
343.415	0.000079791412462	948.463	947.720	-0.743	2313.522	0.000343306725394	1424.497	1354.231	-70.267	3469.010	0.000343306725394	1424.497	1354.231	-70.267	3469.010	0.000343306725394	1424.497	1354.231	-70.267
369.719	0.000085693193003	950.639	949.464	-1.176	2338.818	0.0003449639884931	1433.199	1361.689	-71.510	3497.010	0.0003449639884931	1433.199	1361.689	-71.510	3497.010	0.0003449639884931	1433.199	1361.689	-71.510
393.092	0.000090890949978	952.703	952.038	-0.665	2363.041	0.000345935282290	1441.904	1368.898	-73.007	3525.010	0.000345935282290	1441.904	1368.898	-73.007	3525.010	0.000345935282290	1441.904	1368.898	-73.007
417.457	0.0000962868163738	954.984	953.379	-1.605	2387.157	0.000347124437122	1450.126	1376.166	-73.960	3553.010	0.000347124437122	1450.126	1376.166	-73.960	3553.010	0.000347124437122	1450.126	1376.166	-73.960
443.392	0.00010197669573	957.555	956.346	-1.209	2414.740	0.000348413041834	1459.302	1384.134	-75.163	3581.010	0.000348413041834	1459.302	1384.134	-75.163	3581.010	0.000348413041834	1459.302	1384.134	-75.163
465.151	0.000106710881291	959.825	958.015	-1.810	2438.494	0.000349527636594	1467.801	1392.482	-77.318	3609.010	0.000349527636594	1467.801	1392.482	-77.318	3609.010	0.000349527636594	1467.801	1392.482	-77.318
491.184	0.000112755849030	962.902	960.078	-2.824	2462.799	0.000350700700727	1476.309	1396.500	-79.810	3637.010	0.000350700700727	1476.309	1396.500	-79.810	3637.010	0.000350700700727	1476.309	1396.500	-79.810
515.711	0.000117567408303	965.496	963.346	-2.150	2487.398	0.000351814169023	1484.952	1404.673	-80.279	3665.010	0.000351814169023	1484.952	1404.673	-80.279	3665.010	0.000351814169023	1484.952	1404.673	-80.279
541.511	0.000123026137654	968.600	965.572	-3.028	2515.010	0.000353030117487	1494.683	1412.021	-82.662	3693.010	0.000353030117487	1494.683	1412.021	-82.662	3693.010	0.000353030117487	1494.683	1412.021	-82.662
566.218	0.000128189722330	971.703	968.150	-3.553	2538.668	0.000354044234360	1505.047	1420.411	-82.636	3721.010	0.000354044234360	1505.047	1420.411	-82.636	3721.010	0.000354044234360	1505.047	1420.411	-82.636
594.084	0.000133690486448	975.536	971.846	-3.510	2561.968	0.00035505515937246	1515.286	1425.506	-85.780	3749.010	0.00035505515937246	1515.286	1425.506	-85.780	3749.010	0.00035505515937246	1515.286	1425.506	-85.780
616.525	0.000138565035358	978.414	974.437	-3.978	2586.046	0.000356032252520	1520.188	1432.678	-77.360	3777.010	0.000356032252520	1520.188	1432.678	-77.360	3777.010	0.000356032252520	1520.188	1432.678	-77.360
640.390	0.00014340497382	981.739	977.709	-4.071	2611.466	0.000357009152470	1528.930	1439.409	-89.521	3805.010	0.000357009152470	1528.930	1439.409	-89.521	3805.010	0.000357009152470	1528.930	1439.409	-89.521
666.996	0.000148547911278	985.522	980.848	-4.684	2634.472	0.000357898806761	1537.154	1447.930	-82.224	3833.010	0.000357898806761	1537.154	1447.930	-82.224	3833.010	0.000357898806761	1537.154	1447.930	-82.224
686.674	0.000152622561419	988.631	983.892	-4.739	2664.740	0.000359035793435	1548.004	1457.009	-90.994	3861.010	0.000359035793435	1548.004	1457.009	-90.994	3861.010	0.000359035793435	1548.004	1457.009	-90.994
714.311	0.000157993860172	992.895	987.625	-5.270	2695.145	0.000360068930668	1558.217	1465.913	-92.850	3889.010	0.000360068930668	1558.217	1465.913	-92.850	3889.010	0.000360068930668	1558.217	1465.913	-92.850
734.065	0.00016184613081	996.083	990.735	-5.348	2713.475	0.000360788614433	1565.545	1471.688	-93.873	3917.010	0.000360788614433	1565.545	1471.688	-93.873	3917.010	0.000360788614433	1565.545	1471.688	-93.873
763.765	0.0001671051480444	1000.974	994.462	-6.512	2737.504	0.000361618387668	1574.224	1478.316	-95.907	3945.010	0.000361618387668	1574.224	1478.316	-95.907	3945.010	0.000361618387668	1574.224	1478.316	-95.907
790.341	0.000172502551940	1005.492	998.943	-6.550	2763.498	0.000362491089837	1583.635	1486.156	-97.347	3973.010	0.000362491089837	1583.635	1486.156	-97.347	3973.010	0.000362491089837	1583.635	1486.156	-97.347
818.637	0.000177718108531	1010.430	1002.359	-8.071	2790.900	0.000363363554890	1593.580	1492.776	-100.808	4001.010	0.000363363554890	1593.580	1492.776	-100.808	4001.010	0.000363363554890	1593.580	1492.776	-100.808
838.513	0.0001811380565436	1014.035	1006.107	-7.928	2818.515	0.0003642354599043	1603.627	1501.544	-102.004	4029.010	0.0003642354599043	1603.627	1501.544	-102.004	4029.010	0.0003642354599043	1603.627	1501.544	-102.004
864.183	0.000185983280718	1018.731	1009.904	-8.827	2840.130	0.000364917895020	1611.508	1509.010	-102.499	4057.010	0.000364917895020	1611.508	1509.010	-102.499	4057.010	0.000364917895020	1611.508	1509.010	-102.499
889.644	0.000190497413103	1023.525	1015.459	-8.066	2867.558	0.000365735244114	1621.528	1516.612	-104.912	4085.010	0.000365735244114	1621.528	1516.612	-104.912	4085.010	0.000365735244114	1621.528	1516.612	-104.912
916.870	0.0001952196280085	1028.776	1018.333	-10.443	2891.097	0.000366415880679	1630.145	1522.475	-107.670	4113.010	0.000366415880679	1630.145	1522.475	-107.670	4113.010	0.000366415880679	1630.145	1522.475	-107.670
938.114	0.000198987189801	1032.962	1022.636	-10.327	2913.408	0.000367034582484	1638.208	1527.969	-109.236	4141.010	0.000367034582484	1638.208	1527.969	-109.236	4141.010	0.000367034582484	1638.208	1527.969	-109.236
967.871	0.0002032928584229	1038.556	1028.093	-10.463	2936.083	0.000367675207926	1646.803	1537.739	-110.063	4169.010	0.000367675207926	1646.803	1537.739	-110.063	4169.010	0.000367675207926	1646.803	1537.739	-110.063
984.094	0.000206631032635	1044.286	1032.088	-12.198	2963.685	0.000368397522701	1656.816	1547.113	-112.312	4197.010	0.000368397522701	1656.816	1547.113	-112.312	4197.010	0.000368397522701	1656.816	1547.113	-112.312
1014.404	0.000211637905883	1048.625	1035.925	-12.700	2985.984	0.000369187762214	1666.037	1551.710	-113.321	4225.010	0.000369187762214	1666.037	1551.710	-113.321	4225.010	0.000369187762214	1666.037	1551.710	-113.321
1043.220	0.000216239160838	1054.790	1041.995	-12.795	3013.154	0.0003699650226760	1675.071	1560.112	-114.969	4253.010	0.0003699650226760	1675.071	1560.112	-114.969	4253.010	0.0003699650226760	1675.071	1560.112	-114.969
1065.184	0.0002199171658665	1059.577	1046.384	-13.193	3034.182	0.000370233509600	1683.996	1566.471	-117.526										



**Table F.2b: Inhomogeneous Isotropic Case: Forward modelling using  $a$ , and  $b$  estimates obtained from offset VSP times for segment 1 with receiver at 2014 m.**

$a = 1677.328397137130$					$b = 0.475435538665$					$z = 0$					$z = 2013.927$				
offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)
47.917	0.000011032028389	950.157	949.852	-0.305	2031.400	0.000321410852292	1338.012	1283.866	-54.146	2031.400	0.000321410852292	1338.012	1283.866	-54.146	2031.400	0.000321410852292	1338.012	1283.866	-54.146
67.679	0.000015577283710	950.420	950.437	0.017	2057.867	0.000323263811768	1346.543	1290.939	-55.604	2057.867	0.000323263811768	1346.543	1290.939	-55.604	2057.867	0.000323263811768	1346.543	1290.939	-55.604
87.531	0.000020138324322	950.775	950.647	-0.127	2078.568	0.000324681780021	1353.249	1296.333	-56.917	2078.568	0.000324681780021	1353.249	1296.333	-56.917	2078.568	0.000324681780021	1353.249	1296.333	-56.917
114.917	0.000026420090874	951.412	951.544	0.131	2109.336	0.000326739506013	1363.271	1305.118	-58.153	2109.336	0.000326739506013	1363.271	1305.118	-58.153	2109.336	0.000326739506013	1363.271	1305.118	-58.153
136.226	0.000031297616721	952.027	951.374	-0.653	2133.030	0.000328284180910	1371.031	1311.261	-59.771	2133.030	0.000328284180910	1371.031	1311.261	-59.771	2133.030	0.000328284180910	1371.031	1311.261	-59.771
159.548	0.000036623350588	952.819	953.025	0.205	2156.926	0.000329807533454	1378.894	1317.697	-61.198	2156.926	0.000329807533454	1378.894	1317.697	-61.198	2156.926	0.000329807533454	1378.894	1317.697	-61.198
185.804	0.000042600629033	953.860	953.865	0.006	2181.962	0.000331366981752	1387.171	1322.426	-64.745	2181.962	0.000331366981752	1387.171	1322.426	-64.745	2181.962	0.000331366981752	1387.171	1322.426	-64.745
210.975	0.00004830940268	955.004	954.950	-0.054	2210.257	0.000333085335985	1396.571	1332.953	-63.618	2210.257	0.000333085335985	1396.571	1332.953	-63.618	2210.257	0.000333085335985	1396.571	1332.953	-63.618
234.325	0.000053585336996	956.193	956.605	0.411	2228.452	0.000334166031848	1402.642	1338.401	-64.240	2228.452	0.000334166031848	1402.642	1338.401	-64.240	2228.452	0.000334166031848	1402.642	1338.401	-64.240
258.040	0.000058920667606	957.527	957.373	-0.154	2260.084	0.000336000324081	1413.241	1346.712	-66.529	2260.084	0.000336000324081	1413.241	1346.712	-66.529	2260.084	0.000336000324081	1413.241	1346.712	-66.529
284.557	0.000064856859114	959.169	958.386	-0.783	2282.716	0.000337278732176	1420.860	1353.271	-67.589	2282.716	0.000337278732176	1420.860	1353.271	-67.589	2282.716	0.000337278732176	1420.860	1353.271	-67.589
307.433	0.000069950676092	960.711	960.111	-0.600	2304.890	0.000338504287601	1428.353	1359.676	-68.676	2304.890	0.000338504287601	1428.353	1359.676	-68.676	2304.890	0.000338504287601	1428.353	1359.676	-68.676
332.872	0.000075583207582	962.562	961.630	-0.932	2333.394	0.000340041119443	1438.023	1367.060	-70.963	2333.394	0.000340041119443	1438.023	1367.060	-70.963	2333.394	0.000340041119443	1438.023	1367.060	-70.963
359.049	0.000081341486962	964.616	963.944	-0.672	2358.739	0.000341371887159	1446.658	1375.573	-71.085	2358.739	0.000341371887159	1446.658	1375.573	-71.085	2358.739	0.000341371887159	1446.658	1375.573	-71.085
385.343	0.000087084381166	966.830	965.418	-1.413	2383.962	0.000342663568529	1455.285	1382.318	-72.967	2383.962	0.000342663568529	1455.285	1382.318	-72.967	2383.962	0.000342663568529	1455.285	1382.318	-72.967
409.334	0.000092286563100	968.982	968.447	-0.535	2407.702	0.000343850041913	1463.434	1389.120	-74.315	2407.702	0.000343850041913	1463.434	1389.120	-74.315	2407.702	0.000343850041913	1463.434	1389.120	-74.315
433.705	0.000097532014582	971.295	969.921	-1.374	2434.097	0.000345136496790	1472.527	1396.500	-76.027	2434.097	0.000345136496790	1472.527	1396.500	-76.027	2434.097	0.000345136496790	1472.527	1396.500	-76.027
460.001	0.000103145449060	973.934	972.838	-1.096	2458.515	0.000346296478280	1480.969	1403.233	-77.736	2458.515	0.000346296478280	1480.969	1403.233	-77.736	2458.515	0.000346296478280	1480.969	1403.233	-77.736
482.029	0.000107809414403	976.257	974.457	-1.801	2482.793	0.000347421718729	1489.390	1410.509	-78.881	2482.793	0.000347421718729	1489.390	1410.509	-78.881	2482.793	0.000347421718729	1489.390	1410.509	-78.881
509.907	0.000113659585965	979.344	976.609	-2.735	2507.442	0.000348536001257	1497.967	1418.106	-79.861	2507.442	0.000348536001257	1497.967	1418.106	-79.861	2507.442	0.000348536001257	1497.967	1418.106	-79.861
532.777	0.000118413396137	981.998	979.967	-2.031	2535.041	0.000349750619264	1507.604	1425.056	-82.548	2535.041	0.000349750619264	1507.604	1425.056	-82.548	2535.041	0.000349750619264	1507.604	1425.056	-82.548
558.748	0.00012376905508	985.143	981.933	-3.210	2558.701	0.000350764658315	1515.891	1432.211	-83.680	2558.701	0.000350764658315	1515.891	1432.211	-83.680	2558.701	0.000350764658315	1515.891	1432.211	-83.680
583.493	0.000128803691937	988.268	985.107	-3.161	2581.986	0.000351738526540	1524.070	1439.055	-85.014	2581.986	0.000351738526540	1524.070	1439.055	-85.014	2581.986	0.000351738526540	1524.070	1439.055	-85.014
611.554	0.000134458797130	991.962	988.531	-3.431	2607.071	0.000352761432789	1532.906	1445.480	-87.426	2607.071	0.000352761432789	1532.906	1445.480	-87.426	2607.071	0.000352761432789	1532.906	1445.480	-87.426
634.129	0.000138958081943	995.048	991.086	-3.963	2631.588	0.000353735361238	1541.567	1452.599	-88.968	2631.588	0.000353735361238	1541.567	1452.599	-88.968	2631.588	0.000353735361238	1541.567	1452.599	-88.968
658.248	0.000143714635315	998.457	994.422	-4.035	2654.653	0.000354628737600	1549.736	1459.835	-89.901	2654.653	0.000354628737600	1549.736	1459.835	-89.901	2654.653	0.000354628737600	1549.736	1459.835	-89.901
684.072	0.000148748300773	1002.234	997.434	-4.799	2684.768	0.000355762443642	1560.433	1469.199	-91.234	2684.768	0.000355762443642	1560.433	1469.199	-91.234	2684.768	0.000355762443642	1560.433	1469.199	-91.234
705.124	0.000152805760155	1005.408	1000.876	-4.532	2713.012	0.000356927230417	1570.495	1477.709	-92.786	2713.012	0.000356927230417	1570.495	1477.709	-92.786	2713.012	0.000356927230417	1570.495	1477.709	-92.786
732.526	0.000158023913982	1009.667	1004.018	-5.648	2733.279	0.000357512772309	1577.734	1482.503	-95.231	2733.279	0.000357512772309	1577.734	1482.503	-95.231	2733.279	0.000357512772309	1577.734	1482.503	-95.231
752.696	0.00016181862599	1012.892	1007.432	-5.460	2757.260	0.000358344318452	1586.317	1489.196	-97.121	2757.260	0.000358344318452	1586.317	1489.196	-97.121	2757.260	0.000358344318452	1586.317	1489.196	-97.121
782.323	0.000167321047129	1017.768	1011.254	-6.514	2783.262	0.000359221378831	1595.646	1497.292	-98.355	2783.262	0.000359221378831	1595.646	1497.292	-98.355	2783.262	0.000359221378831	1595.646	1497.292	-98.355
809.041	0.00017228259710	1022.304	1015.565	-6.739	2810.670	0.000360118732028	1605.504	1504.319	-101.186	2810.670	0.000360118732028	1605.504	1504.319	-101.186	2810.670	0.000360118732028	1605.504	1504.319	-101.186
837.034	0.00017725213775	1027.196	1019.073	-8.122	2838.309	0.000360996034726	1615.470	1512.353	-103.117	2838.309	0.000360996034726	1615.470	1512.353	-103.117	2838.309	0.000360996034726	1615.470	1512.353	-103.117
857.170	0.000180832079189	1030.801	1022.852	-7.949	2859.972	0.000361664660259	1623.298	1519.220	-104.078	2859.972	0.000361664660259	1623.298	1519.220	-104.078	2859.972	0.000361664660259	1623.298	1519.220	-104.078
882.753	0.000185320231561	1035.485	1026.294	-9.191	2887.458	0.000362489382655	1633.250	1526.834	-106.415	2887.458	0.000362489382655	1633.250	1526.834	-106.415	2887.458	0.000362489382655	1633.250	1526.834	-106.415
908.363	0.000189746166282	1040.288	1031.885	-8.403	2911.043	0.0003631764448128	1641.807	1534.916	-106.891	2911.043	0.0003631764448128	1641.807	1534.916	-106.891	2911.043	0.0003631764448128	1641.807	1534.916	-106.891
935.422	0.000194348983625	1045.484	1034.363	-11.121	2933.070	0.000363801199084	1649.814	1540.726	-109.088	2933.070	0.000363801199084	1649.814	1540.726	-109.088	2933.070	0.000363801199084	1649.814	1540.726	-109.088
956.725	0.000197919590860	1049.663	1038.713	-10.949	2956.504	0.000364448277027	1658.347	1548.725	-109.621	2956.504	0.000364448277027	1658.347	1548.725	-109.621	2956.504	0.000364448277027	1658.347	1548.725	-109.621
986.543	0.000202838418240	1055.638	1044.700	-10.938	2983.778	0.000365178957903	1668.297	1555.046	-113.251	2983.778	0.000365178957903	1668.297	1555.046	-113.251	2983.778	0.000365178957903	1668.297	1555.046	-113.251
1002.868	0.000205492270865	1058.971	1049.014	-9.957	3006.069	0.000365758528237	1676.443	1562.470	-113.973	3006.069	0.000365758528237	1676.443	1562.470	-113.973	3006.069	0.000365758528237	1676.443	1562.470	-113.973
1033.179	0.000210346179030	1065.273	1052.495	-12.779	3033.245	0.000366444148964	1686.392	1570.417	-115.976	3033.245	0.000366444								



**Table F.3a: Inhomogeneous Isotropic Case: Forward modelling using  $a$ , and  $b$  estimates obtained from offset VSP times for segment 2 with receiver at 1974 m.**

$a = 1293.560359090070$					$b = 0.97265452341$					$z = 0$					$z = 1973.923$				
offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)
84.530	0.000018982190873	936.349	935.707	-0.642	2011.513	0.000290529231397	1294.968	1269.025	-25.943	2011.513	0.000290529231397	1294.968	1269.025	-25.943	2011.513	0.000290529231397	1294.968	1269.025	-25.943
93.234	0.000020931809298	936.523	935.612	-0.911	2038.012	0.000291775190130	1302.683	1276.389	-26.295	2038.012	0.000291775190130	1302.683	1276.389	-26.295	2038.012	0.000291775190130	1302.683	1276.389	-26.295
112.705	0.000025288043555	936.973	936.244	-0.729	2058.654	0.000292711907014	1308.716	1281.452	-27.264	2058.654	0.000292711907014	1308.716	1281.452	-27.264	2058.654	0.000292711907014	1308.716	1281.452	-27.264
130.648	0.000029294613480	937.463	936.110	-1.353	2089.406	0.000294053457127	1317.738	1291.095	-26.643	2089.406	0.000294053457127	1317.738	1291.095	-26.643	2089.406	0.000294053457127	1317.738	1291.095	-26.643
152.613	0.000034187440501	938.160	937.377	-0.783	2113.127	0.000295045134147	1324.725	1297.340	-27.385	2113.127	0.000295045134147	1324.725	1297.340	-27.385	2113.127	0.000295045134147	1324.725	1297.340	-27.385
176.332	0.000039454468919	939.033	938.209	-0.825	2137.010	0.000296006409025	1331.783	1304.095	-27.688	2137.010	0.000296006409025	1331.783	1304.095	-27.688	2137.010	0.000296006409025	1331.783	1304.095	-27.688
200.664	0.000044836912338	940.059	939.183	-0.876	2162.001	0.000296973075142	1339.193	1308.005	-31.188	2162.001	0.000296973075142	1339.193	1308.005	-31.188	2162.001	0.000296973075142	1339.193	1308.005	-31.188
222.033	0.000049544397288	941.067	940.566	-0.501	2190.353	0.000298022280650	1347.628	1318.307	-29.321	2190.353	0.000298022280650	1347.628	1318.307	-29.321	2190.353	0.000298022280650	1347.628	1318.307	-29.321
244.406	0.000054515817143	942.231	941.458	-0.773	2208.538	0.000298669196467	1353.053	1324.103	-28.950	2208.538	0.000298669196467	1353.053	1324.103	-28.950	2208.538	0.000298669196467	1353.053	1324.103	-28.950
270.447	0.000060132726528	943.723	942.481	-1.241	2240.131	0.000299745693439	1362.506	1332.692	-29.814	2240.131	0.000299745693439	1362.506	1332.692	-29.814	2240.131	0.000299745693439	1362.506	1332.692	-29.814
293.032	0.000065030972049	945.136	944.033	-1.103	2262.848	0.000300483382502	1369.324	1340.505	-28.819	2262.848	0.000300483382502	1369.324	1340.505	-28.819	2262.848	0.000300483382502	1369.324	1340.505	-28.819
317.805	0.000070370461679	946.813	945.562	-1.251	2285.069	0.000301176116986	1376.009	1346.629	-29.380	2285.069	0.000301176116986	1376.009	1346.629	-29.380	2285.069	0.000301176116986	1376.009	1346.629	-29.380
343.415	0.00007580867741	948.686	947.720	-0.966	2313.522	0.000302022353100	1384.590	1354.231	-30.360	2313.522	0.000302022353100	1384.590	1354.231	-30.360	2313.522	0.000302022353100	1384.590	1354.231	-30.360
369.719	0.000081435171983	950.755	949.464	-1.291	2338.818	0.000302737080698	1392.239	1361.689	-30.550	2338.818	0.000302737080698	1392.239	1361.689	-30.550	2338.818	0.000302737080698	1392.239	1361.689	-30.550
393.092	0.000086357018149	952.716	952.038	-0.677	2364.031	0.000303415026718	1399.881	1368.898	-30.983	2364.031	0.000303415026718	1399.881	1368.898	-30.983	2364.031	0.000303415026718	1399.881	1368.898	-30.983
417.457	0.000091445255860	954.882	953.379	-1.503	2387.757	0.000304022273043	1407.087	1376.166	-30.921	2387.757	0.000304022273043	1407.087	1376.166	-30.921	2387.757	0.000304022273043	1407.087	1376.166	-30.921
443.392	0.000096811251908	957.323	956.346	-0.977	2414.140	0.000304663294570	1415.116	1384.134	-30.982	2414.140	0.000304663294570	1415.116	1384.134	-30.982	2414.140	0.000304663294570	1415.116	1384.134	-30.982
465.151	0.000101271431056	959.478	958.015	-1.463	2438.493	0.000305223712555	1422.543	1389.482	-33.061	2438.493	0.000305223712555	1422.543	1389.482	-33.061	2438.493	0.000305223712555	1422.543	1389.482	-33.061
493.184	0.000106959619316	962.397	960.078	-2.319	2462.794	0.000305753646708	1429.967	1396.500	-33.467	2462.794	0.000305753646708	1429.967	1396.500	-33.467	2462.794	0.000305753646708	1429.967	1396.500	-33.467
515.711	0.00011481011748	964.857	963.346	-1.512	2487.398	0.000306261023094	1437.496	1404.673	-32.823	2487.398	0.000306261023094	1437.496	1404.673	-32.823	2487.398	0.000306261023094	1437.496	1404.673	-32.823
541.511	0.000116603458744	967.800	965.572	-2.228	2515.010	0.000306796282210	1445.959	1412.021	-33.938	2515.010	0.000306796282210	1445.959	1412.021	-33.938	2515.010	0.000306796282210	1445.959	1412.021	-33.938
566.218	0.000121450934432	970.741	968.150	-2.591	2538.668	0.000307226832845	1453.223	1420.411	-32.812	2538.668	0.000307226832845	1453.223	1420.411	-32.812	2538.668	0.000307226832845	1453.223	1420.411	-32.812
594.084	0.000126848297592	974.201	971.846	-2.354	2561.908	0.000307625092185	1460.367	1425.506	-34.862	2561.908	0.000307625092185	1460.367	1425.506	-34.862	2561.908	0.000307625092185	1460.367	1425.506	-34.862
616.525	0.00013139401836	977.095	974.437	-2.659	2586.946	0.000308027407436	1468.075	1432.678	-35.397	2586.946	0.000308027407436	1468.075	1432.678	-35.397	2586.946	0.000308027407436	1468.075	1432.678	-35.397
640.390	0.000135647489417	980.729	977.709	-3.020	2611.466	0.000308395086963	1475.632	1439.409	-36.224	2611.466	0.000308395086963	1475.632	1439.409	-36.224	2611.466	0.000308395086963	1475.632	1439.409	-36.224
666.096	0.000140437668720	983.828	980.848	-2.980	2634.472	0.000308716899894	1482.731	1447.930	-34.801	2634.472	0.000308716899894	1482.731	1447.930	-34.801	2634.472	0.000308716899894	1482.731	1447.930	-34.801
686.674	0.00014422780769	986.757	983.892	-2.865	2664.740	0.000309106955361	1492.081	1457.009	-35.072	2664.740	0.000309106955361	1492.081	1457.009	-35.072	2664.740	0.000309106955361	1492.081	1457.009	-35.072
714.131	0.000149202767804	990.785	987.625	-3.160	2693.145	0.000309439411736	1500.866	1465.913	-34.953	2693.145	0.000309439411736	1500.866	1465.913	-34.953	2693.145	0.000309439411736	1500.866	1465.913	-34.953
734.065	0.000152767296822	993.795	990.735	-3.060	2713.475	0.000309657863337	1507.159	1471.688	-35.472	2713.475	0.000309657863337	1507.159	1471.688	-35.472	2713.475	0.000309657863337	1507.159	1471.688	-35.472
763.765	0.000157997503982	998.410	994.462	-3.948	2737.504	0.000309895561469	1514.603	1478.316	-36.287	2737.504	0.000309895561469	1514.603	1478.316	-36.287	2737.504	0.000309895561469	1514.603	1478.316	-36.287
790.341	0.000162594460799	1002.670	998.943	-3.728	2763.498	0.000310128250682	1522.661	1486.156	-36.505	2763.498	0.000310128250682	1522.661	1486.156	-36.505	2763.498	0.000310128250682	1522.661	1486.156	-36.505
818.537	0.000167384952159	1007.322	1002.359	-4.963	2790.900	0.000310346692380	1531.163	1492.776	-38.386	2790.900	0.000310346692380	1531.163	1492.776	-38.386	2790.900	0.000310346692380	1531.163	1492.776	-38.386
838.613	0.000170740792904	1010.717	1006.107	-4.610	2818.515	0.000310539656788	1539.736	1501.544	-38.192	2818.515	0.000310539656788	1539.736	1501.544	-38.192	2818.515	0.000310539656788	1539.736	1501.544	-38.192
864.183	0.000174948191663	1015.136	1009.904	-5.232	2840.130	0.000310672122258	1546.450	1509.010	-37.440	2840.130	0.000310672122258	1546.450	1509.010	-37.440	2840.130	0.000310672122258	1546.450	1509.010	-37.440
889.644	0.000179062994476	1019.643	1015.459	-4.184	2867.558	0.000310817292801	1554.973	1516.612	-38.361	2867.558	0.000310817292801	1554.973	1516.612	-38.361	2867.558	0.000310817292801	1554.973	1516.612	-38.361
916.870	0.000183379909046	1024.577	1018.333	-6.244	2891.097	0.000310921916937	1562.290	1522.475	-39.815	2891.097	0.000310921916937	1562.290	1522.475	-39.815	2891.097	0.000310921916937	1562.290	1522.475	-39.815
938.114	0.000186688343706	1028.508	1022.636	-5.873	2913.083	0.000311003372687	1569.127	1527.969	-41.158	2913.083	0.000311003372687	1569.127	1527.969	-41.158	2913.083	0.000311003372687	1569.127	1527.969	-41.158
967.871	0.000191234274093	1034.132	1028.093	-6.039	2936.480	0.000311073176291	1576.404	1537.739	-38.665	2936.480	0.000311073176291	1576.404	1537.739	-38.665	2936.480	0.000311073176291	1576.404	1537.739	-38.665
984.094	0.000193668904164	1037.254	1032.088	-5.166	2963.685	0.000311132972100	1584.868	1544.497	-40.372	2963.685	0.000311132972100	1584.868	1544.497	-40.372	2963.685	0.000311132972100	1584.868	1544.497	-40.372
1014.404	0.000198135268599	1043.192	1035.925	-7.267	2985.984	0.000311165248682	1591.806	1551.710	-40.096	2985.984	0.000311165248682	1591.806	1551.710	-40.096	2985.984	0.000311165248682	1591.806	1551.710	-40.096
1043.220	0.000202281936662	1048.961	1041.995	-6.966	3013.154	0.000311184708355	1600.261	1560.112	-40.149	3013.154	0.000311184708355	1600.261	1560.112	-40.14					



**Table F.3b: Inhomogeneous Isotropic Case: Forward modelling using  $a$ , and  $b$  estimates obtained from offset VSP times for segment 2 with receiver at 2014 m.**

$a = 1293.560359090070$					$b = 0.972655452341$					$x = 0$					$x = 2013.927$				
offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)
47.917	0.000010464177093	948.171	949.852	1.681	2031.400	0.000286537190995	1305.166033	1283.866	-21.3	2031.400	0.000286537190995	1305.166033	1283.866	-21.3	2031.400	0.000286537190995	1305.166033	1283.866	-21.3
67.679	0.000014774907294	948.421	950.437	2.016	2057.867	0.000287770570065	1312.766161	1290.939	-21.83	2057.867	0.000287770570065	1312.766161	1290.939	-21.83	2057.867	0.000287770570065	1312.766161	1290.939	-21.83
87.531	0.000019100022460	948.757	950.647	1.890	2078.568	0.000288702303441	1318.732972	1296.333	-22.4	2078.568	0.000288702303441	1318.732972	1296.333	-22.4	2078.568	0.000288702303441	1318.732972	1296.333	-22.4
114.917	0.000025055576537	949.362	951.544	2.182	2109.336	0.000290034804078	1327.636639	1305.118	-22.52	2109.336	0.000290034804078	1327.636639	1305.118	-22.52	2109.336	0.000290034804078	1327.636639	1305.118	-22.52
136.226	0.000029678525789	949.945	951.374	1.429	2133.030	0.000291019066588	1334.520425	1311.261	-23.26	2133.030	0.000291019066588	1334.520425	1311.261	-23.26	2133.030	0.000291019066588	1334.520425	1311.261	-23.26
159.548	0.000034724726342	950.696	953.025	2.329	2156.926	0.000291975607088	1341.486155	1317.697	-23.79	2156.926	0.000291975607088	1341.486155	1317.697	-23.79	2156.926	0.000291975607088	1341.486155	1317.697	-23.79
185.804	0.000040385985163	951.682	953.865	2.183	2181.962	0.000292939578749	1348.807974	1322.426	-26.38	2181.962	0.000292939578749	1348.807974	1322.426	-26.38	2181.962	0.000292939578749	1348.807974	1322.426	-26.38
210.975	0.000045790819716	952.767	954.950	2.183	2210.257	0.000293983019095	1357.111558	1332.953	-24.16	2210.257	0.000293983019095	1357.111558	1332.953	-24.16	2210.257	0.000293983019095	1357.111558	1332.953	-24.16
234.325	0.000050782279183	953.894	956.605	2.711	2228.452	0.000294628700401	1362.466612	1338.401	-24.07	2228.452	0.000294628700401	1362.466612	1338.401	-24.07	2228.452	0.000294628700401	1362.466612	1338.401	-24.07
258.040	0.000055827596446	955.158	957.373	2.215	2260.084	0.000295705007115	1371.803415	1346.712	-25.09	2260.084	0.000295705007115	1371.803415	1346.712	-25.09	2260.084	0.000295705007115	1371.803415	1346.712	-25.09
284.557	0.000061437365257	956.713	958.386	1.672	2282.716	0.000296439825048	1378.504243	1353.271	-25.23	2282.716	0.000296439825048	1378.504243	1353.271	-25.23	2282.716	0.000296439825048	1378.504243	1353.271	-25.23
307.433	0.000066247609643	958.174	960.111	1.937	2304.890	0.000297131846297	1385.085356	1359.676	-25.41	2304.890	0.000297131846297	1385.085356	1359.676	-25.41	2304.890	0.000297131846297	1385.085356	1359.676	-25.41
332.872	0.000071562481723	959.927	961.630	1.703	2333.394	0.000297981602401	1393.566938	1367.060	-26.51	2333.394	0.000297981602401	1393.566938	1367.060	-26.51	2333.394	0.000297981602401	1393.566938	1367.060	-26.51
359.049	0.000076991158602	961.871	963.944	2.072	2358.739	0.000298700373423	1401.12827	1375.573	-25.56	2358.739	0.000298700373423	1401.12827	1375.573	-25.56	2358.739	0.000298700373423	1401.12827	1375.573	-25.56
385.343	0.000082400008864	963.967	965.418	1.451	2383.962	0.000299382080420	1408.671125	1382.318	-26.35	2383.962	0.000299382080420	1408.671125	1382.318	-26.35	2383.962	0.000299382080420	1408.671125	1382.318	-26.35
409.334	0.000087294629779	966.002	968.447	2.445	2407.702	0.000299993705062	1415.785889	1389.120	-26.67	2407.702	0.000299993705062	1415.785889	1389.120	-26.67	2407.702	0.000299993705062	1415.785889	1389.120	-26.67
433.705	0.000092224811595	968.190	969.921	1.731	2434.097	0.000300640294930	1423.712876	1396.500	-27.21	2434.097	0.000300640294930	1423.712876	1396.500	-27.21	2434.097	0.000300640294930	1423.712876	1396.500	-27.21
460.001	0.0000974940707894	970.685	972.838	2.153	2458.515	0.000301207761040	1431.060711	1403.233	-27.83	2458.515	0.000301207761040	1431.060711	1403.233	-27.83	2458.515	0.000301207761040	1431.060711	1403.233	-27.83
482.029	0.000101868070568	972.880	974.457	1.576	2482.793	0.000301743389345	1438.380001	1410.509	-27.87	2482.793	0.000301743389345	1438.380001	1410.509	-27.87	2482.793	0.000301743389345	1438.380001	1410.509	-27.87
509.907	0.000107346628809	975.797	976.609	0.813	2507.442	0.000302258647601	1445.824115	1418.106	-27.72	2507.442	0.000302258647601	1445.824115	1418.106	-27.72	2507.442	0.000302258647601	1445.824115	1418.106	-27.72
532.777	0.000111792732378	978.303	979.967	1.664	2535.041	0.000302802182772	1454.173731	1425.056	-29.12	2535.041	0.000302802182772	1454.173731	1425.056	-29.12	2535.041	0.000302802182772	1454.173731	1425.056	-29.12
558.748	0.000116786051718	981.271	981.933	0.662	2558.701	0.000303240689692	1461.343342	1432.211	-29.13	2558.701	0.000303240689692	1461.343342	1432.211	-29.13	2558.701	0.000303240689692	1461.343342	1432.211	-29.13
583.493	0.000121487973313	984.219	985.107	0.888	2581.986	0.000303648033500	1468.40907	1439.055	-29.35	2581.986	0.000303648033500	1468.40907	1439.055	-29.35	2581.986	0.000303648033500	1468.40907	1439.055	-29.35
611.554	0.000126751860891	987.702	988.531	0.829	2607.071	0.000304060567873	1476.031308	1445.480	-30.55	2607.071	0.000304060567873	1476.031308	1445.480	-30.55	2607.071	0.000304060567873	1476.031308	1445.480	-30.55
634.129	0.000130932708626	990.611	991.086	0.475	2631.588	0.000304437973542	1483.490671	1452.599	-30.89	2631.588	0.000304437973542	1483.490671	1452.599	-30.89	2631.588	0.000304437973542	1483.490671	1452.599	-30.89
658.248	0.000135345292465	993.822	994.422	0.600	2654.653	0.000304770257394	1490.516445	1459.835	-30.68	2654.653	0.000304770257394	1490.516445	1459.835	-30.68	2654.653	0.000304770257394	1490.516445	1459.835	-30.68
684.072	0.00014006291512	997.378	997.434	0.057	2684.768	0.000305171643450	1499.700643	1469.199	-30.5	2684.768	0.000305171643450	1499.700643	1469.199	-30.5	2684.768	0.000305171643450	1499.700643	1469.199	-30.5
705.124	0.000143756528023	1000.365	1000.876	0.511	2713.012	0.000305515503270	1508.324723	1477.709	-30.62	2713.012	0.000305515503270	1508.324723	1477.709	-30.62	2713.012	0.000305515503270	1508.324723	1477.709	-30.62
732.526	0.000148570112923	1004.370	1004.018	-0.352	2733.279	0.000305743276314	1514.519031	1482.503	-32.02	2733.279	0.000305743276314	1514.519031	1482.503	-32.02	2733.279	0.000305743276314	1514.519031	1482.503	-32.02
752.696	0.000152063811018	1007.402	1007.432	0.030	2757.260	0.000305992752994	1521.854023	1489.196	-32.66	2757.260	0.000305992752994	1521.854023	1489.196	-32.66	2757.260	0.000305992752994	1521.854023	1489.196	-32.66
782.323	0.000157118123098	1011.982	1011.254	-0.728	2783.262	0.000306239248766	1529.813684	1497.292	-32.52	2783.262	0.000306239248766	1529.813684	1497.292	-32.52	2783.262	0.000306239248766	1529.813684	1497.292	-32.52
809.041	0.000161596143601	1016.240	1015.565	-0.675	2810.670	0.000306472672865	1538.210337	1504.319	-33.89	2810.670	0.000306472672865	1538.210337	1504.319	-33.89	2810.670	0.000306472672865	1538.210337	1504.319	-33.89
837.034	0.000166205575137	1020.829	1019.073	-1.755	2838.309	0.000306681309221	1546.683912	1512.353	-34.33	2838.309	0.000306681309221	1546.683912	1512.353	-34.33	2838.309	0.000306681309221	1546.683912	1512.353	-34.33
857.170	0.000169468549131	1024.208	1022.852	-1.356	2859.972	0.000306826502368	1553.329408	1519.220	-34.11	2859.972	0.000306826502368	1553.329408	1519.220	-34.11	2859.972	0.000306826502368	1553.329408	1519.220	-34.11
882.753	0.000173550246682	1028.596	1026.294	-2.302	2887.458	0.000306988071186	1561.764953	1526.834	-34.93	2887.458	0.000306988071186	1561.764953	1526.834	-34.93	2887.458	0.000306988071186	1561.764953	1526.834	-34.93
908.363	0.000177564231130	1033.092	1031.885	-1.207	2911.043	0.000307106984342	1569.00688	1534.916	-34.09	2911.043	0.000307106984342	1569.00688	1534.916	-34.09	2911.043	0.000307106984342	1569.00688	1534.916	-34.09
935.422	0.000181726277618	1037.953	1034.363	-3.590	2933.070	0.000307201956332	1575.772417	1540.726	-35.05	2933.070	0.000307201956332	1575.772417	1540.726	-35.05	2933.070	0.000307201956332	1575.772417	1540.726	-35.05
956.725	0.000184945842462	1041.859	1038.713	-3.146	2956.504	0.000307286317245	1582.972457	1548.725	-34.25	2956.504	0.000307286317245	1582.972457	1548.725	-34.25	2956.504	0.000307286317245	1582.972457	1548.725	-34.25
986.543	0.000189367338202	1047.440	1044.700	-2.740	2983.778	0.000307363343420	1591.354556	1555.046	-36.31	2983.778	0.000307363343420	1591.354556	1555.046	-36.31	2983.778	0.000307363343420	1591.354556	1555.046	-36.31
1002.868	0.000191745952373	1050.551	1049.014	-1.537	3006.069	0.000307409782915	1598.206304	1562.470	-35.74	3006.069	0.000307409782915	1598.206304	1562.470	-35.74	3006.069	0.000307409782915	1598.206304	1562.4	



**Table F.4a:** Inhomogeneous Isotropic Case: Forward modelling using  $\alpha$ , and  $b$  estimates obtained from offset VSP times for segment 3 with receiver at 1974 m.

$a = 1131.623428157450$					$b = 1.219952706708$					$x = 0$					$z = 1973.923$				
offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)
84.530	0.000018313250589	935.559	935.707	0.148	2011.513	0.000270528167845	1275.503	1269.025	-6.478	2011.513	0.000270528167845	1275.503	1269.025	-6.478	2011.513	0.000270528167845	1275.503	1269.025	-6.478
93.234	0.000020193826047	935.727	935.612	-0.115	2038.012	0.000271481523931	1282.685	1276.389	-6.296	2038.012	0.000271481523931	1282.685	1276.389	-6.296	2038.012	0.000271481523931	1282.685	1276.389	-6.296
112.705	0.000024395417815	936.161	936.244	0.083	2058.654	0.000272191125791	1288.296	1281.452	-6.845	2058.654	0.000272191125791	1288.296	1281.452	-6.845	2058.654	0.000272191125791	1288.296	1281.452	-6.845
130.648	0.000028259230231	936.633	936.110	-0.523	2089.406	0.000273195755973	1296.682	1291.095	-5.587	2089.406	0.000273195755973	1296.682	1291.095	-5.587	2089.406	0.000273195755973	1296.682	1291.095	-5.587
152.613	0.000032976912204	937.306	937.377	0.071	2113.127	0.000273928759408	1303.171	1297.340	-5.831	2113.127	0.000273928759408	1303.171	1297.340	-5.831	2113.127	0.000273928759408	1303.171	1297.340	-5.831
176.332	0.000038054241407	938.148	938.209	0.060	2137.010	0.000274630722561	1309.722	1304.095	-5.627	2137.010	0.000274630722561	1309.722	1304.095	-5.627	2137.010	0.000274630722561	1309.722	1304.095	-5.627
200.664	0.000043241390854	939.137	939.183	0.045	2162.001	0.000275327329885	1316.594	1308.005	-8.589	2162.001	0.000275327329885	1316.594	1308.005	-8.589	2162.001	0.000275327329885	1316.594	1308.005	-8.589
222.033	0.00004776716390	940.110	940.566	0.456	2190.353	0.000276071802233	1324.411	1318.307	-6.104	2190.353	0.000276071802233	1324.411	1318.307	-6.104	2190.353	0.000276071802233	1324.411	1318.307	-6.104
244.406	0.000052502929612	941.232	941.458	0.226	2208.538	0.000276524221343	1329.435	1324.103	-5.333	2208.538	0.000276524221343	1329.435	1324.103	-5.333	2208.538	0.000276524221343	1329.435	1324.103	-5.333
270.447	0.000057972420960	942.670	942.481	-0.189	2240.131	0.000277264685708	1338.183	1332.692	-5.491	2240.131	0.000277264685708	1338.183	1332.692	-5.491	2240.131	0.000277264685708	1338.183	1332.692	-5.491
293.032	0.000062686143767	944.033	944.033	0.000	2262.848	0.000277622466698	1344.488	1340.505	-3.983	2262.848	0.000277622466698	1344.488	1340.505	-3.983	2262.848	0.000277622466698	1344.488	1340.505	-3.983
317.805	0.000067822124266	945.649	945.562	-0.087	2285.069	0.000278221364623	1350.665	1346.629	-4.036	2285.069	0.000278221364623	1350.665	1346.629	-4.036	2285.069	0.000278221364623	1350.665	1346.629	-4.036
343.415	0.000073090846801	947.454	947.720	0.266	2313.522	0.000278770351021	1358.589	1354.231	-4.359	2313.522	0.000278770351021	1358.589	1354.231	-4.359	2313.522	0.000278770351021	1358.589	1354.231	-4.359
369.719	0.000078456264101	949.447	949.464	0.017	2338.818	0.000279222639365	1365.647	1361.689	-3.958	2338.818	0.000279222639365	1365.647	1361.689	-3.958	2338.818	0.000279222639365	1365.647	1361.689	-3.958
393.092	0.000083182291977	951.336	952.038	0.702	2364.031	0.000279640771954	1372.692	1368.898	-3.794	2364.031	0.000279640771954	1372.692	1368.898	-3.794	2364.031	0.000279640771954	1372.692	1368.898	-3.794
417.457	0.000088065009761	953.423	953.379	-0.044	2387.757	0.000280005174918	1379.331	1376.166	-3.165	2387.757	0.000280005174918	1379.331	1376.166	-3.165	2387.757	0.000280005174918	1379.331	1376.166	-3.165
443.392	0.000093210615246	955.773	956.346	0.573	2414.140	0.000280378087612	1386.724	1384.134	-2.590	2414.140	0.000280378087612	1386.724	1384.134	-2.590	2414.140	0.000280378087612	1386.724	1384.134	-2.590
465.151	0.000097484550949	957.848	958.015	0.167	2438.493	0.000280692865186	1393.556	1389.482	-4.073	2438.493	0.000280692865186	1393.556	1389.482	-4.073	2438.493	0.000280692865186	1393.556	1389.482	-4.073
493.184	0.000102393090570	960.657	960.078	-0.580	2462.794	0.000280979487546	1400.380	1396.500	-3.881	2462.794	0.000280979487546	1400.380	1396.500	-3.881	2462.794	0.000280979487546	1400.380	1396.500	-3.881
515.711	0.000107256378387	963.025	963.346	0.321	2487.398	0.000281242393517	1407.297	1404.673	-2.624	2487.398	0.000281242393517	1407.297	1404.673	-2.624	2487.398	0.000281242393517	1407.297	1404.673	-2.624
541.511	0.000112152653870	965.855	965.572	-0.284	2515.010	0.000281505582120	1415.066	1412.021	-3.045	2515.010	0.000281505582120	1415.066	1412.021	-3.045	2515.010	0.000281505582120	1415.066	1412.021	-3.045
566.218	0.000116781713602	968.684	968.150	-0.534	2538.668	0.000281704972904	1421.728	1420.411	-1.318	2538.668	0.000281704972904	1421.728	1420.411	-1.318	2538.668	0.000281704972904	1421.728	1420.411	-1.318
594.084	0.000121930529493	972.010	971.846	-0.164	2561.908	0.000281877957231	1428.277	1425.506	-2.772	2561.908	0.000281877957231	1428.277	1425.506	-2.772	2561.908	0.000281877957231	1428.277	1425.506	-2.772
616.525	0.000126019750225	974.792	974.437	-0.355	2586.946	0.000282039580937	1435.337	1432.678	-2.659	2586.946	0.000282039580937	1435.337	1432.678	-2.659	2586.946	0.000282039580937	1435.337	1432.678	-2.659
640.390	0.000130311413722	977.851	977.709	-0.142	2611.466	0.000282173604967	1442.254	1439.409	-2.846	2611.466	0.000282173604967	1442.254	1439.409	-2.846	2611.466	0.000282173604967	1442.254	1439.409	-2.846
666.096	0.000134866478516	981.259	980.848	-0.412	2634.472	0.000282278072496	1448.747	1447.930	-0.817	2634.472	0.000282278072496	1448.747	1447.930	-0.817	2634.472	0.000282278072496	1448.747	1447.930	-0.817
686.674	0.000138461846155	984.072	983.892	-0.180	2664.740	0.000282384983711	1457.293	1457.009	-0.284	2664.740	0.000282384983711	1457.293	1457.009	-0.284	2664.740	0.000282384983711	1457.293	1457.009	-0.284
714.131	0.000143186553927	987.938	987.625	-0.314	2693.145	0.000282454659565	1465.315	1465.913	0.598	2693.145	0.000282454659565	1465.315	1465.913	0.598	2693.145	0.000282454659565	1465.315	1465.913	0.598
734.065	0.000146564220369	990.826	990.735	-0.092	2713.475	0.000282486809048	1471.058	1471.688	0.630	2713.475	0.000282486809048	1471.058	1471.688	0.630	2713.475	0.000282486809048	1471.058	1471.688	0.630
763.765	0.0001513618445	995.253	994.462	-0.791	2737.504	0.000282506239161	1477.846	1478.316	0.470	2737.504	0.000282506239161	1477.846	1478.316	0.470	2737.504	0.000282506239161	1477.846	1478.316	0.470
790.341	0.000155856877013	999.338	998.943	-0.395	2763.498	0.000282505176003	1485.189	1486.156	0.967	2763.498	0.000282505176003	1485.189	1486.156	0.967	2763.498	0.000282505176003	1485.189	1486.156	0.967
818.537	0.000160375690842	1003.796	1002.359	-1.437	2790.900	0.000282479896306	1492.930	1492.776	-0.154	2790.900	0.000282479896306	1492.930	1492.776	-0.154	2790.900	0.000282479896306	1492.930	1492.776	-0.154
838.613	0.000163536528566	1007.048	1006.107	-0.941	2818.515	0.000282430067201	1500.730	1501.544	0.813	2818.515	0.000282430067201	1500.730	1501.544	0.813	2818.515	0.000282430067201	1500.730	1501.544	0.813
864.183	0.000167493835880	1011.280	1009.904	-1.376	2840.130	0.000282374482239	1506.835	1509.010	2.175	2840.130	0.000282374482239	1506.835	1509.010	2.175	2840.130	0.000282374482239	1506.835	1509.010	2.175
889.644	0.000171357225174	1015.594	1015.459	-0.135	2867.558	0.000282283579839	1514.578	1516.612	2.033	2867.558	0.000282283579839	1514.578	1516.612	2.033	2867.558	0.000282283579839	1514.578	1516.612	2.033
916.870	0.000175403197378	1020.315	1018.333	-1.982	2891.097	0.000282284882724	1521.222	1522.475	1.253	2891.097	0.000282284882724	1521.222	1522.475	1.253	2891.097	0.000282284882724	1521.222	1522.475	1.253
938.114	0.00017848618880	1024.074	1022.636	-1.438	2913.083	0.0002822084141967	1527.425	1527.969	0.544	2913.083	0.0002822084141967	1527.425	1527.969	0.544	2913.083	0.0002822084141967	1527.425	1527.969	0.544
967.871	0.000182743825248	1029.449	1028.093	-1.356	2936.480	0.000281958910318	1534.023	1537.739	3.716	2936.480	0.000281958910318	1534.023	1537.739	3.716	2936.480	0.000281958910318	1534.023	1537.739	3.716
984.094	0.000185013384794	1032.432	1032.088	-0.344	2963.685	0.000281794579443	1541.692	1544.497	2.805	2963.685	0.000281794579443	1541.692	1544.497	2.805	2963.685	0.000281794579443	1541.692	1544.497	2.805
1014.404	0.000189169234577	1038.103	1035.925	-2.178	2985.984	0.000281645299694	1547.974	1551.710	3.736	2985.984	0.000281645299694	1547.974	1551.710	3.736	2985.984	0.000281645299694	1547.974	1551.710	3.736
1043.220	0.000193018206931	1043.610	1041.995	-1.615	3013.154	0.000281446158424	1555.624	1560.112	4.488	3013.154	0.000281446158424	1555.624	1560.112	4.488	3013.154	0.000281446158424	1555.624	1560.112	4.488
1065.184	0.000195885011217	10																	



**Table F.4b:** Inhomogeneous Isotropic Case: Forward modelling using  $\alpha$ , and  $b$  estimates obtained from offset VSP times for segment 3 with receiver at 2014 m.

$a = 1131.623428157450$					$b = 1.219952706708$					$z = 0$					$z = 2013.927$				
offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)
47.917	0.000010077824609	946.251	949.852	3.601	2031.400	0.000266416385435	1284.105	1283.866	-0.239	2031.400	0.000266416385435	1284.105	1283.866	-0.239	2031.400	0.000266416385435	1284.105	1283.866	-0.239
67.679	0.000014229054921	946.491	950.437	3.946	2057.867	0.000267363526428	1291.169	1290.939	-0.230	2057.867	0.000267363526428	1291.169	1290.939	-0.230	2057.867	0.000267363526428	1291.169	1290.939	-0.230
87.531	0.000018393785357	946.815	950.647	3.833	2078.568	0.000268072222036	1296.711	1296.333	-0.378	2078.568	0.000268072222036	1296.711	1296.333	-0.378	2078.568	0.000268072222036	1296.711	1296.333	-0.378
114.917	0.000024127724152	947.397	951.544	4.147	2109.336	0.000269074657789	1304.975	1305.118	0.143	2109.336	0.000269074657789	1304.975	1305.118	0.143	2109.336	0.000269074657789	1304.975	1305.118	0.143
136.226	0.000028577872757	947.958	951.374	3.415	2133.030	0.000269805988668	1311.359	1311.261	-0.098	2133.030	0.000269805988668	1311.359	1311.261	-0.098	2133.030	0.000269805988668	1311.359	1311.261	-0.098
159.548	0.000033434512520	948.682	953.025	4.343	2156.926	0.000270508585433	1317.815	1317.697	-0.118	2156.926	0.000270508585433	1317.815	1317.697	-0.118	2156.926	0.000270508585433	1317.815	1317.697	-0.118
185.804	0.000038881731216	949.631	953.865	4.234	2181.962	0.000271207796769	1324.596	1322.426	-2.170	2181.962	0.000271207796769	1324.596	1322.426	-2.170	2181.962	0.000271207796769	1324.596	1322.426	-2.170
210.975	0.000044080645241	950.675	954.950	4.275	2210.257	0.000271953658372	1332.280	1332.953	0.673	2210.257	0.000271953658372	1332.280	1332.953	0.673	2210.257	0.000271953658372	1332.280	1332.953	0.673
234.325	0.000048880373575	951.761	956.605	4.844	2228.452	0.000272408939781	1337.233	1338.401	1.169	2228.452	0.000272408939781	1337.233	1338.401	1.169	2228.452	0.000272408939781	1337.233	1338.401	1.169
258.040	0.000053730183215	952.977	957.373	4.396	2260.084	0.000273156107298	1345.861	1346.712	0.851	2260.084	0.000273156107298	1345.861	1346.712	0.851	2260.084	0.000273156107298	1345.861	1346.712	0.851
284.557	0.000059120328414	954.474	958.386	3.912	2282.716	0.000273656926951	1352.049	1353.271	1.222	2282.716	0.000273656926951	1352.049	1353.271	1.222	2282.716	0.000273656926951	1352.049	1353.271	1.222
307.433	0.000063740175762	955.879	960.111	4.232	2304.890	0.000274120933976	1358.123	1359.676	1.554	2304.890	0.000274120933976	1358.123	1359.676	1.554	2304.890	0.000274120933976	1358.123	1359.676	1.554
332.872	0.000068842230892	957.565	961.630	4.065	2333.394	0.000274679466011	1365.944	1367.060	1.116	2333.394	0.000274679466011	1365.944	1367.060	1.116	2333.394	0.000274679466011	1365.944	1367.060	1.116
359.049	0.000074050641333	959.436	963.944	4.508	2358.739	0.000275141112531	1372.912	1375.573	2.661	2358.739	0.000275141112531	1372.912	1375.573	2.661	2358.739	0.000275141112531	1372.912	1375.573	2.661
385.343	0.000079236861167	961.451	965.418	3.966	2383.962	0.00027568672667	1379.857	1382.318	2.461	2383.962	0.00027568672667	1379.857	1382.318	2.461	2383.962	0.00027568672667	1379.857	1382.318	2.461
409.334	0.000083927064236	963.408	968.447	5.039	2407.702	0.000276242724770	1386.404	1389.120	2.716	2407.702	0.000276242724770	1386.404	1389.120	2.716	2407.702	0.000276242724770	1386.404	1389.120	2.716
433.705	0.000088648286473	965.512	969.921	4.409	2434.097	0.000276327079259	1393.692	1396.500	2.808	2434.097	0.000276327079259	1393.692	1396.500	2.808	2434.097	0.000276327079259	1393.692	1396.500	2.808
460.001	0.000093691180609	967.909	972.838	4.929	2458.515	0.000276653783263	1400.444	1403.233	2.789	2458.515	0.000276653783263	1400.444	1403.233	2.789	2458.515	0.000276653783263	1400.444	1403.233	2.789
482.029	0.00009873101194	970.019	974.457	4.438	2482.793	0.000276951798117	1407.164	1410.509	3.345	2482.793	0.000276951798117	1407.164	1410.509	3.345	2482.793	0.000276951798117	1407.164	1410.509	3.345
509.907	0.000103107646990	972.821	976.609	3.789	2507.442	0.000277227656401	1413.994	1418.106	4.112	2507.442	0.000277227656401	1413.994	1418.106	4.112	2507.442	0.000277227656401	1413.994	1418.106	4.112
532.777	0.000107351634784	975.227	979.967	4.740	2535.041	0.000277505389580	1421.649	1425.056	3.407	2535.041	0.000277505389580	1421.649	1425.056	3.407	2535.041	0.000277505389580	1421.649	1425.056	3.407
558.748	0.00011214731485	978.077	981.933	3.856	2558.701	0.000277717952447	1428.217	1432.211	3.994	2558.701	0.000277717952447	1428.217	1432.211	3.994	2558.701	0.000277717952447	1428.217	1432.211	3.994
583.493	0.000116595176078	980.907	985.107	4.200	2581.986	0.000277904699109	1434.686	1439.055	4.369	2581.986	0.000277904699109	1434.686	1439.055	4.369	2581.986	0.000277904699109	1434.686	1439.055	4.369
611.554	0.000121605870133	984.249	988.531	4.281	2607.071	0.000278081568837	1441.660	1445.480	3.820	2607.071	0.000278081568837	1441.660	1445.480	3.820	2607.071	0.000278081568837	1441.660	1445.480	3.820
634.129	0.000125581426486	987.040	991.086	4.046	2631.588	0.000278230663522	1448.479	1452.599	4.119	2631.588	0.000278230663522	1448.479	1452.599	4.119	2631.588	0.000278230663522	1448.479	1452.599	4.119
658.248	0.000129773072567	990.119	994.422	4.303	2654.653	0.000278350003618	1454.898	1459.835	4.936	2654.653	0.000278350003618	1454.898	1459.835	4.936	2654.653	0.000278350003618	1454.898	1459.835	4.936
684.072	0.000134195663345	993.528	997.434	3.907	2684.768	0.000278476091829	1463.283	1469.199	5.916	2684.768	0.000278476091829	1463.283	1469.199	5.916	2684.768	0.000278476091829	1463.283	1469.199	5.916
705.124	0.000137750115596	996.390	1000.876	4.486	2713.012	0.000278564604367	1471.149	1477.709	6.560	2713.012	0.000278564604367	1471.149	1477.709	6.560	2713.012	0.000278564604367	1471.149	1477.709	6.560
732.526	0.000142306930320	1000.227	1004.018	3.791	2733.279	0.000278610860593	1476.795	1482.503	5.708	2733.279	0.000278610860593	1476.795	1482.503	5.708	2733.279	0.000278610860593	1476.795	1482.503	5.708
752.696	0.000145610210205	1003.131	1007.432	4.301	2757.260	0.000278647434411	1483.477	1489.196	5.719	2757.260	0.000278647434411	1483.477	1489.196	5.719	2757.260	0.000278647434411	1483.477	1489.196	5.719
782.323	0.000150382657366	1007.516	1011.254	3.738	2783.262	0.000278665397393	1490.723	1497.292	6.569	2783.262	0.000278665397393	1490.723	1497.292	6.569	2783.262	0.000278665397393	1490.723	1497.292	6.569
809.041	0.000154604277738	1011.591	1015.565	3.974	2810.670	0.000278660561922	1498.161	1504.319	6.158	2810.670	0.000278660561922	1498.161	1504.319	6.158	2810.670	0.000278660561922	1498.161	1504.319	6.158
837.034	0.000158942824314	1015.979	1019.073	3.094	2838.309	0.000278631688574	1506.062	1512.353	6.291	2838.309	0.000278631688574	1506.062	1512.353	6.291	2838.309	0.000278631688574	1506.062	1512.353	6.291
857.170	0.000162009536929	1019.211	1022.852	3.642	2859.972	0.000278592671319	1512.098	1519.220	7.122	2859.972	0.000278592671319	1512.098	1519.220	7.122	2859.972	0.000278592671319	1512.098	1519.220	7.122
882.753	0.000165840187052	1023.405	1026.294	2.889	2887.458	0.000278523015010	1519.754	1526.834	7.080	2887.458	0.000278523015010	1519.754	1526.834	7.080	2887.458	0.000278523015010	1519.754	1526.834	7.080
908.363	0.000169600969009	1027.700	1031.885	4.185	2911.043	0.000278445743150	1526.323	1534.916	8.593	2911.043	0.000278445743150	1526.323	1534.916	8.593	2911.043	0.000278445743150	1526.323	1534.916	8.593
935.422	0.000173493477275	1032.342	1034.363	2.021	2933.070	0.000278359371603	1532.455	1540.726	8.271	2933.070	0.000278359371603	1532.455	1540.726	8.271	2933.070	0.000278359371603	1532.455	1540.726	8.271
956.725	0.000176499391288	1036.070	1038.713	2.643	2956.504	0.000278252794326	1538.977	1548.725	9.748	2956.504	0.000278252794326	1538.977	1548.725	9.748	2956.504	0.000278252794326	1538.977	1548.725	9.748
986.543	0.00018018619740861	1041.395	1044.700	3.305	2983.778	0.000278110196770	1546.564	1555.046	8.482	2983.778	0.000278110196770	1546.564	1555.046	8.482	2983.778	0.000278110196770	1546.564	1555.046	8.482
1002.868	0.000182832464849	1044.362	1049.014	4.652	3006.069	0.000277979234002	1552.762	1562.470	9.709	3006.069	0.000277979234002	1552.762	1562.470	9.709	3006.069	0.000277979234002	1552.762	1562.470	9.709
1033.179	0.000186859902941	1049.965	1052.495	2.530	3033.245	0.000277802516034	1560.314	1570.417	10.103	3033.245	0.000277802516034	1560.314	1570.417	10.103	3033.245	0.000277802516034	1560.314	1570.417	10.103
1061.975	0.00019058883883																		



**Table F.5a: Inhomogeneous Isotropic Case: Forward modelling using  $a$ , and  $b$  estimates obtained from offset VSP times for segment 4 with receiver at 1974 m.**

$a = 1425.43934659450$					$b = 0.853369860705650$					$x = 0$					$x = 1973.923$				
offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)
84.530	0.000018864508023	914.960	935.707	20.747	2011.513	0.000294367466121	1274.747	1269.025	-5.722	2011.513	0.000294367466121	1274.747	1269.025	-5.722	2011.513	0.000294367466121	1274.747	1269.025	-5.722
93.234	0.000020802219123	915.133	935.612	20.479	2038.012	0.000295759812817	1282.566	1276.389	-6.178	2038.012	0.000295759812817	1282.566	1276.389	-6.178	2038.012	0.000295759812817	1282.566	1276.389	-6.178
112.705	0.000025132045942	915.580	936.244	20.664	2058.654	0.000296811394128	1288.683	1281.452	-7.231	2058.654	0.000296811394128	1288.683	1281.452	-7.231	2058.654	0.000296811394128	1288.683	1281.452	-7.231
130.648	0.000029114609078	916.067	936.110	20.043	2089.406	0.000298325331650	1297.833	1291.095	-6.739	2089.406	0.000298325331650	1297.833	1291.095	-6.739	2089.406	0.000298325331650	1297.833	1291.095	-6.739
152.613	0.000033978550086	916.760	937.377	20.618	2113.127	0.000299450968586	1304.923	1297.340	-7.583	2113.127	0.000299450968586	1304.923	1297.340	-7.583	2113.127	0.000299450968586	1304.923	1297.340	-7.583
176.332	0.000039215100961	917.628	938.209	20.581	2137.010	0.000300547932548	1312.088	1304.095	-7.993	2137.010	0.000300547932548	1312.088	1304.095	-7.993	2137.010	0.000300547932548	1312.088	1304.095	-7.993
200.664	0.000044567165685	918.647	939.183	20.535	2162.001	0.000301657398038	1319.613	1308.005	-11.608	2162.001	0.000301657398038	1319.613	1308.005	-11.608	2162.001	0.000301657398038	1319.613	1308.005	-11.608
222.033	0.000049248804581	919.649	940.566	20.917	2190.353	0.000302869557998	1328.183	1318.307	-9.876	2190.353	0.000302869557998	1328.183	1318.307	-9.876	2190.353	0.000302869557998	1328.183	1318.307	-9.876
244.406	0.000054129852080	920.806	941.458	20.652	2208.538	0.000303621488930	1333.698	1324.103	-9.595	2208.538	0.000303621488930	1333.698	1324.103	-9.595	2208.538	0.000303621488930	1333.698	1324.103	-9.595
270.447	0.000059781881043	922.289	942.481	20.192	2240.131	0.000304881274748	1343.310	1332.692	-10.618	2240.131	0.000304881274748	1343.310	1332.692	-10.618	2240.131	0.000304881274748	1343.310	1332.692	-10.618
293.032	0.000064656112610	923.694	944.033	20.338	2262.848	0.000305751382153	1350.246	1340.505	-9.741	2262.848	0.000305751382153	1350.246	1340.505	-9.741	2262.848	0.000305751382153	1350.246	1340.505	-9.741
317.805	0.000069970691303	925.362	945.562	20.200	2285.069	0.000306574098918	1357.049	1346.629	-10.421	2285.069	0.000306574098918	1357.049	1346.629	-10.421	2285.069	0.000306574098918	1357.049	1346.629	-10.421
343.415	0.000075427032321	927.224	947.720	20.496	2313.522	0.000307587372938	1365.787	1354.231	-11.556	2313.522	0.000307587372938	1365.787	1354.231	-11.556	2313.522	0.000307587372938	1365.787	1354.231	-11.556
369.719	0.000080988528352	929.281	949.464	20.183	2338.818	0.000308451118525	1373.579	1361.689	-11.890	2338.818	0.000308451118525	1373.579	1361.689	-11.890	2338.818	0.000308451118525	1373.579	1361.689	-11.890
393.092	0.000085891830139	931.232	952.038	20.807	2364.031	0.000309278021622	1381.366	1368.898	-12.468	2364.031	0.000309278021622	1381.366	1368.898	-12.468	2364.031	0.000309278021622	1381.366	1368.898	-12.468
417.457	0.000090962356139	933.386	953.379	19.992	2387.757	0.000310025788105	1388.713	1376.166	-12.546	2387.757	0.000310025788105	1388.713	1376.166	-12.546	2387.757	0.000310025788105	1388.713	1376.166	-12.546
443.392	0.000096312054229	935.815	956.346	20.531	2414.140	0.000310823407643	1396.903	1384.134	-12.769	2414.140	0.000310823407643	1396.903	1384.134	-12.769	2414.140	0.000310823407643	1396.903	1384.134	-12.769
465.151	0.000100760171659	937.959	958.015	20.056	2438.493	0.000311528651305	1404.481	1389.482	-14.999	2438.493	0.000311528651305	1404.481	1389.482	-14.999	2438.493	0.000311528651305	1404.481	1389.482	-14.999
493.184	0.000106435314073	940.863	960.078	19.215	2462.794	0.000312203320240	1412.060	1396.500	-15.560	2462.794	0.000312203320240	1412.060	1396.500	-15.560	2462.794	0.000312203320240	1412.060	1396.500	-15.560
515.711	0.000110948334028	943.312	963.346	20.034	2487.398	0.000312857414637	1419.749	1404.673	-15.077	2487.398	0.000312857414637	1419.749	1404.673	-15.077	2487.398	0.000312857414637	1419.749	1404.673	-15.077
541.511	0.000116063584573	946.240	965.572	19.331	2515.010	0.000313557492972	1428.397	1412.021	-16.376	2515.010	0.000313557492972	1428.397	1412.021	-16.376	2515.010	0.000313557492972	1428.397	1412.021	-16.376
566.218	0.000120906637628	949.168	968.150	18.982	2538.668	0.000314129362439	1435.823	1420.411	-15.412	2538.668	0.000314129362439	1435.823	1420.411	-15.412	2538.668	0.000314129362439	1435.823	1420.411	-15.412
594.084	0.000126301998337	952.612	971.846	19.234	2561.908	0.000314666487247	1443.129	1425.506	-17.623	2561.908	0.000314666487247	1443.129	1425.506	-17.623	2561.908	0.000314666487247	1443.129	1425.506	-17.623
616.525	0.000130593850834	955.495	974.437	18.942	2586.946	0.000315218430762	1451.015	1432.678	-18.337	2586.946	0.000315218430762	1451.015	1432.678	-18.337	2586.946	0.000315218430762	1451.015	1432.678	-18.337
640.390	0.000135105099198	958.666	977.709	19.043	2611.466	0.000315732621618	1458.750	1439.409	-19.342	2611.466	0.000315732621618	1458.750	1439.409	-19.342	2611.466	0.000315732621618	1458.750	1439.409	-19.342
666.096	0.000139901465396	962.200	980.848	18.647	2634.472	0.000316191842139	1466.019	1447.930	-18.089	2634.472	0.000316191842139	1466.019	1447.930	-18.089	2634.472	0.000316191842139	1466.019	1447.930	-18.089
686.674	0.000143693647688	965.118	983.892	18.773	2664.740	0.000316762546889	1475.599	1457.009	-18.589	2664.740	0.000316762546889	1475.599	1457.009	-18.589	2664.740	0.000316762546889	1475.599	1457.009	-18.589
714.131	0.000148686048953	969.132	987.625	18.492	2693.145	0.000317264345332	1484.604	1465.913	-18.691	2693.145	0.000317264345332	1484.604	1465.913	-18.691	2693.145	0.000317264345332	1484.604	1465.913	-18.691
734.065	0.000152261755518	972.132	990.735	18.603	2713.475	0.000317603850216	1491.057	1471.688	-19.369	2713.475	0.000317603850216	1491.057	1471.688	-19.369	2713.475	0.000317603850216	1491.057	1471.688	-19.369
763.765	0.0001575112041203	976.732	994.462	17.729	2737.504	0.000317984436441	1498.693	1478.316	-20.377	2737.504	0.000317984436441	1498.693	1478.316	-20.377	2737.504	0.000317984436441	1498.693	1478.316	-20.377
790.341	0.000162130479224	980.980	998.943	17.962	2763.498	0.000318371440441	1506.964	1486.156	-20.808	2763.498	0.000318371440441	1506.964	1486.156	-20.808	2763.498	0.000318371440441	1506.964	1486.156	-20.808
818.537	0.000166947431300	985.620	1002.359	16.739	2790.900	0.000318752219733	1515.693	1492.776	-22.917	2790.900	0.000318752219733	1515.693	1492.776	-22.917	2790.900	0.000318752219733	1515.693	1492.776	-22.917
838.613	0.00017032443154	989.005	1006.107	17.101	2818.515	0.000319108390521	1524.501	1501.544	-22.957	2818.515	0.000319108390521	1524.501	1501.544	-22.957	2818.515	0.000319108390521	1524.501	1501.544	-22.957
864.183	0.000174561596796	993.415	1009.904	16.489	2840.130	0.000319368298854	1531.401	1509.010	-22.392	2840.130	0.000319368298854	1531.401	1509.010	-22.392	2840.130	0.000319368298854	1531.401	1509.010	-22.392
889.644	0.000178709184991	997.912	1015.459	17.547	2867.558	0.000319674760786	1540.165	1516.612	-23.553	2867.558	0.000319674760786	1540.165	1516.612	-23.553	2867.558	0.000319674760786	1540.165	1516.612	-23.553
916.870	0.000183064643530	1002.837	1018.333	15.496	2891.097	0.000319917403190	1547.692	1522.475	-25.218	2891.097	0.000319917403190	1547.692	1522.475	-25.218	2891.097	0.000319917403190	1547.692	1522.475	-25.218
938.114	0.000186405660243	1006.762	1022.636	15.874	2913.083	0.000320127414863	1554.729	1527.969	-26.760	2913.083	0.000320127414863	1554.729	1527.969	-26.760	2913.083	0.000320127414863	1554.729	1527.969	-26.760
967.871	0.00019100931004	1012.377	1028.093	15.716	2936.480	0.000320333615615	1562.221	1537.739	-24.482	2936.480	0.000320333615615	1562.221	1537.739	-24.482	2936.480	0.000320333615615	1562.221	1537.739	-24.482
984.094	0.000193464276457	1015.496	1032.088	16.592	2963.685	0.000320551457522	1570.939	1544.497	-26.442	2963.685	0.000320551457522	1570.939	1544.497	-26.442	2963.685	0.000320551457522	1570.939	1544.497	-26.442
1014.404	0.0001977723294	1021.429	1035.925	14.496	2985.984	0.000320712801999	1578.089	1551.710	-26.378	2985.984	0.000320712801999	1578.089	1551.710	-26.378	2985.984	0.000320712801999	1578.089	1551.710	-26.378
1043.220	0.000202192793448	1027.195	1041.995	14.800	3013.154	0.000320888924966	1586.805	1560.112	-26.693	3013.154	0.000320888924966	1586.805	1560.11						



**Table F.5b: Inhomogeneous Isotropic Case: Forward modelling using  $a$ , and  $b$  estimates obtained from offset VSP times for segment 4 with receiver at 2014 m.**

$a = 1425.439346594540$					$b = 0.853369860706$					$z = 0$					$x = 2013.927$				
offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)
47.917	0.000010410433917	927.205	949.852	22.647	2031.400	0.000290613328763	1285.738	1283.866	-1.872	2031.400	0.000290613328763	1285.738	1283.866	-1.872	2031.400	0.000290613328763	1285.738	1283.866	-1.872
67.679	0.000014699207540	927.453	950.437	22.984	2057.867	0.000291990415347	1293.448	1290.939	-2.509	2057.867	0.000291990415347	1293.448	1290.939	-2.509	2057.867	0.000291990415347	1293.448	1290.939	-2.509
87.531	0.000019002481816	927.788	950.647	22.859	2078.568	0.000293035323724	1299.503	1296.333	-3.170	2078.568	0.000293035323724	1299.503	1296.333	-3.170	2078.568	0.000293035323724	1299.503	1296.333	-3.170
114.917	0.000024928374583	928.389	951.544	23.154	2109.336	0.000294537226947	1308.542	1305.118	-3.425	2109.336	0.000294537226947	1308.542	1305.118	-3.425	2109.336	0.000294537226947	1308.542	1305.118	-3.425
136.226	0.000029528714363	928.970	951.374	22.404	2133.030	0.000295652851243	1315.535	1311.261	-4.274	2133.030	0.000295652851243	1315.535	1311.261	-4.274	2133.030	0.000295652851243	1315.535	1311.261	-4.274
159.548	0.000034550739504	929.717	953.025	23.308	2156.926	0.000296742627665	1322.613	1317.697	-4.916	2156.926	0.000296742627665	1322.613	1317.697	-4.916	2156.926	0.000296742627665	1322.613	1317.697	-4.916
185.804	0.000040185614222	930.698	953.865	23.167	2181.962	0.000297846948076	1330.055	1322.426	-7.630	2181.962	0.000297846948076	1330.055	1322.426	-7.630	2181.962	0.000297846948076	1330.055	1322.426	-7.630
210.975	0.000045566105947	931.777	954.950	23.173	2210.257	0.000299049885862	1338.500	1332.953	-5.547	2210.257	0.000299049885862	1338.500	1332.953	-5.547	2210.257	0.000299049885862	1338.500	1332.953	-5.547
234.325	0.000050535923015	932.899	956.605	23.705	2228.452	0.000299798591567	1343.948	1338.401	-5.547	2228.452	0.000299798591567	1343.948	1338.401	-5.547	2228.452	0.000299798591567	1343.948	1338.401	-5.547
258.040	0.000055602832222	934.158	957.373	23.215	2260.084	0.000301054787022	1353.452	1346.712	-6.739	2260.084	0.000301054787022	1353.452	1346.712	-6.739	2260.084	0.000301054787022	1353.452	1346.712	-6.739
284.557	0.000061147958592	935.705	958.386	22.681	2282.716	0.000301918879419	1360.275	1353.271	-7.004	2282.716	0.000301918879419	1360.275	1353.271	-7.004	2282.716	0.000301918879419	1360.275	1353.271	-7.004
307.433	0.000065940377086	937.159	960.111	22.952	2304.890	0.000302737978647	1366.979	1359.676	-7.303	2304.890	0.000302737978647	1366.979	1359.676	-7.303	2304.890	0.000302737978647	1366.979	1359.676	-7.303
332.872	0.000071236873466	938.904	961.630	22.726	2333.394	0.000303751638532	1375.623	1367.060	-8.563	2333.394	0.000303751638532	1375.623	1367.060	-8.563	2333.394	0.000303751638532	1375.623	1367.060	-8.563
359.049	0.000076648344440	940.839	963.944	23.104	2358.739	0.000304616616821	1383.332	1375.373	-7.959	2358.739	0.000304616616821	1383.332	1375.373	-7.959	2358.739	0.000304616616821	1383.332	1375.373	-7.959
385.343	0.000082041766424	942.926	965.418	22.492	2383.962	0.000305444222095	1391.026	1382.318	-8.708	2383.962	0.000305444222095	1391.026	1382.318	-8.708	2383.962	0.000305444222095	1391.026	1382.318	-8.708
409.334	0.000086924026567	944.953	968.447	23.495	2407.702	0.000306193480773	1398.286	1389.120	-9.167	2407.702	0.000306193480773	1398.286	1389.120	-9.167	2407.702	0.000306193480773	1398.286	1389.120	-9.167
433.705	0.00009183417036	947.131	969.921	22.790	2434.097	0.000306993403767	1406.379	1396.500	-9.879	2434.097	0.000306993403767	1406.379	1396.500	-9.879	2434.097	0.000306993403767	1406.379	1396.500	-9.879
460.001	0.000097103759853	949.615	972.838	23.223	2458.515	0.000307702959098	1413.884	1403.233	-10.651	2458.515	0.000307702959098	1413.884	1403.233	-10.651	2458.515	0.000307702959098	1413.884	1403.233	-10.651
482.029	0.000101470859992	951.803	974.457	22.654	2482.797	0.000308390058144	1421.362	1410.509	-10.853	2482.797	0.000308390058144	1421.362	1410.509	-10.853	2482.797	0.000308390058144	1421.362	1410.509	-10.853
509.907	0.000106943859793	954.708	976.609	21.902	2507.442	0.000309039105363	1428.972	1418.106	-10.866	2507.442	0.000309039105363	1428.972	1418.106	-10.866	2507.442	0.000309039105363	1428.972	1418.106	-10.866
532.777	0.000111386988901	957.204	979.967	22.762	2535.041	0.000309743774462	1437.511	1425.056	-12.455	2535.041	0.000309743774462	1437.511	1425.056	-12.455	2535.041	0.000309743774462	1437.511	1425.056	-12.455
558.748	0.000116380221290	960.162	981.933	21.771	2558.701	0.000310320494083	1444.846	1432.211	-12.635	2558.701	0.000310320494083	1444.846	1432.211	-12.635	2558.701	0.000310320494083	1444.846	1432.211	-12.635
583.493	0.000121083976409	963.100	985.107	22.006	2581.986	0.000310863890483	1452.078	1439.055	-13.023	2581.986	0.000310863890483	1452.078	1439.055	-13.023	2581.986	0.000310863890483	1452.078	1439.055	-13.023
611.554	0.00012652802555	966.572	988.531	21.959	2607.071	0.000311422994028	1459.884	1445.480	-14.404	2607.071	0.000311422994028	1459.884	1445.480	-14.404	2607.071	0.000311422994028	1459.884	1445.480	-14.404
634.129	0.000130539884165	969.472	991.086	21.613	2631.588	0.000311943613072	1467.525	1452.599	-14.926	2631.588	0.000311943613072	1467.525	1452.599	-14.926	2631.588	0.000311943613072	1467.525	1452.599	-14.926
658.248	0.000134961405799	972.674	994.422	21.748	2654.653	0.000312410562416	1474.726	1459.835	-14.891	2654.653	0.000312410562416	1474.726	1459.835	-14.891	2654.653	0.000312410562416	1474.726	1459.835	-14.891
684.072	0.000139634633405	976.220	997.434	21.215	2684.768	0.000312987626710	1484.143	1469.199	-14.944	2684.768	0.000312987626710	1484.143	1469.199	-14.944	2684.768	0.000312987626710	1484.143	1469.199	-14.944
705.124	0.000143396908364	979.199	1000.876	21.677	2713.012	0.000313496047300	1492.990	1477.709	-15.280	2713.012	0.000313496047300	1492.990	1477.709	-15.280	2713.012	0.000313496047300	1492.990	1477.709	-15.280
732.526	0.000148228991585	983.195	1004.018	20.824	2733.279	0.000313841757411	1499.347	1482.503	-16.844	2733.279	0.000313841757411	1499.347	1482.503	-16.844	2733.279	0.000313841757411	1499.347	1482.503	-16.844
752.696	0.000151738378121	986.220	1007.432	21.212	2757.260	0.000314230590008	1506.878	1489.196	-17.681	2757.260	0.000314230590008	1506.878	1489.196	-17.681	2757.260	0.000314230590008	1506.878	1489.196	-17.681
782.323	0.00015681896065	990.791	1011.254	20.463	2783.262	0.000314627921255	1515.054	1497.292	-17.762	2783.262	0.000314627921255	1515.054	1497.292	-17.762	2783.262	0.000314627921255	1515.054	1497.292	-17.762
809.041	0.000161324001542	995.041	1015.565	20.524	2810.670	0.000315019997955	1523.682	1504.319	-19.364	2810.670	0.000315019997955	1523.682	1504.319	-19.364	2810.670	0.000315019997955	1523.682	1504.319	-19.364
837.034	0.000165965164487	999.622	1019.073	19.451	2838.309	0.000315388230155	1532.394	1512.353	-20.041	2838.309	0.000315388230155	1532.394	1512.353	-20.041	2838.309	0.000315388230155	1532.394	1512.353	-20.041
857.170	0.000169253144013	1002.997	1022.852	19.855	2859.972	0.000315658211853	1539.230	1519.220	-20.010	2859.972	0.000315658211853	1539.230	1519.220	-20.010	2859.972	0.000315658211853	1539.230	1519.220	-20.010
882.753	0.000173369259218	1007.380	1026.294	18.914	2887.458	0.000315977684310	1547.910	1526.834	-21.076	2887.458	0.000315977684310	1547.910	1526.834	-21.076	2887.458	0.000315977684310	1547.910	1526.834	-21.076
908.363	0.000177420679461	1011.872	1031.885	20.013	2911.043	0.000316231695260	1555.366	1534.916	-20.450	2911.043	0.000316231695260	1555.366	1534.916	-20.450	2911.043	0.000316231695260	1555.366	1534.916	-20.450
935.422	0.000181625528743	1016.730	1034.363	17.633	2933.070	0.000316452477058	1562.334	1540.726	-21.608	2933.070	0.000316452477058	1562.334	1540.726	-21.608	2933.070	0.000316452477058	1562.334	1540.726	-21.608
956.725	0.000184881146646	1020.634	1038.713	18.079	2956.504	0.000316670287806	1569.752	1548.725	-21.027	2956.504	0.000316670287806	1569.752	1548.725	-21.027	2956.504	0.000316670287806	1569.752	1548.725	-21.027
986.543	0.000189356590958	1026.214	1044.700	18.486	2983.778	0.000316902082238	1578.392	1555.046	-23.346	2983.778	0.000316902082238	1578.392	1555.046	-23.346	2983.778	0.000316902082238	1578.392	1555.046	-23.346
1002.868	0.000191766461690	1029.325	1049.014	19.689	3006.069	0.000317074546371	1585.458	1562.470	-22.988	3006.069	0.000317074546371	1585.458	1562.470	-22.988	3006.069	0.000317074546371	1585.458	1562.470	-22.988
1033.179	0.000196165032363	1035.204	1052.495	17.290	3033.245	0.000317264622841	1594.078	1570.417	-23.661	3033.245	0.000317264622841	1594.078	1570.417	-23.661	303				



**Table F.6a: Inhomogeneous Anisotropic Case: Forward modelling using  $\alpha$ ,  $b$  and  $\chi$  estimates obtained from offset VSP times for segment 1 with receiver at 1974 m.**

$\alpha = 1684.101561548270$					$b = 0.466527250379$					$\chi = 0.052892411471$					$z = 1973.923$				
offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)
84.530	0.000018042557228	935.749	935.707	-0.042	2011.513	0.000302122566926	1292.655	1269.025	-23.630	2011.513	0.000302122566926	1292.655	1269.025	-23.630	2011.513	0.000302122566926	1292.655	1269.025	-23.630
93.234	0.000019896596324	935.915	935.612	-0.302	2038.012	0.000303988352806	1300.686	1276.389	-24.297	2038.012	0.000303988352806	1300.686	1276.389	-24.297	2038.012	0.000303988352806	1300.686	1276.389	-24.297
112.705	0.000024040291855	936.342	936.244	-0.098	2058.654	0.000305412175872	1306.975	1281.452	-25.524	2058.654	0.000305412175872	1306.975	1281.452	-25.524	2058.654	0.000305412175872	1306.975	1281.452	-25.524
130.648	0.000027852832880	936.808	936.110	-0.698	2089.406	0.000307486016395	1316.399	1291.095	-25.305	2089.406	0.000307486016395	1316.399	1291.095	-25.305	2089.406	0.000307486016395	1316.399	1291.095	-25.305
152.613	0.000032510933807	937.471	937.377	-0.094	2113.127	0.000309047783220	1323.712	1297.340	-26.372	2113.127	0.000309047783220	1323.712	1297.340	-26.372	2113.127	0.000309047783220	1323.712	1297.340	-26.372
176.332	0.000037528464206	938.302	938.209	-0.093	2137.010	0.000310587437044	1331.111	1304.095	-27.016	2137.010	0.000310587437044	1331.111	1304.095	-27.016	2137.010	0.000310587437044	1331.111	1304.095	-27.016
200.664	0.000042659883281	939.277	939.183	-0.095	2162.001	0.000312163809163	1338.893	1308.005	-30.888	2162.001	0.000312163809163	1338.893	1308.005	-30.888	2162.001	0.000312163809163	1338.893	1308.005	-30.888
222.033	0.000047151532857	940.237	940.566	0.330	2190.353	0.000313910066289	1347.768	1318.307	-29.461	2190.353	0.000313910066289	1347.768	1318.307	-29.461	2190.353	0.000313910066289	1347.768	1318.307	-29.461
244.406	0.000051837851093	941.344	941.458	0.114	2208.538	0.000315006929916	1353.487	1324.103	-29.384	2208.538	0.000315006929916	1353.487	1324.103	-29.384	2208.538	0.000315006929916	1353.487	1324.103	-29.384
270.447	0.000057269137741	942.765	942.481	-0.283	2240.131	0.000316870148345	1363.468	1332.692	-30.776	2240.131	0.000316870148345	1363.468	1332.692	-30.776	2240.131	0.000316870148345	1363.468	1332.692	-30.776
293.032	0.000061957511319	944.111	944.033	-0.078	2262.848	0.000318177334382	1370.682	1340.505	-30.177	2262.848	0.000318177334382	1370.682	1340.505	-30.177	2262.848	0.000318177334382	1370.682	1340.505	-30.177
317.805	0.000067074661067	945.710	945.562	-0.148	2285.069	0.000319430020627	1377.766	1346.629	-31.137	2285.069	0.000319430020627	1377.766	1346.629	-31.137	2285.069	0.000319430020627	1377.766	1346.629	-31.137
343.415	0.000072334480667	947.495	947.720	0.225	2313.522	0.000320997217534	1386.877	1354.231	-32.646	2313.522	0.000320997217534	1386.877	1354.231	-32.646	2313.522	0.000320997217534	1386.877	1354.231	-32.646
369.719	0.000077702673340	949.468	949.464	-0.004	2338.818	0.000322356458898	1395.014	1361.689	-33.325	2338.818	0.000322356458898	1395.014	1361.689	-33.325	2338.818	0.000322356458898	1395.014	1361.689	-33.325
393.092	0.000082441892707	951.340	952.038	0.698	2364.031	0.000323679931858	1403.158	1368.898	-34.261	2364.031	0.000323679931858	1403.158	1368.898	-34.261	2364.031	0.000323679931858	1403.158	1368.898	-34.261
417.457	0.000087349659797	953.408	953.379	-0.030	2387.757	0.000324897333905	1410.853	1376.166	-34.686	2387.757	0.000324897333905	1410.853	1376.166	-34.686	2387.757	0.000324897333905	1410.853	1376.166	-34.686
443.392	0.000092535185017	955.741	956.346	0.605	2414.140	0.000326219711977	1419.442	1384.134	-35.308	2414.140	0.000326219711977	1419.442	1384.134	-35.308	2414.140	0.000326219711977	1419.442	1384.134	-35.308
465.151	0.000096853586993	957.801	958.015	0.214	2438.493	0.000327411593448	1427.401	1389.482	-37.919	2438.493	0.000327411593448	1427.401	1389.482	-37.919	2438.493	0.000327411593448	1427.401	1389.482	-37.919
493.184	0.000102372562189	960.594	960.078	-0.516	2462.794	0.000328573895356	1435.371	1396.500	-38.872	2462.794	0.000328573895356	1435.371	1396.500	-38.872	2462.794	0.000328573895356	1435.371	1396.500	-38.872
515.711	0.000106769327292	962.950	963.346	0.396	2487.398	0.000329723657779	1443.470	1404.673	-38.797	2487.398	0.000329723657779	1443.470	1404.673	-38.797	2487.398	0.000329723657779	1443.470	1404.673	-38.797
541.511	0.000111761849999	965.769	965.572	-0.197	2515.010	0.000330982215803	1452.591	1412.021	-40.570	2515.010	0.000330982215803	1452.591	1412.021	-40.570	2515.010	0.000330982215803	1452.591	1412.021	-40.570
566.218	0.000116498082625	968.589	968.150	-0.439	2538.668	0.000332034362597	1460.435	1420.411	-40.024	2538.668	0.000332034362597	1460.435	1420.411	-40.024	2538.668	0.000332034362597	1460.435	1420.411	-40.024
594.084	0.000121785846091	971.909	971.846	-0.063	2561.908	0.000333044737206	1468.163	1425.506	-42.657	2561.908	0.000333044737206	1468.163	1425.506	-42.657	2561.908	0.000333044737206	1468.163	1425.506	-42.657
616.525	0.000126001188022	974.689	974.437	-0.253	2586.946	0.000334108093086	1476.515	1432.678	-43.837	2586.946	0.000334108093086	1476.515	1432.678	-43.837	2586.946	0.000334108093086	1476.515	1432.678	-43.837
640.390	0.000130441172486	977.750	977.709	-0.041	2611.466	0.000335124564631	1484.720	1439.409	-45.311	2611.466	0.000335124564631	1484.720	1439.409	-45.311	2611.466	0.000335124564631	1484.720	1439.409	-45.311
666.096	0.000135172613304	981.163	980.848	-0.316	2634.472	0.000336056252287	1492.440	1447.930	-44.510	2634.472	0.000336056252287	1492.440	1447.930	-44.510	2634.472	0.000336056252287	1492.440	1447.930	-44.510
686.674	0.000138921776724	983.984	983.892	-0.092	2664.740	0.000337250210684	1502.630	1457.009	-45.621	2664.740	0.000337250210684	1502.630	1457.009	-45.621	2664.740	0.000337250210684	1502.630	1457.009	-45.621
714.131	0.000143869330328	987.866	987.625	-0.241	2693.145	0.000338338471993	1512.226	1465.913	-46.313	2693.145	0.000338338471993	1512.226	1465.913	-46.313	2693.145	0.000338338471993	1512.226	1465.913	-46.313
734.065	0.000147421545179	990.769	990.735	-0.035	2713.475	0.000339085535581	1519.112	1471.688	-47.424	2713.475	0.000339085535581	1519.112	1471.688	-47.424	2713.475	0.000339085535581	1519.112	1471.688	-47.424
763.765	0.000152651095384	995.226	994.462	-0.764	2737.504	0.000339977052701	1527.270	1478.316	-48.954	2737.504	0.000339977052701	1527.270	1478.316	-48.954	2737.504	0.000339977052701	1527.270	1478.316	-48.954
790.341	0.000157265541020	999.344	998.943	-0.402	2763.498	0.000340903618065	1536.120	1486.156	-49.964	2763.498	0.000340903618065	1536.120	1486.156	-49.964	2763.498	0.000340903618065	1536.120	1486.156	-49.964
818.537	0.000162093364603	1003.847	1002.359	-1.488	2790.900	0.000341854108338	1545.474	1492.776	-52.698	2790.900	0.000341854108338	1545.474	1492.776	-52.698	2790.900	0.000341854108338	1545.474	1492.776	-52.698
838.613	0.000165487609873	1007.135	1006.107	-1.028	2818.515	0.000342785258433	1554.927	1501.544	-53.384	2818.515	0.000342785258433	1554.927	1501.544	-53.384	2818.515	0.000342785258433	1554.927	1501.544	-53.384
864.183	0.000169758189694	1011.421	1009.904	-1.517	2840.130	0.000343495736753	1562.345	1509.010	-53.335	2840.130	0.000343495736753	1562.345	1509.010	-53.335	2840.130	0.000343495736753	1562.345	1509.010	-53.335
889.644	0.000173951796213	1015.797	1015.459	-0.338	2867.558	0.000344374461649	1571.778	1516.612	-55.166	2867.558	0.000344374461649	1571.778	1516.612	-55.166	2867.558	0.000344374461649	1571.778	1516.612	-55.166
916.870	0.000178370500921	1020.593	1018.333	-2.260	2891.097	0.000345108639046	1579.893	1522.475	-57.418	2891.097	0.000345108639046	1579.893	1522.475	-57.418	2891.097	0.000345108639046	1579.893	1522.475	-57.418
938.114	0.000181770908673	1024.419	1022.636	-1.783	2913.083	0.000345778046629	1587.488	1527.969	-59.519	2913.083	0.000345778046629	1587.488	1527.969	-59.519	2913.083	0.000345778046629	1587.488	1527.969	-59.519
967.871	0.000186464103375	1029.898	1028.093	-1.804	2936.480	0.000346473341861	1595.586	1537.739	-57.847	2936.480	0.000346473341861	1595.586	1537.739	-57.847	2936.480	0.000346473341861	1595.586	1537.739	-57.847
984.094	0.000188988032494	1032.943	1032.088	-0.855	2963.685	0.000347260113459	1605.023	1544.497	-60.526	2963.685	0.000347260113459	1605.023	1544.497	-60.526	2963.685	0.000347260113459	1605.023	1544.497	-60.526
1014.404	0.000193638189971	1038.742	1035.925	-2.817	2985.984	0.000347887866741	1612.773	1551.710	-61.063	2985.984	0.000347887866741	1612.773	1551.710	-61.063	2985.984	0.000347887866741	1612.773	1551.710	-61.063
1043.220	0.000197979919863	1044.385	1041.995	-2.390	3013.154	0.000348632334556	1622.236	1560.112	-62.124	3013.154	0.000348632334556	1622							



**Table F.6b:** Inhomogeneous Anisotropic Case: Forward modelling using  $a$ ,  $b$  and  $\chi$  estimates obtained from offset VSP times for segment 1 with receiver at 2014 m.

[illegible]



**Table F.7a: Inhomogeneous Anisotropic Case: Forward modelling using  $a$ ,  $b$  and  $\chi$  estimates obtained from offset VSP times for segment 2 with receiver at 1974 m.**

$a = 1395.795218556840$					$b = 0.824486851129$					$\chi = 0.058662431005$					$z = 1973.923$				
offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)
84.530	0.000017329910318	938.133	935.707	-2.426	2011.513	0.000280040286497	1275.180	1269.025	-6.155										
93.234	0.000019110451367	938.292	935.612	-2.679	2038.012	0.000281516676240	1282.620	1276.389	-6.232										
112.705	0.000023089586999	938.703	936.244	-2.458	2058.654	0.000282635658262	1288.443	1281.452	-6.992										
130.648	0.000026750301196	939.150	936.110	-3.040	2089.406	0.000284252986143	1297.160	1291.095	-6.065										
152.613	0.00003122260499	939.786	937.377	-2.409	2113.127	0.000285460697563	1303.917	1297.340	-6.577										
176.332	0.000036038365385	940.584	938.209	-2.376	2137.010	0.000286642234648	1310.749	1304.095	-6.654										
200.664	0.000040962646667	941.521	939.183	-2.338	2162.001	0.000287842172773	1317.927	1308.005	-9.922										
222.033	0.000045271895604	942.442	940.566	-1.876	2190.353	0.000289159295347	1326.107	1318.307	-7.800										
244.406	0.000049766706703	943.506	941.458	-2.048	2208.538	0.000289979783243	1331.373	1324.103	-7.270										
270.447	0.000054974329102	944.869	942.481	-2.388	2240.131	0.000291360834115	1340.556	1332.692	-7.864										
293.032	0.000059467996324	946.162	944.033	-2.129	2262.848	0.000292319749642	1347.186	1340.505	-6.681										
317.805	0.000064370727998	947.696	945.562	-2.134	2285.069	0.000293230560639	1353.692	1346.629	-7.063										
343.415	0.000069407885206	949.409	947.720	-1.689	2313.522	0.000294358305796	1362.051	1354.231	-7.821										
369.719	0.000074546239407	951.302	949.464	-1.838	2338.818	0.000295325303793	1369.509	1361.689	-7.820										
393.092	0.000079080189968	953.098	952.038	-1.059	2364.031	0.000296256420375	1376.967	1368.898	-8.069										
417.457	0.000083772868389	955.082	953.379	-1.703	2387.757	0.00029710367886	1384.006	1376.166	-7.840										
443.392	0.000088728133628	957.319	956.346	-0.973	2414.140	0.000298012458876	1391.857	1384.134	-7.723										
465.151	0.000092852259782	959.294	958.015	-1.279	2438.493	0.000298821632895	1399.124	1389.482	-9.642										
493.184	0.000098119371242	961.971	960.078	-1.893	2462.794	0.000299600931577	1406.396	1396.500	-9.896										
515.711	0.000102312420257	964.229	963.346	-0.883	2487.398	0.000300361832049	1413.776	1404.673	-9.104										
541.511	0.000107070099529	966.930	965.572	-1.358	2515.010	0.000301182741805	1422.081	1412.021	-10.060										
566.218	0.000111579857579	969.631	968.150	-1.481	2538.668	0.000301858895275	1429.215	1420.411	-8.804										
594.084	0.000116610246374	972.811	971.846	-0.964	2561.908	0.000302499078695	1436.237	1425.506	-10.732										
616.525	0.000120616774927	975.472	974.437	-1.036	2586.946	0.000303162690252	1443.820	1432.678	-11.142										
640.390	0.000124831115341	978.401	977.709	-0.693	2611.466	0.000303786822369	1451.261	1439.409	-11.852										
666.096	0.000129321806774	981.668	980.848	-0.821	2634.472	0.000304349670425	1458.257	1447.930	-10.326										
686.674	0.000132875194322	984.366	983.892	-0.474	2664.740	0.000305057345433	1467.479	1457.009	-10.470										
714.131	0.00013759493681	988.079	987.625	-0.454	2693.145	0.000305688264684	1476.154	1465.913	-10.241										
734.065	0.000140919079624	990.854	990.735	-0.119	2713.475	0.000306120484055	1482.373	1471.688	-10.685										
763.765	0.000145859212564	995.113	994.462	-0.651	2737.504	0.000306610936597	1489.734	1478.316	-11.418										
790.341	0.000150212183263	999.048	998.943	-0.105	2763.498	0.000307117098271	1497.711	1486.156	-11.555										
818.537	0.000154759932287	1003.347	1002.359	-0.988	2790.900	0.000307623778817	1506.133	1492.776	-13.357										
838.613	0.00015795363371	1006.486	1006.107	-0.380	2818.515	0.000308107074099	1514.635	1501.544	-13.092										
864.183	0.000161965405648	1010.577	1009.904	-0.673	2840.130	0.0003088466624382	1521.299	1509.010	-12.290										
889.644	0.000165895900085	1014.751	1015.459	0.708	2867.558	0.000308899645341	1529.766	1516.612	-13.154										
916.870	0.000170038047132	1019.324	1018.333	-0.991	2891.097	0.0003093250982640	1537.041	1522.475	-14.566										
938.114	0.000173217919485	1022.970	1022.636	-0.334	2913.083	0.000309562558801	1543.844	1527.969	-15.875										
967.871	0.000177599283121	1028.190	1028.093	-0.097	2936.480	0.000309876851949	1551.090	1537.739	-13.351										
984.094	0.000179951771702	1031.090	1032.088	0.998	2963.685	0.000310220364141	1559.525	1544.497	-15.029										
1014.404	0.000184278840546	1036.610	1035.925	-0.686	2985.984	0.000310484667314	1566.446	1551.710	-14.736										
1043.220	0.000188310014723	1041.979	1041.995	0.016	3013.154	0.000310786155472	1574.886	1560.112	-14.774										
1065.184	0.000191328210329	1046.148	1046.384	0.236	3037.280	0.00031035325070	1582.387	1566.471	-15.916										
1088.895	0.000194531998826	1050.723	1050.471	-0.252	3062.143	0.000311274236486	1590.123	1575.806	-14.317										
1115.015	0.000198002098427	1055.849	1055.210	-0.640	3087.867	0.000311502728359	1598.133	1582.710	-15.424										
1140.098	0.000201270282873	1060.857	1060.235	-0.622	3113.355	0.000311710766688	1606.076	1587.800	-18.275										
1165.295	0.000204491867701	1065.969	1065.256	-0.713	3137.870	0.000311893985178	1613.719	1597.852	-15.868										
1187.085	0.0002072072846087	1070.455	1070.389	-0.066	3163.910	0.000312070859714	1621.843	1605.218	-16.625										
1214.352	0.000210588523019	1076.151	1075.694	-0.458	3187.722	0.000312216938835	1629.276	1614.170	-15.106										
1238.248	0.000213474756061	1081.218	1080.502	-0.717	3214.578	0.000312364124515	1637.663	1620.041	-17.622										
1262.578	0.000216257366083	1086.447	1085.769	-0.678	3236.351	0.000312470058344	1644.466	1627.195	-17.270										
1288.093	0.000219320101677	1092.006	1092.119	0.113	3259.675	0.000312570500589	1651.755	1634.435	-17.320										
1312.260	0.000222069775452	1097.339	1097.591	0.251	3288.287	0.000312675688636	1660.700	1643.422	-15.278										
1337.566	0.000224890507786	1102.995	1102.887	-0.108	3312.831	0.000312750429104	1668.375	1651.273	-17.101										
1366.579	0.000228051260168	1109.565	1110.075	0.510	3338.804	0.000312814296361	1676.499	1660.710	-15.788										
1386.806	0.000230208993971	1114.200	1113.877	-0.323	3361.215	0.000312857079956	1683.510	1665.429	-18.081										
1413.235	0.000232972138081	1120.321	1120.171	-0.150	3387.640	0.000312893174513	1691.778	1674.863	-16.915										
1434.249	0.000235124029618	1125.239	1125.078	-0.162	3405.836	0.000312909170843	1697.471	1681.033	-16.438										
1457.820	0.000237490678202	1130.810	1129.865	-0.945	3438.279	0.000312920165957	1707.623	1690.683	-16.940										
1485.368	0.000240194003045	1137.389	1136.798	-0.591	3462.882	0.000312913854587	1715.322	1698.660	-16.662										
1513.211	0.000242858647825	1144.114	1143.508	-0.607	3488.647	0.000312894022020	1723.384	1706.745	-16.639										
1539.303	0.000245294562174	1150.483	1149.417	-1.066	3512.857	0.000312863325031	1730.958	1712.753	-18.206										
1565.130	0.000247648256507	1156.849	1154.933	-1.916	3539.715	0.000312815900984	1739.361	1720.417	-18.944										
1588.644	0.000249741966588	1162.696	1160.874	-1.822	3562.825	0.000312764079935	1746.589	1742.573	-4.017										
1612.475	0.000251816713427	1168.673</																	



**Table F.7b: Inhomogeneous Anisotropic Case: Forward modelling using  $a$ ,  $b$  and  $\chi$  estimates obtained from offset VSP times for segment 2 with receiver at 2014 m.**

$a = 1395.795218556840$					$b = 0.824486851129$					$\chi = 0.058662431005$					$z = 2013.927$				
offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)
47.917	0.000009563428875	950.790	949.852	-0.938	2031.400	0.000276414586196	1286.611	1283.866	-2.745										
67.679	0.000013503726036	951.018	950.437	-0.581	2057.867	0.00027872705905	1293.946	1290.939	-3.008										
87.531	0.000017457823207	951.325	950.647	-0.678	2078.568	0.000278982912614	1299.710	1296.333	-3.377										
114.917	0.000022903917748	951.878	951.544	-0.334	2109.336	0.000280584833493	1308.319	1305.118	-3.201										
136.226	0.000027132828561	952.411	951.374	-1.037	2133.030	0.000281779776954	1314.981	1311.261	-3.720										
159.548	0.000031750642524	953.098	953.025	-0.073	2156.926	0.000282951473938	1321.729	1317.697	-4.032										
185.804	0.000036933823471	953.999	953.865	-0.134	2181.962	0.000284143594306	1328.827	1322.426	-6.402										
210.975	0.000041885118145	954.991	954.950	-0.041	2210.257	0.000285448071070	1336.886	1332.953	-3.933										
234.325	0.000046460572982	956.023	956.605	0.582	2228.452	0.000286263302953	1342.087	1338.401	-3.686										
258.040	0.000051088504470	957.180	957.373	0.193	2260.084	0.000287637318376	1351.164	1346.712	-4.452										
284.557	0.000056238259886	958.603	958.386	-0.217	2282.716	0.000288587312011	1357.685	1353.271	-4.413										
307.433	0.000060657802210	959.940	960.111	0.171	2304.890	0.000289491799270	1364.094	1359.676	-4.418										
332.872	0.000065545385309	961.545	961.630	0.085	2333.394	0.000290616902514	1372.362	1367.060	-5.302										
359.049	0.000070542804574	963.326	963.944	0.617	2358.739	0.000291582469641	1379.739	1375.573	-4.167										
385.343	0.000075527619010	965.247	965.418	0.171	2383.962	0.000292511496534	1387.106	1382.318	-4.788										
409.334	0.000080043754202	967.113	968.447	1.334	2407.702	0.000293357339911	1394.060	1389.120	-4.941										
433.705	0.000084598091112	969.119	969.921	0.801	2434.097	0.000294265849624	1401.816	1396.500	-5.315										
460.001	0.000089472636133	971.408	972.838	1.430	2458.515	0.000295076910246	1409.011	1403.233	-5.778										
482.029	0.000093523239632	973.424	974.457	1.033	2482.793	0.000295855874083	1416.184	1410.509	-5.675										
509.907	0.000098604737663	976.102	976.609	0.507	2507.442	0.000296619236809	1423.486	1418.106	-5.380										
532.777	0.000102734469947	978.404	979.967	1.563	2535.041	0.000297441697078	1431.684	1425.056	-6.628										
558.748	0.000107380506656	981.133	981.933	0.800	2558.701	0.000298120169548	1438.730	1432.211	-6.518										
583.493	0.000111762281830	983.844	985.107	1.262	2581.986	0.000298764347649	1445.679	1439.055	-6.624										
611.554	0.000116676614480	987.050	988.531	1.481	2607.071	0.000299432682684	1453.182	1445.480	-7.702										
634.129	0.000120586854456	989.728	991.086	1.358	2631.588	0.000300060666974	1460.531	1452.599	-7.932										
658.248	0.000124720933387	992.686	994.422	1.736	2654.653	0.000300629123804	1467.458	1459.835	-7.624										
684.072	0.000129096064939	995.964	997.434	1.471	2684.768	0.000301339380646	1476.522	1469.199	-7.324										
705.124	0.000132622793294	998.718	1000.876	2.158	2713.012	0.000301973325349	1485.042	1477.709	-7.333										
732.526	0.000137158411645	1002.415	1004.018	1.604	2733.279	0.000302409431858	1491.167	1482.503	-8.664										
752.696	0.000140456921246	1005.215	1007.432	2.218	2757.260	0.000302905532230	1498.425	1489.196	-9.229										
782.323	0.000145239109564	1009.447	1011.254	1.807	2783.262	0.000303419505718	1506.308	1497.292	-9.016										
809.041	0.000149486662820	1013.384	1015.565	2.181	2810.670	0.000303934854832	1514.631	1504.319	-10.313										
837.034	0.000153869859046	1017.631	1019.073	1.443	2838.309	0.000304427679220	1523.038	1512.353	-10.685										
857.170	0.000156979714771	1020.760	1022.852	2.092	2859.972	0.000304795478950	1529.638	1519.220	-10.418										
882.753	0.000160878542810	1024.826	1026.294	1.468	2887.458	0.000305239216528	1538.021	1526.834	-11.187										
908.363	0.000164722428873	1028.996	1031.885	2.889	2911.043	0.000305599969237	1545.225	1534.916	-10.309										
935.422	0.000168718817825	1033.507	1034.363	0.856	2933.070	0.000305920498660	1551.960	1540.726	-11.234										
956.725	0.000171818064664	1037.134	1038.713	1.579	2956.504	0.000306244470788	1559.132	1548.725	-10.407										
986.543	0.000176085991771	1042.322	1044.700	2.378	2983.778	0.000306599837212	1567.490	1555.046	-12.444										
1002.868	0.000178387809907	1045.215	1049.014	3.799	3006.069	0.000306873275951	1574.327	1562.470	-11.857										
1033.179	0.00018259066268	1050.686	1052.495	1.809	3033.245	0.000307186406052	1582.671	1570.417	-12.255										
1061.975	0.000186515101414	1056.001	1058.421	2.420	3057.374	0.000307446163088	1590.087	1578.054	-12.032										
1084.068	0.000189469542222	1060.154	1062.677	2.523	3082.250	0.000307696322724	1597.737	1585.655	-12.083										
1107.805	0.000192593240990	1064.689	1066.960	2.272	3107.982	0.000307936665325	1605.658	1593.522	-12.137										
1133.931	0.000195970807571	1069.765	1071.377	1.612	3133.483	0.000308156718937	1613.514	1600.080	-13.434										
1159.036	0.000199156598290	1074.725	1076.518	1.793	3158.005	0.000308351673394	1621.073	1608.654	-12.419										
1184.402	0.000202316131063	1079.816	1081.816	2.000	3184.048	0.0003085411208431	1629.106	1615.445	-13.661										
1206.284	0.000204994087625	1084.273	1087.232	2.959	3207.868	0.000308699092987	1636.457	1623.756	-12.701										
1233.606	0.000208275784224	1089.919	1092.486	2.567	3234.734	0.000308859808290	1644.753	1630.595	-14.158										
1257.536	0.000211093806210	1094.937	1096.881	1.944	3256.536	0.000308976966888	1651.488	1639.147	-12.341										
1281.929	0.000213912602179	1100.120	1102.535	2.414	3279.827	0.000309089267394	1658.686	1646.444	-12.241										
1307.463	0.000216805316419	1105.620	1108.661	3.041	3308.451	0.000309209460966	1667.535	1654.579	-12.956										
1331.536	0.000219478655420	1110.871	1113.833	2.962	3333.029	0.000309297308945	1675.136	1662.212	-12.924										
1356.935	0.00022243034967	1116.481	1119.047	2.566	3358.978	0.000309375007293	1683.163	1669.892	-13.271										
1386.199	0.000225356739309	1123.030	1125.490	2.460	3381.389	0.000309429920568	1690.097	1674.585	-15.511										
1406.463	0.000227468678214	1127.618	1130.003	2.385	3407.830	0.000309480487467	1698.279	1683.330	-14.949										
1432.981	0.000230177971268	1133.686	1136.112	2.425	3426.021	0.000309506506520	1703.909	1689.103	-14.806										
1453.941	0.00023276315511	1138.533	1141.041	2.508	3458.467	0.000309535549448	1713.952	1699.251	-14.701										
1477.524	0.000234591932334	1144.038	1145.902	1.864	3483.057	0.000309543052571	1721.563	1707.174	-14.389										
1504.896	0.00023720247642	1150.496	1152.406	1.910	3508.829	0.000309537805639	1729.541	1714.270	-15.270										
1532.702	0.000239825386588	1157.128	1159.518	2.390	3533.031	0.000309520919398	1737.032	1721.476	-15.557										
1558.966	0.000242268893863	1163.458	1164.752	1.293	3559.898	0.000309488905012	1745.348	1730.402	-14.946										
1584.736	0.000244528000946	1169.730	1170.728	0.998	3583.016	0.000309450419191	1752.502	1738.836	-13.666										
1608.206	0.000246576578246	1175.493	1																



**Table F.8a: Inhomogeneous Anisotropic Case: Forward modelling using  $a$ ,  $b$  and  $\chi$  estimates obtained from offset VSP times for segment 3 with receiver at 1974 m.**

$a = 1275.727651271120$					$b = 0.991031560690$					$\chi = 0.045011486195$					$z = 1973.923$				
offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)
84.530	0.000017413594550	938.717	935.707	-3.010	2011.513	0.000273327501561	1272.425	1269.025	-3.400	2038.012	0.000274600433128	1279.685	1276.389	-3.297					
93.234	0.000019202452677	938.876	935.612	-3.264	2038.012	0.000274600433128	1279.685	1276.389	-3.297	2058.654	0.000275560135536	1285.364	1281.452	-3.912					
112.705	0.000023199865313	939.289	936.244	-3.045	2058.654	0.000275560135536	1285.364	1281.452	-3.912	2089.406	0.000276938995057	1293.859	1291.095	-2.764					
130.648	0.000026876955133	939.738	936.110	-3.628	2089.406	0.000276938995057	1293.859	1291.095	-2.764	2113.127	0.000277961854453	1300.440	1297.340	-3.101					
152.613	0.000031368246441	940.378	937.377	-3.001	2113.127	0.000277961854453	1300.440	1297.340	-3.101	2137.010	0.000278956544946	1307.091	1304.095	-2.996					
176.332	0.000036204208528	941.179	938.209	-2.971	2137.010	0.000278956544946	1307.091	1304.095	-2.996	2162.001	0.000279960254583	1314.075	1308.005	-6.070					
200.664	0.000041147596040	942.120	939.183	-2.938	2162.001	0.000279960254583	1314.075	1308.005	-6.070	2190.353	0.000281053944259	1322.028	1318.307	-3.721					
222.033	0.000045472449116	943.046	940.566	-2.480	2190.353	0.000281053944259	1322.028	1318.307	-3.721	2208.538	0.000281730709470	1327.145	1324.103	-3.042					
244.406	0.00004982283185	944.114	941.458	-2.656	2208.538	0.000281730709470	1327.145	1324.103	-3.042	2240.131	0.000282861395072	1336.064	1332.692	-3.372					
270.447	0.000055205541812	945.483	942.481	-3.002	2240.131	0.000282861395072	1336.064	1332.692	-3.372	2262.848	0.000283639799769	1342.499	1340.505	-1.994					
293.032	0.000059711019831	946.781	944.033	-2.748	2262.848	0.000283639799769	1342.499	1340.505	-1.994	2285.069	0.000284373708916	1348.810	1346.629	-2.181					
317.805	0.000064624688042	948.321	945.562	-2.759	2285.069	0.000284373708916	1348.810	1346.629	-2.181	2313.522	0.000285274524553	1356.914	1354.231	-2.683					
343.415	0.000069670773706	950.041	947.720	-2.321	2313.522	0.000285274524553	1356.914	1354.231	-2.683	2338.818	0.000286039443048	1364.140	1361.689	-2.451					
369.719	0.000074815614082	951.941	949.464	-2.478	2338.818	0.000286039443048	1364.140	1361.689	-2.451	2364.031	0.000286768897092	1371.361	1368.898	-2.463					
393.092	0.000079352911295	953.743	952.038	-1.705	2364.031	0.000286768897092	1371.361	1368.898	-2.463	2387.757	0.000287425899608	1378.173	1376.166	-2.006					
417.457	0.0000840466530893	955.734	953.379	-2.355	2387.757	0.000287425899608	1378.173	1376.166	-2.006	2414.140	0.000288123638338	1385.765	1384.134	-1.631					
443.392	0.00008899806663	957.978	956.346	-1.632	2414.140	0.000288123638338	1385.765	1384.134	-1.631	2438.493	0.000288837643225	1392.789	1389.482	-3.307					
465.151	0.000093119785342	959.959	958.015	-1.944	2438.493	0.000288837643225	1392.789	1389.482	-3.307	2462.794	0.000289322168006	1399.813	1396.500	-3.313					
493.184	0.000098378087702	962.644	960.078	-2.566	2462.794	0.000289322168006	1399.813	1396.500	-3.313	2487.398	0.000289885894324	1406.939	1404.673	-2.266					
515.711	0.000102561134146	964.907	963.346	-1.561	2487.398	0.000289885894324	1406.939	1404.673	-2.266	2515.010	0.000290485614692	1414.951	1412.021	-2.930					
541.511	0.000107304052376	967.614	965.572	-2.042	2515.010	0.000290485614692	1414.951	1412.021	-2.930	2538.668	0.000290972369261	1421.829	1420.411	-1.419					
566.218	0.000111796275579	970.321	968.150	-2.171	2538.668	0.000290972369261	1421.829	1420.411	-1.419	2561.908	0.000291426661165	1428.597	1425.506	-3.091					
594.084	0.000116802789647	973.506	971.846	-1.660	2561.908	0.000291426661165	1428.597	1425.506	-3.091	2586.946	0.000291890208830	1435.899	1432.678	-3.221					
616.525	0.000120786862759	976.172	974.437	-1.736	2586.946	0.000291890208830	1435.899	1432.678	-3.221	2611.466	0.000292318673009	1443.062	1439.409	-3.653					
640.390	0.000124976097795	979.105	977.709	-1.396	2611.466	0.000292318673009	1443.062	1439.409	-3.653	2634.472	0.000292698209739	1449.791	1447.930	-1.861					
666.096	0.000129431814580	982.375	980.848	-1.527	2634.472	0.000292698209739	1449.791	1447.930	-1.861	2664.740	0.000293165167712	1458.658	1457.009	-1.649					
686.674	0.000132955937010	985.075	983.892	-1.183	2664.740	0.000293165167712	1458.658	1457.009	-1.649	2693.145	0.000293570716598	1466.991	1465.913	-1.078					
714.131	0.000137597169253	988.789	987.625	-1.164	2693.145	0.000293570716598	1466.991	1465.913	-1.078	2713.475	0.000293841990950	1472.962	1471.688	-1.274					
734.065	0.000140922578114	991.565	990.735	-0.830	2713.475	0.000293841990950	1472.962	1471.688	-1.274	2737.504	0.000294142631918	1480.027	1478.316	-1.710					
763.765	0.000145807203944	995.823	994.462	-1.362	2737.504	0.000294142631918	1480.027	1478.316	-1.710	2763.498	0.000294444001919	1487.676	1486.156	-1.520					
790.341	0.000150105820233	999.756	998.943	-0.813	2763.498	0.000294444001919	1487.676	1486.156	-1.520	2790.900	0.000294735452183	1495.749	1492.776	-2.972					
818.537	0.000154591029895	1004.051	1002.359	-1.692	2790.900	0.000294735452183	1495.749	1492.776	-2.972	2818.515	0.000295002574784	1503.892	1501.544	-2.348					
838.613	0.000157736565259	1007.187	1006.107	-1.080	2818.515	0.000295002574784	1503.892	1501.544	-2.348	2840.130	0.000295193461914	1510.270	1509.010	-1.261					
864.183	0.000161684850507	1011.271	1009.904	-1.367	2840.130	0.000295193461914	1510.270	1509.010	-1.261	2867.558	0.000295413196827	1518.370	1516.612	-1.758					
889.644	0.000165550505187	1015.437	1014.559	-0.878	2867.558	0.000295413196827	1518.370	1516.612	-1.758	2891.097	0.000295582168688	1525.326	1522.475	-2.851					
916.870	0.000169611604726	1019.999	1018.333	-1.666	2891.097	0.000295582168688	1525.326	1522.475	-2.851	2913.083	0.000295723999208	1531.826	1527.969	-3.857					
938.114	0.000172277790797	1023.636	1022.636	-1.000	2913.083	0.000295723999208	1531.826	1527.969	-3.857	2936.480	0.000295858312530	1538.747	1537.739	-1.008					
967.871	0.000177015160541	1028.840	1028.093	-0.746	2936.480	0.000295858312530	1538.747	1537.739	-1.008	2963.685	0.000295993426883	1546.798	1544.497	-2.301					
984.094	0.000179314068670	1031.730	1032.088	0.358	2963.685	0.000295993426883	1546.798	1544.497	-2.301	2985.984	0.000296087656542	1553.399	1551.710	-1.689					
1014.404	0.000183536632630	1037.229	1035.925	-1.305	2985.984	0.000296087656542	1553.399	1551.710	-1.689	3013.154	0.000296182841104	1561.445	1560.112	-1.333					
1043.220	0.000187463182044	1042.575	1041.995	-0.580	3013.154	0.000296182841104	1561.445	1560.112	-1.333	3037.280	0.000296249697852	1568.591	1566.471	-2.121					
1065.184	0.000190398221240	1046.724	1046.384	-0.340	3037.280	0.000296249697852	1568.591	1566.471	-2.121	3062.143	0.000296301621727	1575.958	1575.806	-0.152					
1088.895	0.000193510951010	1051.276	1050.471	-0.806	3062.143	0.000296301621727	1575.958	1575.806	-0.152	3087.867	0.000296373630921	1583.580	1582.710	-0.871					
1115.015	0.000196872638882	1056.375	1055.210	-1.165	3087.867	0.000296373630921	1583.580	1582.710	-0.871	3113.355	0.000296355965042	1591.134	1587.800	-3.333					
1140.098	0.000200034830404	1061.353	1060.235	-1.118	3113.355	0.000296355965042	1591.134	1587.800	-3.333	3137.870	0.000296357698345	1598.399	1597.852	-0.547					
1165.295	0.000203146245076	1066.432	1065.256	-1.176	3137.870	0.000296357698345	1598.399	1597.852	-0.547	3163.910	0.000296342873308	1606.116	1605.218	-0.898					
1187.085	0.000205784615494	1070.888	1070.389	-0.499	3163.910	0.000296342873308	1606.116	1605.218	-0.898	3187.722	0.000296314642529	1613.172	1614.170	0.998					
1214.352	0.000209017977982	1076.543	1075.694	-0.849	3187.722	0.000296314642529	1613.172	1614.170	0.998	3214.578	0.000296266391863	1621.129	1620.041	-1.088					
1238.248	0.000211789761603	1081.571	1080.502	-1.070	3214.578	0.000296266391863	1621.129	1620.041	-1.088	3236.351	0.000296214800984	1627.579	1627.195	-0.384					
1262.578	0.000214552636599	1086.758	1085.769	-0.989	3236.351	0.000296214800984	1627.579	1627.195	-0.384	3259.675	0.000296147432782	1634.487	1634.435	-0.053					
1288.093	0.000217386388841	1092.268	1092.119	-0.149	3259.675	0.000296147432782	1634.487	1634.435	-0.053	3288.287	0.000296048092463	1642.960	1645.422	2.463					
1312.260	0.000220010730922	1097.554	1097.591	0.037	3288.287	0.000296048092463	1642.960	1645.422	2.463	3312.831	0.000295948585469	1650.224	1651.273	1.049					
1337.566	0.000222696995141	1103.155	1102.887	-0.268	3312.831	0.000295948585469	1650.224	1651.273	1.049	3338.804	0.000295829275148	1657.910	1660.710	2.801					
1366.579	0.000225699613392	1109.660	1110.075	0.415	3338.804	0.000295829275148	1657.910	1660.710	2.801	3361.215	0.000295715031928	1664.538	1665.429	0.890					
1386.806	0.000227744648859	1114.246	1113.877	-0.369	3361.215	0.0002957													



**Table F.8b: Inhomogeneous Anisotropic Case: Forward modelling using  $a$ ,  $b$  and  $\chi$  estimates obtained from offset VSP times for segment 3 with receiver at 2014 m.**

$a = 1275.727651271120$					$b = 0.991031560690$					$\chi = 0.045011486195$					$x = 2013.927$				
offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)
47.917	0.00009597374003	950.513	949.852	-0.661	2031.400	0.000269477929025	1282.605	1283.866	1.261	2031.400	0.000269477929025	1282.605	1283.866	1.261	2031.400	0.000269477929025	1282.605	1283.866	1.261
67.679	0.000013551372420	950.742	950.437	-0.304	2057.867	0.000270736300021	1289.754	1290.939	1.185	2057.867	0.000270736300021	1289.754	1290.939	1.185	2057.867	0.000270736300021	1289.754	1290.939	1.185
87.531	0.000017518924973	951.050	950.647	-0.403	2078.568	0.000271689536234	1295.368	1296.333	0.965	2078.568	0.000271689536234	1295.368	1296.333	0.965	2078.568	0.000271689536234	1295.368	1296.333	0.965
114.917	0.000022982910238	951.605	951.544	-0.061	2109.336	0.000273057035682	1303.749	1305.118	1.369	2109.336	0.000273057035682	1303.749	1305.118	1.369	2109.336	0.000273057035682	1303.749	1305.118	1.369
136.226	0.000027225069039	952.140	951.374	-0.766	2133.030	0.000274070623295	1310.231	1311.261	1.030	2133.030	0.000274070623295	1310.231	1311.261	1.030	2133.030	0.000274070623295	1310.231	1311.261	1.030
159.548	0.000031856567481	952.829	953.025	0.196	2156.926	0.000275058740235	1316.792	1317.697	0.905	2156.926	0.000275058740235	1316.792	1317.697	0.905	2156.926	0.000275058740235	1316.792	1317.697	0.905
185.804	0.000037053965192	953.733	953.865	0.132	2181.962	0.000276057860980	1323.690	1322.426	-1.265	2181.962	0.000276057860980	1323.690	1322.426	-1.265	2181.962	0.000276057860980	1323.690	1322.426	-1.265
210.975	0.000042017531823	954.728	954.950	0.222	2210.257	0.000277143461824	1331.517	1332.953	1.436	2210.257	0.000277143461824	1331.517	1332.953	1.436	2210.257	0.000277143461824	1331.517	1332.953	1.436
234.325	0.000046603032428	955.763	956.605	0.842	2228.452	0.000277817563466	1336.566	1338.401	1.836	2228.452	0.000277817563466	1336.566	1338.401	1.836	2228.452	0.000277817563466	1336.566	1338.401	1.836
258.040	0.000051239709169	956.923	957.373	0.450	2260.084	0.0002789456604024	1345.372	1346.712	1.341	2260.084	0.0002789456604024	1345.372	1346.712	1.341	2260.084	0.0002789456604024	1345.372	1346.712	1.341
284.557	0.000056397338438	958.350	958.386	0.035	2282.716	0.000279719171955	1351.694	1353.271	1.578	2282.716	0.000279719171955	1351.694	1353.271	1.578	2282.716	0.000279719171955	1351.694	1353.271	1.578
307.433	0.000060821922417	959.691	960.111	0.419	2304.890	0.000280450498439	1357.904	1359.676	1.772	2304.890	0.000280450498439	1357.904	1359.676	1.772	2304.890	0.000280450498439	1357.904	1359.676	1.772
332.872	0.000065713061630	961.301	961.630	0.329	2333.394	0.000281352638348	1365.911	1367.060	1.149	2333.394	0.000281352638348	1365.911	1367.060	1.149	2333.394	0.000281352638348	1365.911	1367.060	1.149
359.049	0.000070711732476	963.086	963.944	0.857	2358.739	0.000282119661133	1373.052	1375.573	2.521	2358.739	0.000282119661133	1373.052	1375.573	2.521	2358.739	0.000282119661133	1373.052	1375.573	2.521
385.343	0.000075695188041	965.011	965.418	0.406	2383.962	0.000282850876211	1380.177	1382.318	2.141	2383.962	0.000282850876211	1380.177	1382.318	2.141	2383.962	0.000282850876211	1380.177	1382.318	2.141
409.334	0.000080207666384	966.882	968.447	1.566	2407.702	0.000283510389113	1386.900	1389.120	2.220	2407.702	0.000283510389113	1386.900	1389.120	2.220	2407.702	0.000283510389113	1386.900	1389.120	2.220
433.705	0.000084755089671	968.902	969.921	1.019	2434.097	0.000284211619738	1394.392	1396.500	2.108	2434.097	0.000284211619738	1394.392	1396.500	2.108	2434.097	0.000284211619738	1394.392	1396.500	2.108
460.001	0.000089620743727	971.185	972.838	1.653	2458.515	0.000284830878033	1401.340	1403.233	1.893	2458.515	0.000284830878033	1401.340	1403.233	1.893	2458.515	0.000284830878033	1401.340	1403.233	1.893
482.029	0.000093660863360	973.203	974.457	1.253	2482.793	0.000285419129935	1408.262	1410.509	2.247	2482.793	0.000285419129935	1408.262	1410.509	2.247	2482.793	0.000285419129935	1408.262	1410.509	2.247
509.907	0.000098725794113	975.885	976.609	0.724	2507.442	0.000285988908045	1415.304	1418.106	2.802	2507.442	0.000285988908045	1415.304	1418.106	2.802	2507.442	0.000285988908045	1415.304	1418.106	2.802
532.777	0.00010283994265	978.190	979.967	1.777	2535.041	0.000286594723762	1423.206	1425.056	1.850	2535.041	0.000286594723762	1423.206	1425.056	1.850	2535.041	0.000286594723762	1423.206	1425.056	1.850
558.748	0.000107463268028	980.921	981.933	1.012	2558.701	0.000287087060435	1429.993	1432.211	2.218	2558.701	0.000287087060435	1429.993	1432.211	2.218	2558.701	0.000287087060435	1429.993	1432.211	2.218
583.493	0.000111820960993	983.634	985.107	1.472	2581.986	0.000287549301929	1436.683	1439.055	2.372	2581.986	0.000287549301929	1436.683	1439.055	2.372	2581.986	0.000287549301929	1436.683	1439.055	2.372
611.554	0.000116704047358	986.841	988.531	1.690	2607.071	0.000288021270694	1443.902	1445.480	1.578	2607.071	0.000288021270694	1443.902	1445.480	1.578	2607.071	0.000288021270694	1443.902	1445.480	1.578
634.129	0.000120586047398	989.519	991.086	1.566	2631.588	0.000288457599563	1450.969	1452.599	1.630	2631.588	0.000288457599563	1450.969	1452.599	1.630	2631.588	0.000288457599563	1450.969	1452.599	1.630
658.248	0.000124686839373	992.477	994.422	1.945	2654.653	0.000288846027576	1457.627	1459.835	2.208	2654.653	0.000288846027576	1457.627	1459.835	2.208	2654.653	0.000288846027576	1457.627	1459.835	2.208
684.072	0.000129022706676	995.753	997.434	1.681	2684.768	0.000289321690745	1466.333	1469.199	2.866	2684.768	0.000289321690745	1466.333	1469.199	2.866	2684.768	0.000289321690745	1466.333	1469.199	2.866
705.124	0.000132514614962	998.506	1000.876	2.370	2713.012	0.000289736148143	1474.510	1477.709	3.199	2713.012	0.000289736148143	1474.510	1477.709	3.199	2713.012	0.000289736148143	1474.510	1477.709	3.199
732.526	0.000137001082576	1002.199	1004.018	1.819	2733.279	0.000290015102455	1480.385	1482.503	2.118	2733.279	0.000290015102455	1480.385	1482.503	2.118	2733.279	0.000290015102455	1480.385	1482.503	2.118
752.696	0.000140260617631	1004.995	1007.432	2.437	2757.260	0.000290325665409	1487.344	1489.196	1.853	2757.260	0.000290325665409	1487.344	1489.196	1.853	2757.260	0.000290325665409	1487.344	1489.196	1.853
782.323	0.000144981223322	1009.221	1011.254	2.033	2783.262	0.000290639001536	1494.897	1497.292	2.395	2783.262	0.000290639001536	1494.897	1497.292	2.395	2783.262	0.000290639001536	1494.897	1497.292	2.395
809.041	0.000149168786763	1013.151	1015.565	2.414	2810.670	0.000290943514117	1502.867	1504.319	1.452	2810.670	0.000290943514117	1502.867	1504.319	1.452	2810.670	0.000290943514117	1502.867	1504.319	1.452
837.034	0.000153484864445	1017.387	1019.073	1.686	2838.309	0.00029124446651	1510.912	1512.353	1.441	2838.309	0.00029124446651	1510.912	1512.353	1.441	2838.309	0.00029124446651	1510.912	1512.353	1.441
857.170	0.000156543066667	1020.508	1022.852	2.344	2859.972	0.000291426700969	1517.223	1519.220	1.996	2859.972	0.000291426700969	1517.223	1519.220	1.996	2859.972	0.000291426700969	1517.223	1519.220	1.996
882.753	0.000160373096215	1024.562	1026.294	1.732	2887.458	0.000291661124461	1525.237	1526.834	1.597	2887.458	0.000291661124461	1525.237	1526.834	1.597	2887.458	0.000291661124461	1525.237	1526.834	1.597
908.363	0.000164144207724	1028.718	1031.885	3.167	2911.043	0.000291842932914	1532.118	1534.916	2.798	2911.043	0.000291842932914	1532.118	1534.916	2.798	2911.043	0.000291842932914	1532.118	1534.916	2.798
935.422	0.000168059450971	1033.212	1034.363	1.151	2933.070	0.000291996931697	1538.548	1540.726	2.178	2933.070	0.000291996931697	1538.548	1540.726	2.178	2933.070	0.000291996931697	1538.548	1540.726	2.178
956.725	0.000171091741750	1036.825	1038.713	1.888	2956.504	0.000292144373679	1545.392	1548.725	3.333	2956.504	0.000292144373679	1545.392	1548.725	3.333	2956.504	0.000292144373679	1545.392	1548.725	3.333
986.543	0.000175261427370	1041.989	1044.700	2.711	2983.778	0.000292295150627	1553.362	1555.046	1.683	2983.778	0.000292295150627	1553.362	1555.046	1.683	2983.778	0.000292295150627	1553.362	1555.046	1.683
1002.869	0.000177507236237	1044.869	1049.014	4.145	3006.069	0.000292402104354	1559.879	1562.470	2.591	3006.069	0.000292402104354	1559.879	1562.470	2.591	3006.069	0.000292402104354	1559.879	1562.470	2.591
1033.179	0.000181607355804	1050.111	1052.495	2.383	3033.245	0.000292531162491	1567.827	1570.417	2.590	3033.245	0.000292531162491	1567.827	1570.417	2.590	3033.245	0.000292531162491	1567.827	1570.417	2.590
1061.975																			



**Table F.9a:** Inhomogeneous Anisotropic Case: Forward modelling using  $a$ ,  $b$  and  $\chi$  estimates obtained from offset VSP times for segment 4 with receiver at 1974 m.

$a = 1347.931539688680$					$b = 0.884981169823$					$\chi = 0.065305746933$					$x = 1973.923$				
offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)
84.530	0.000017034880302	939.901	935.707	-4.194	2011.513	0.000274122629927	1270.614	1269.025	-1.589										
93.234	0.000018785090694	940.057	935.612	-4.445	2038.012	0.000275533305612	1277.897	1276.389	-1.508										
112.705	0.000022696423500	940.461	936.244	-4.217	2058.654	0.000276601210772	1283.596	1281.452	-2.144										
130.648	0.000026294731928	940.900	936.110	-4.790	2089.406	0.000278142634885	1292.125	1291.095	-1.031										
152.613	0.000030690411467	941.526	937.377	-4.149	2113.127	0.000279291948329	1298.737	1297.340	-1.397										
176.332	0.000035424302294	942.310	938.209	-4.102	2137.010	0.000280414823679	1305.421	1304.095	-1.326										
200.664	0.000040264438563	943.231	939.183	-4.049	2162.001	0.000281553528606	1312.443	1308.005	-4.438										
222.033	0.00004499982698	944.137	940.566	-3.570	2190.353	0.000282801367518	1320.443	1318.307	-2.136										
244.406	0.000048917824561	945.182	941.458	-3.724	2208.538	0.000283757522098	1325.593	1324.103	-1.490										
270.447	0.000054036147011	946.522	942.481	-4.041	2240.131	0.000284881754263	1334.573	1332.692	-1.881										
293.032	0.000058452636685	947.793	944.033	-3.760	2262.848	0.000285785589649	1341.055	1340.505	-0.550										
317.805	0.000063271022896	949.301	945.562	-3.739	2285.069	0.000286642655550	1347.415	1346.629	-0.786										
343.415	0.000068221350033	950.984	947.720	-3.265	2313.522	0.000287701776683	1355.586	1354.231	-1.355										
369.719	0.000073270929951	952.845	949.464	-3.382	2338.818	0.000288607950932	1362.875	1361.689	-1.186										
393.092	0.00007726363080	954.610	952.038	-2.572	2364.031	0.000289478621626	1370.163	1368.898	-1.265										
417.457	0.000082337573934	956.560	953.379	-3.181	2387.757	0.000290268853212	1377.041	1376.166	-0.874										
443.392	0.000087206569064	958.759	956.346	-2.413	2414.140	0.000291115070658	1384.710	1384.134	-0.576										
465.151	0.000091258864626	960.700	958.015	-2.685	2438.493	0.000291866392485	1391.809	1389.482	-2.326										
493.184	0.000096433530392	963.331	960.078	-3.254	2462.794	0.000292588143421	1398.910	1396.500	-2.410										
515.711	0.000100522636111	965.550	963.346	-2.204	2487.398	0.000293290967220	1406.118	1404.673	-1.445										
541.511	0.000105226591981	968.205	965.572	-2.633	2515.010	0.000294046930396	1414.226	1412.021	-2.205										
566.218	0.00010956444886	970.859	968.150	-2.709	2538.668	0.000294667633327	1421.191	1420.411	-0.780										
594.084	0.000114597291931	973.984	971.846	-2.138	2561.908	0.000295253530062	1428.045	1425.506	-2.540										
616.525	0.000118532166379	976.600	974.437	-2.163	2586.946	0.000295858859704	1435.446	1432.678	-2.768										
640.390	0.000122672750671	979.478	977.709	-1.770	2611.466	0.000296426126789	1442.707	1439.409	-3.298										
666.096	0.000127080367278	982.688	980.848	-1.841	2634.472	0.000296935816611	1449.533	1447.930	-1.603										
686.674	0.000130569238798	985.340	983.892	-1.448	2664.740	0.000297573846661	1458.530	1457.009	-1.521										
714.131	0.000135168001423	988.988	987.625	-1.363	2693.145	0.000298139716147	1466.991	1465.913	-1.078										
734.065	0.000138465874302	991.715	990.735	-0.980	2713.475	0.000298525567574	1473.056	1471.688	-1.368										
763.765	0.000143314660573	995.900	994.462	-1.438	2737.504	0.000298961423888	1480.234	1478.316	-1.918										
790.341	0.000147586502881	999.765	998.943	-0.823	2763.498	0.000299408780058	1488.011	1486.156	-1.855										
818.537	0.000152048798808	1003.990	1002.359	-1.631	2790.900	0.000299853764457	1496.222	1492.776	-3.445										
838.613	0.000155181474239	1007.074	1006.107	-0.967	2818.515	0.000300275196382	1504.508	1501.544	-2.965										
864.183	0.000159117277987	1011.092	1009.904	-1.188	2840.130	0.000300586546909	1511.002	1509.010	-1.993										
889.644	0.000162975663823	1015.193	1015.459	0.266	2867.558	0.000300958695872	1519.252	1516.612	-2.640										
916.870	0.000167033805258	1019.686	1018.333	-1.352	2891.097	0.000301258052820	1526.340	1522.475	-3.865										
938.114	0.000170151328488	1023.267	1022.636	-0.631	2913.083	0.000301521298040	1532.966	1527.969	-4.997										
967.871	0.000174445913874	1028.394	1028.093	-0.301	2936.480	0.000301784398540	1540.024	1537.739	-2.285										
984.094	0.000176751365573	1031.243	1032.088	0.845	2963.685	0.000302068698443	1548.238	1544.497	-3.741										
1014.404	0.000180991050398	1036.665	1035.925	-0.740	2985.984	0.000302284726100	1554.976	1551.710	-3.266										
1043.220	0.000184939734991	1041.938	1041.995	0.058	3013.154	0.000302527708894	1563.192	1560.112	-3.081										
1065.184	0.000187895453431	1046.032	1046.384	0.352	3037.280	0.00030275223191	1570.494	1566.471	-4.023										
1088.895	0.000191034108912	1050.525	1050.471	-0.054	3062.143	0.000302911197517	1578.023	1575.806	-2.217										
1115.015	0.000194428692814	1055.559	1055.210	-0.349	3087.867	0.000303085239153	1585.817	1582.710	-3.108										
1140.098	0.000197626675935	1060.476	1060.235	-0.241	3113.355	0.000303239652968	1593.544	1587.800	-5.744										
1165.295	0.000200778123168	1065.495	1065.256	-0.239	3137.870	0.000303371604994	1600.980	1597.852	-3.128										
1187.085	0.000203454359188	1069.900	1070.389	0.489	3163.910	0.000303494362376	1608.881	1605.218	-3.663										
1214.352	0.000206739272053	1075.492	1075.694	0.202	3187.722	0.000303591262625	1616.109	1614.170	-1.939										
1238.248	0.000209559976715	1080.466	1080.502	0.035	3214.578	0.000303683339959	1624.264	1620.041	-4.222										
1262.578	0.000212376180338	1085.599	1085.769	0.170	3236.351	0.000303744878128	1630.877	1627.195	-3.681										
1288.093	0.000215269599056	1091.055	1092.119	1.064	3259.675	0.000303798046722	1637.962	1634.435	-3.527										
1312.260	0.000217953912883	1096.290	1097.591	1.301	3288.287	0.000303845644805	1646.655	1645.422	-1.233										
1337.566	0.000220706500945	1101.841	1102.887	1.046	3312.831	0.000303871344018	1654.112	1651.273	-2.839										
1366.579	0.000223789487205	1108.289	1110.075	1.787	3338.804	0.000303883677531	1662.005	1660.710	-1.295										
1386.806	0.0002258932323524	1112.837	1113.877	1.040	3361.215	0.000303882300511	1668.815	1665.429	-3.387										
1413.235	0.000228586072156	1118.842	1120.171	1.328	3387.640	0.000303866688789	1676.846	1674.863	-1.983										
1434.249	0.000230682274404	1123.668	1125.078	1.410	3405.836	0.000303847313924	1682.374	1681.033	-1.341										
1457.820	0.00023298663172	1129.133	1129.865	0.732	3438.279	0.000303795714058	1692.231	1690.683	-1.548										
1485.368	0.000235617493175	1135.587	1136.798	1.211	3462.882	0.000303742343747	1699.705	1698.660	-1.045										
1513.211	0.000238209145077	1142.184	1143.508	1.324	3488.647	0.000303673607998	1707.530	1706.745	-0.786										
1539.303	0.000240576905552	1148.430	1149.417	0.986	3512.857	0.000303597318105	1714.881	1712.753	-2.128										
1565.130	0.000242863363700	1154.673	1154.933	0.259	3539.715	0.000303499722545	1723.034	1720.417	-2.617										
1588.644	0.000244896048707	1160.408	1160.874	0.466	3562.825	0.000303405076289	1730.047	1724.573	-5.474										
1612.475	0.000246909123601	1166.268	1167.062	0.794	3586.331	0.00													



**Table F.9b: Inhomogeneous Anisotropic Case: Forward modelling using  $a$ ,  $b$  and  $\chi$  estimates obtained from offset VSP times for segment 4 with receiver at 2014 m.**

$a = 1347.931539688680$					$b = 0.884981169823$					$\chi = 0.065305746933$					$x = 2013.927$				
offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)	offset (m)	$p$	computed time (ms)	observed time (ms)	residual (ms)
47.917	0.00009395937084	952.259	949.852	-2.407	2031.400	0.000270438693884	1281.602	1283.866	2.263	2031.400	0.000270438693884	1281.602	1283.866	2.263	2031.400	0.000270438693884	1281.602	1283.866	2.263
67.679	0.000013267205690	952.483	950.437	-2.046	2057.867	0.000271831834381	1288.778	1290.939	2.160	2057.867	0.000271831834381	1288.778	1290.939	2.160	2057.867	0.000271831834381	1288.778	1290.939	2.160
87.531	0.000017152012800	952.785	950.647	-2.137	2078.568	0.000272891346433	1294.417	1296.333	1.916	2078.568	0.000272891346433	1294.417	1296.333	1.916	2078.568	0.000272891346433	1294.417	1296.333	1.916
114.917	0.000022502628735	953.328	951.544	-1.784	2109.336	0.000274418127137	1302.837	1305.118	2.281	2109.336	0.000274418127137	1302.837	1305.118	2.281	2109.336	0.000274418127137	1302.837	1305.118	2.281
136.226	0.000026657356263	953.851	951.374	-2.477	2133.030	0.00027555379606	1309.352	1311.261	1.908	2133.030	0.00027555379606	1309.352	1311.261	1.908	2133.030	0.00027555379606	1309.352	1311.261	1.908
159.548	0.000031194111175	954.526	953.025	-1.501	2156.926	0.000276669045626	1315.950	1317.697	1.746	2156.926	0.000276669045626	1315.950	1317.697	1.746	2156.926	0.000276669045626	1315.950	1317.697	1.746
185.804	0.000036286229626	955.412	953.865	-1.547	2181.962	0.00027800534381	1322.891	1322.426	-0.466	2181.962	0.00027800534381	1322.891	1322.426	-0.466	2181.962	0.00027800534381	1322.891	1322.426	-0.466
210.975	0.000041150443927	956.387	954.950	-1.437	2210.257	0.000279036691003	1330.769	1332.953	2.184	2210.257	0.000279036691003	1330.769	1332.953	2.184	2210.257	0.000279036691003	1330.769	1332.953	2.184
234.325	0.000045645336327	957.400	956.605	-0.795	2228.452	0.000279808105462	1335.853	1338.401	2.548	2228.452	0.000279808105462	1335.853	1338.401	2.548	2228.452	0.000279808105462	1335.853	1338.401	2.548
258.040	0.000050191679189	958.536	957.373	-1.163	2260.084	0.000281106167080	1344.725	1346.712	1.987	2260.084	0.000281106167080	1344.725	1346.712	1.987	2260.084	0.000281106167080	1344.725	1346.712	1.987
284.557	0.000055250510134	959.934	958.386	-1.549	2282.716	0.000282001990510	1351.097	1353.271	2.174	2282.716	0.000282001990510	1351.097	1353.271	2.174	2282.716	0.000282001990510	1351.097	1353.271	2.174
307.433	0.000059591892602	961.248	960.111	-1.138	2304.890	0.00028353546059	1357.360	1359.676	2.317	2304.890	0.00028353546059	1357.360	1359.676	2.317	2304.890	0.00028353546059	1357.360	1359.676	2.317
332.872	0.000064392884894	962.825	961.630	-1.195	2333.394	0.000283910820027	1365.437	1367.060	1.623	2333.394	0.000283910820027	1365.437	1367.060	1.623	2333.394	0.000283910820027	1365.437	1367.060	1.623
359.049	0.000069301582419	964.575	963.944	-0.631	2358.739	0.000284816278575	1372.644	1375.573	2.928	2358.739	0.000284816278575	1372.644	1375.573	2.928	2358.739	0.000284816278575	1372.644	1375.573	2.928
385.343	0.000074197692143	966.462	965.418	-1.044	2383.962	0.000285685676718	1379.839	1382.318	2.479	2383.962	0.000285685676718	1379.839	1382.318	2.479	2383.962	0.000285685676718	1379.839	1382.318	2.479
409.334	0.000078633266098	968.295	968.447	0.152	2407.702	0.000286475575365	1386.631	1389.120	2.488	2407.702	0.000286475575365	1386.631	1389.120	2.488	2407.702	0.000286475575365	1386.631	1389.120	2.488
433.705	0.000083106152550	970.266	969.921	-0.345	2434.097	0.000287322091259	1394.204	1396.500	2.296	2434.097	0.000287322091259	1394.204	1396.500	2.296	2434.097	0.000287322091259	1394.204	1396.500	2.296
460.001	0.000087993267459	972.514	972.838	0.324	2458.515	0.000288076000716	1401.229	1403.233	2.004	2458.515	0.000288076000716	1401.229	1403.233	2.004	2458.515	0.000288076000716	1401.229	1403.233	2.004
482.029	0.000091871002291	974.494	974.457	-0.038	2482.793	0.000288798331235	1408.232	1410.509	2.278	2482.793	0.000288798331235	1408.232	1410.509	2.278	2482.793	0.000288798331235	1408.232	1410.509	2.278
509.907	0.000096860782417	977.125	976.609	-0.516	2507.442	0.000289504394162	1415.359	1418.106	2.747	2507.442	0.000289504394162	1415.359	1418.106	2.747	2507.442	0.000289504394162	1415.359	1418.106	2.747
532.777	0.000100915705138	979.387	979.967	0.580	2535.041	0.000290262939964	1423.360	1425.056	1.696	2535.041	0.000290262939964	1423.360	1425.056	1.696	2535.041	0.000290262939964	1423.360	1425.056	1.696
558.748	0.000105477263909	982.067	981.933	-0.134	2558.701	0.000290886827482	1430.235	1432.211	1.976	2558.701	0.000290886827482	1430.235	1432.211	1.976	2558.701	0.000290886827482	1430.235	1432.211	1.976
583.493	0.000109779034433	984.730	985.107	0.376	2581.986	0.000291477477552	1437.015	1439.055	2.040	2581.986	0.000291477477552	1437.015	1439.055	2.040	2581.986	0.000291477477552	1437.015	1439.055	2.040
611.554	0.000114603221915	987.879	988.531	0.652	2607.071	0.000292088362496	1444.334	1445.480	1.146	2607.071	0.000292088362496	1444.334	1445.480	1.146	2607.071	0.000292088362496	1444.334	1445.480	1.146
634.129	0.000118441394268	990.509	991.086	0.576	2631.588	0.000292660417695	1451.503	1452.599	1.096	2631.588	0.000292660417695	1451.503	1452.599	1.096	2631.588	0.000292660417695	1451.503	1452.599	1.096
658.248	0.00012249825119	993.415	994.422	1.007	2654.653	0.000293176460279	1458.259	1459.835	1.576	2654.653	0.000293176460279	1458.259	1459.835	1.576	2654.653	0.000293176460279	1458.259	1459.835	1.576
684.072	0.000126792617113	996.634	997.434	0.800	2684.768	0.000293818584388	1467.097	1469.199	2.101	2684.768	0.000293818584388	1467.097	1469.199	2.101	2684.768	0.000293818584388	1467.097	1469.199	2.101
705.124	0.0001302535353981	999.340	1000.876	1.536	2713.012	0.000294388945858	1475.404	1477.709	2.305	2713.012	0.000294388945858	1475.404	1477.709	2.305	2713.012	0.000294388945858	1475.404	1477.709	2.305
732.526	0.000134703616122	1002.970	1004.018	1.048	2733.279	0.000294779618038	1481.375	1482.503	1.129	2733.279	0.000294779618038	1481.375	1482.503	1.129	2733.279	0.000294779618038	1481.375	1482.503	1.129
752.696	0.000137939682831	1005.720	1007.432	1.713	2757.260	0.000295222170511	1488.449	1489.196	0.747	2757.260	0.000295222170511	1488.449	1489.196	0.747	2757.260	0.000295222170511	1488.449	1489.196	0.747
782.323	0.000142630747943	1009.876	1011.254	1.378	2783.262	0.000295678345799	1496.131	1497.292	1.160	2783.262	0.000295678345799	1496.131	1497.292	1.160	2783.262	0.000295678345799	1496.131	1497.292	1.160
809.041	0.000146796731247	1013.743	1015.565	1.822	2810.670	0.000296133072729	1504.242	1504.319	0.077	2810.670	0.000296133072729	1504.242	1504.319	0.077	2810.670	0.000296133072729	1504.242	1504.319	0.077
837.034	0.00015095070901	1017.912	1019.073	1.161	2838.309	0.000296565082731	1512.432	1512.353	-0.079	2838.309	0.000296565082731	1512.432	1512.353	-0.079	2838.309	0.000296565082731	1512.432	1512.353	-0.079
857.170	0.000154144299565	1020.986	1022.852	1.867	2859.972	0.000296885443287	1518.861	1519.220	0.359	2859.972	0.000296885443287	1518.861	1519.220	0.359	2859.972	0.000296885443287	1518.861	1519.220	0.359
882.753	0.00015796507412	1024.978	1026.294	1.316	2887.458	0.000297269286577	1527.026	1526.834	-0.192	2887.458	0.000297269286577	1527.026	1526.834	-0.192	2887.458	0.000297269286577	1527.026	1526.834	-0.192
908.363	0.000161734217376	1029.072	1031.885	2.813	2911.043	0.000297578908650	1534.041	1534.916	0.875	2911.043	0.000297578908650	1534.041	1534.916	0.875	2911.043	0.000297578908650	1534.041	1534.916	0.875
935.422	0.000165650667147	1033.501	1034.363	0.862	2933.070	0.000297851912192	1540.599	1540.726	0.127	2933.070	0.000297851912192	1540.599	1540.726	0.127	2933.070	0.000297851912192	1540.599	1540.726	0.127
956.725	0.000168687364062	1037.063	1038.713	1.651	2956.504	0.000298125562579	1547.582	1548.725	1.143	2956.504	0.000298125562579	1547.582	1548.725	1.143	2956.504	0.000298125562579	1547.582	1548.725	1.143
986.543	0.000172868301365	1042.155	1044.700	2.545	2983.778	0.00029842679435	1555.717	1555.046	-0.671	2983.778	0.00029842679435	1555.717	1555.046	-0.671	2983.778	0.00029842679435	1555.717	1555.046	-0.671
1002.868	0.000175122767489	1044.996	1049.014	4.018	3006.069	0.000298648770741	1562.371	1562.470	0.099	3006.069	0.000298648770741	1562.371	1562.470	0.099	3006.069	0.000298648770741	1562.371	1562.470	0.099
1033.179	0.000179243608370	1050.366	1052.495	2.128	3033.245	0.000298904493463	1570.491	1570.417	-0.075	3033.245	0.000298904493463	1570.491	1570.417	-0.075	3033.245	0.000298904493463	1570.491	1570.417	-0.075
1061.975	0.0001830801																		

## **APPENDIX G**

### **Elliptical Rays - Upgoing and Downgoing signals**



Equations used:

$x$  corresponding to maximum of the takeoff angle (turning point) at depth  $Z$ :

$$x = \sqrt{\frac{1+2\chi}{b}(2a+bZ)Z} . \quad (1.38)$$

$$p(x;Z) = \frac{2x}{\sqrt{[x^2 + (1+2\chi)Z^2] [(2a+bZ)^2(1+2\chi) + b^2x^2]}} , \quad (1.37)$$

Example Calculation:

For receiver at depth,  $Z$ , of 200 m and  $a = 1502.014$ ,  $b = 0.6735$ ,  $\chi = 0.1087$ .

$$x = \text{SQRT}(((1+(2*0.1087))/0.6735)*(((2*1502.014)+(0.6735*200))*200))$$

$$x = 1065.244$$

Substituting for  $x$ ,  $Z$ ,  $a$ ,  $b$ ,  $\chi$  in equation for  $p$  above:

$$p = 0.00055373$$

Since ray parameter,  $p$ , is unique for a particular ray, we can use the expression below to find  $X$  corresponding to  $Z$  along the ray to  $x = 1065.244$  m:

$$X = \frac{1}{pb} \left[ \sqrt{1 - p^2 a^2 (1 + 2\chi)} - \sqrt{1 - p^2 (a + bZ)^2 (1 + 2\chi)} \right] .$$

**Table G.1:** Elliptical Rays and Turning Points Example

$Z$ (m)	$X$ (m)	$Z$ (m)	$X$ (m)
0	0	0	1732.225
100	244.504	100	1487.721
150	423.361	150	1308.864
180	584.882	180	1147.344
190	666.968	190	1065.257
192	687.941	192	1044.284
194	711.768	194	1020.458
196	740.055	196	992.171
197	756.928	197	975.298
198	776.951	198	955.275
199	803.057	199	929.169
200	866.113	200	866.113

This is done for each ray shown in Figures 6.13a and 6.13b. The locus of points corresponding to the turning point for each set of rays is joined by the white curve in Figures 6.13a and 6.13b.











